

Gravitational waves within the magnetar model of superluminous supernovae and gamma-ray bursts

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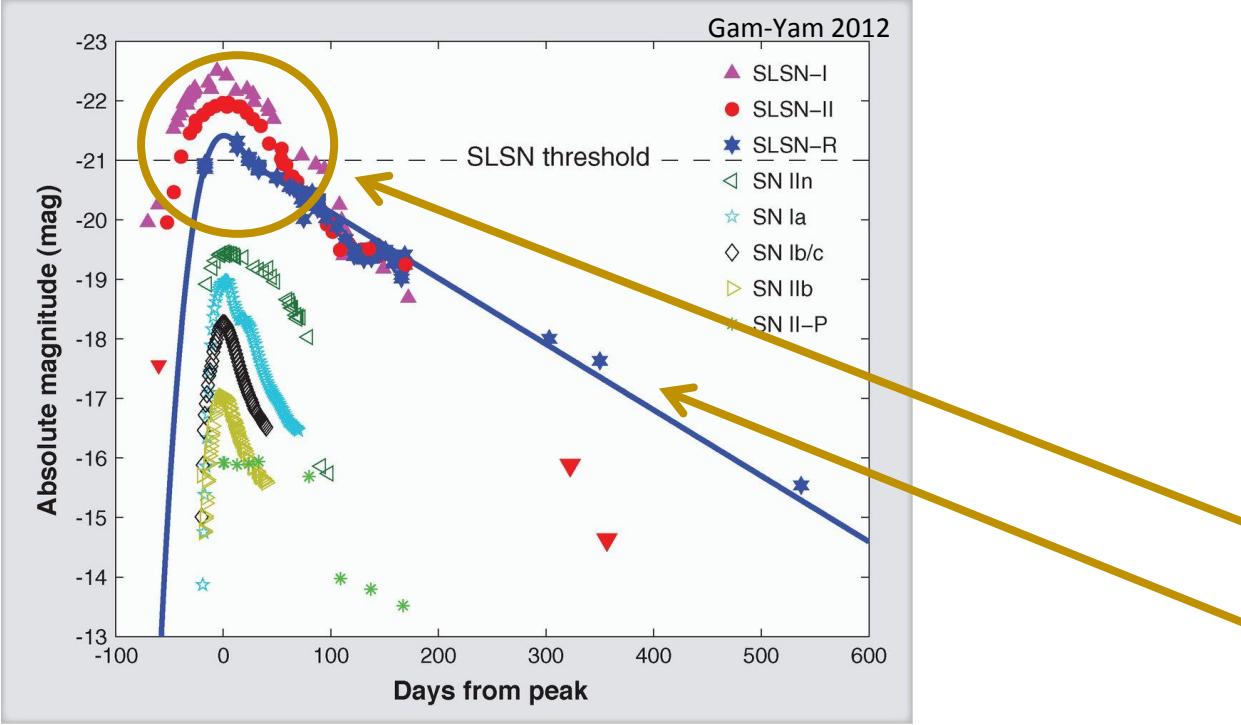
for details, see MNRAS, in press (arXiv:1606.00454)

GRavitational-wave Astronomy Meeting in PAris – 29 August–2 September 2016

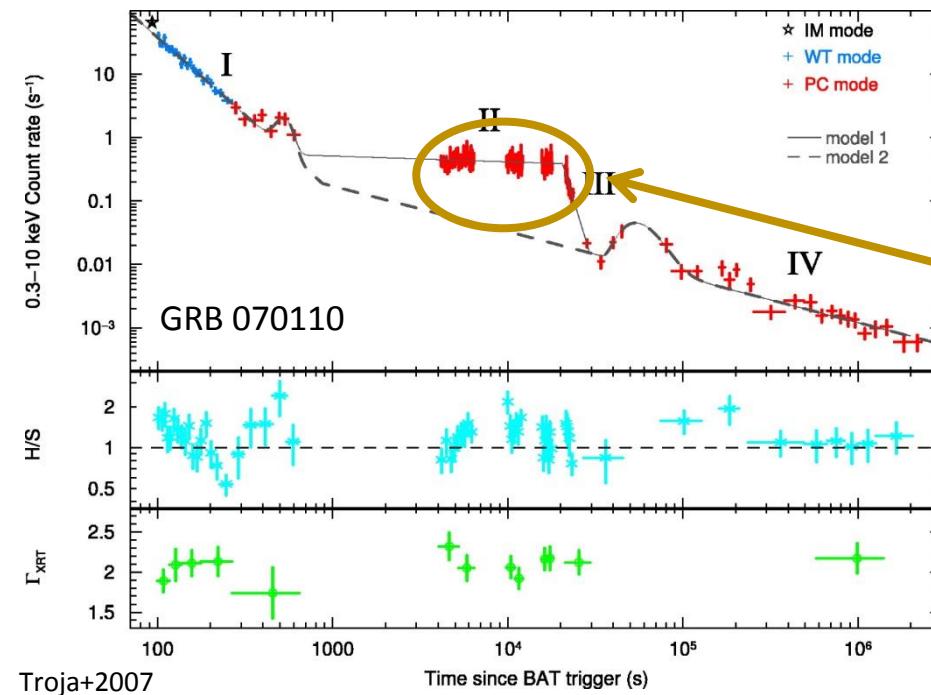
Outline

- Superluminous supernovae (SLSNe) and long-lived gamma-ray bursts (GRBs)
- Magnetars and their spin-down power and timescale
- Millisecond magnetar energy and spin evolution
- Gravitational wave (GW) emission versus electromagnetic dipole radiation
 - simple constraints
 - effect on light curve
- Conclusions

Superluminous supernovae and long-lived gamma-ray bursts



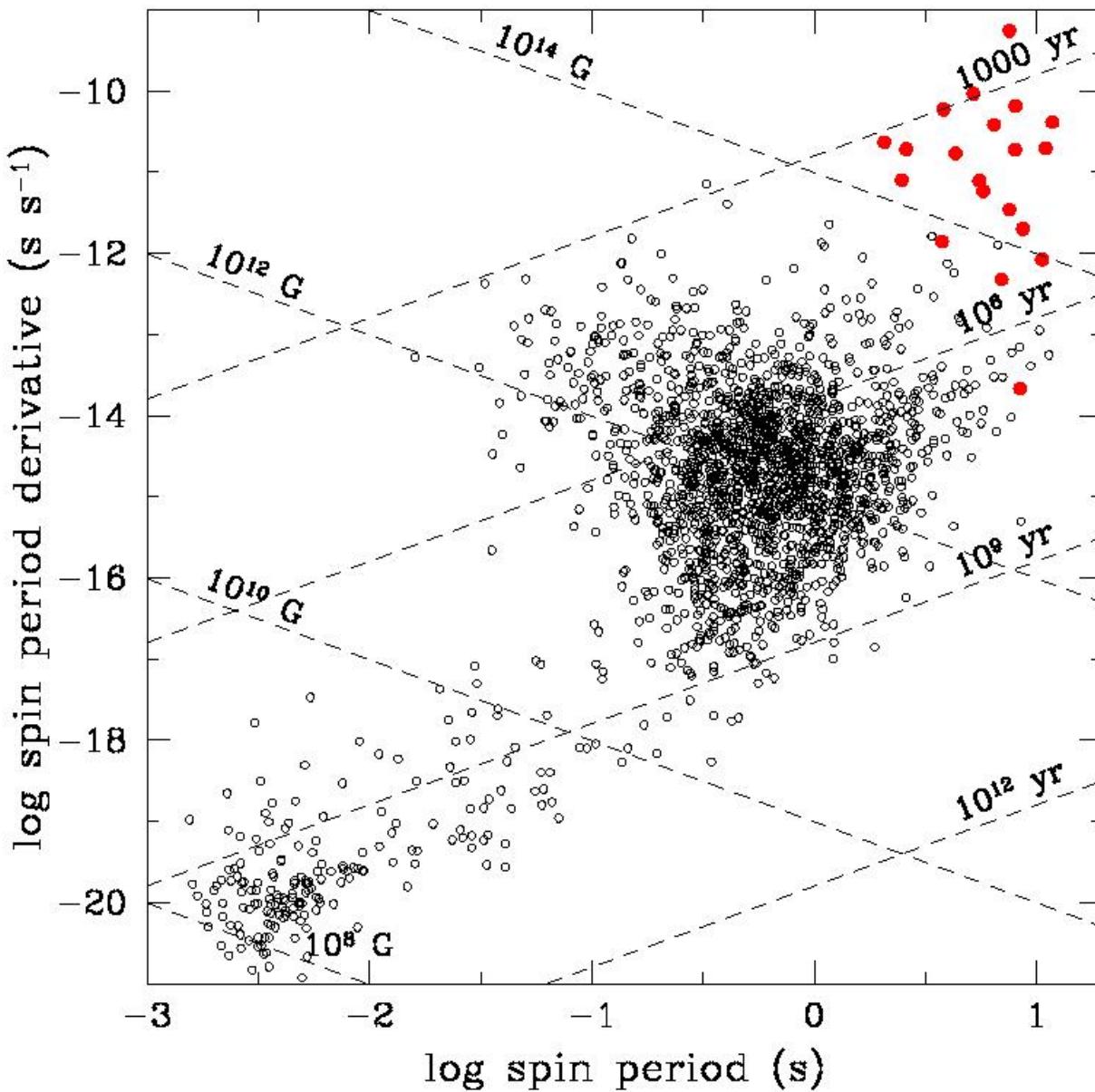
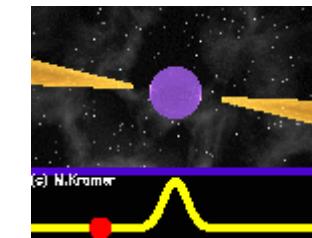
- Superluminous supernovae (SLSNe)
 - more luminous
 - bright at late times ($\sim 10\text{--}100$ of days)



- Long-lived gamma-ray bursts (GRBs)
 - subset of short and long GRBs
 - bright late-time plateau – extra energy for prolonged time ($\sim 10^4$ s)

Neutron star spins and magnetic fields

see talks by Kramer and Lentati



- $P-\dot{P}$ diagram: measured spin period and time derivative
 - millisecond pulsars $B \sim 10^8 - 10^{10}$ G
 - radio pulsars $B \sim 10^{11} - 10^{13}$ G
 - **magnetars** $B \sim 10^{13} - 10^{15}$ G
- Rotational energy $E_{\text{rot}} = I\Omega^2/2 = 2 \times 10^{52}$ erg ($P/1$ ms) $^{-2}$
- Magnetic dipole radiation
 - energy loss $L_{\text{mag}} \equiv \dot{E}_{\text{mag}} \sim -B^2 R^6 \Omega^4 / c^3$
 - timescale $t_{\text{mag}} = |E_{\text{rot}} / \dot{E}_{\text{mag}}| = 2 \times 10^5$ s B_{14}^{-2} ($P/1$ ms) 2
 - infer magnetic field with $\dot{E}_{\text{rot}} \equiv I\Omega\dot{\Omega} = 4\pi^2 \dot{P}/P^3 = L_{\text{mag}}$
 $\Rightarrow B = 3.2 \times 10^{19}$ G $(P\dot{P})^{1/2}$

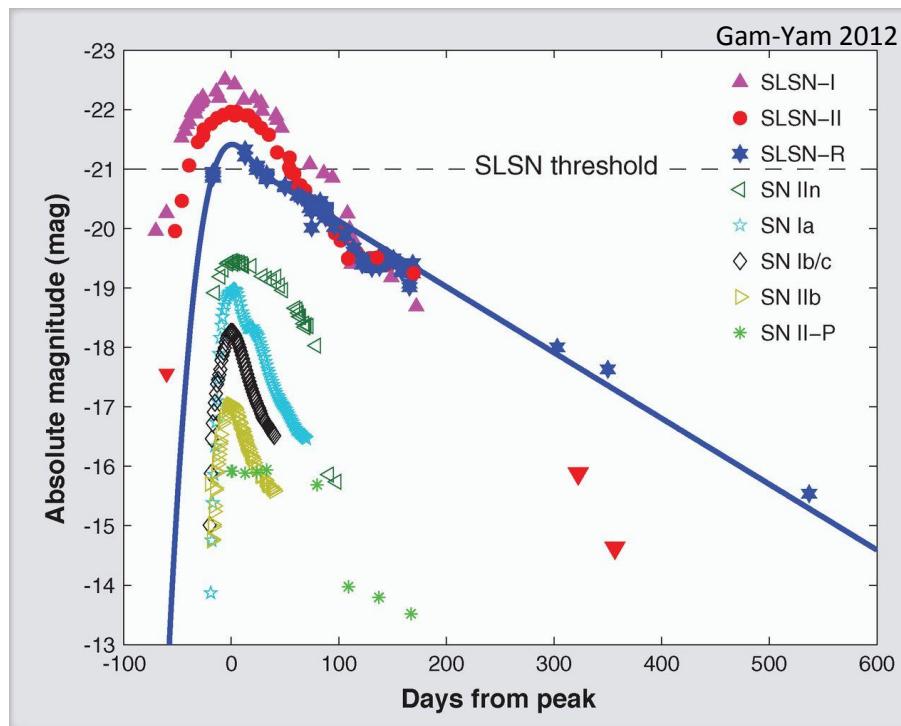
Using millisecond magnetars to power SLSNe and GRBs

see also talk by Rezzolla for GRBs

Superluminous supernovae (SLSNe)

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where $L_{\text{mag}} \sim -B^2 R^6 \Omega^4/c^3$
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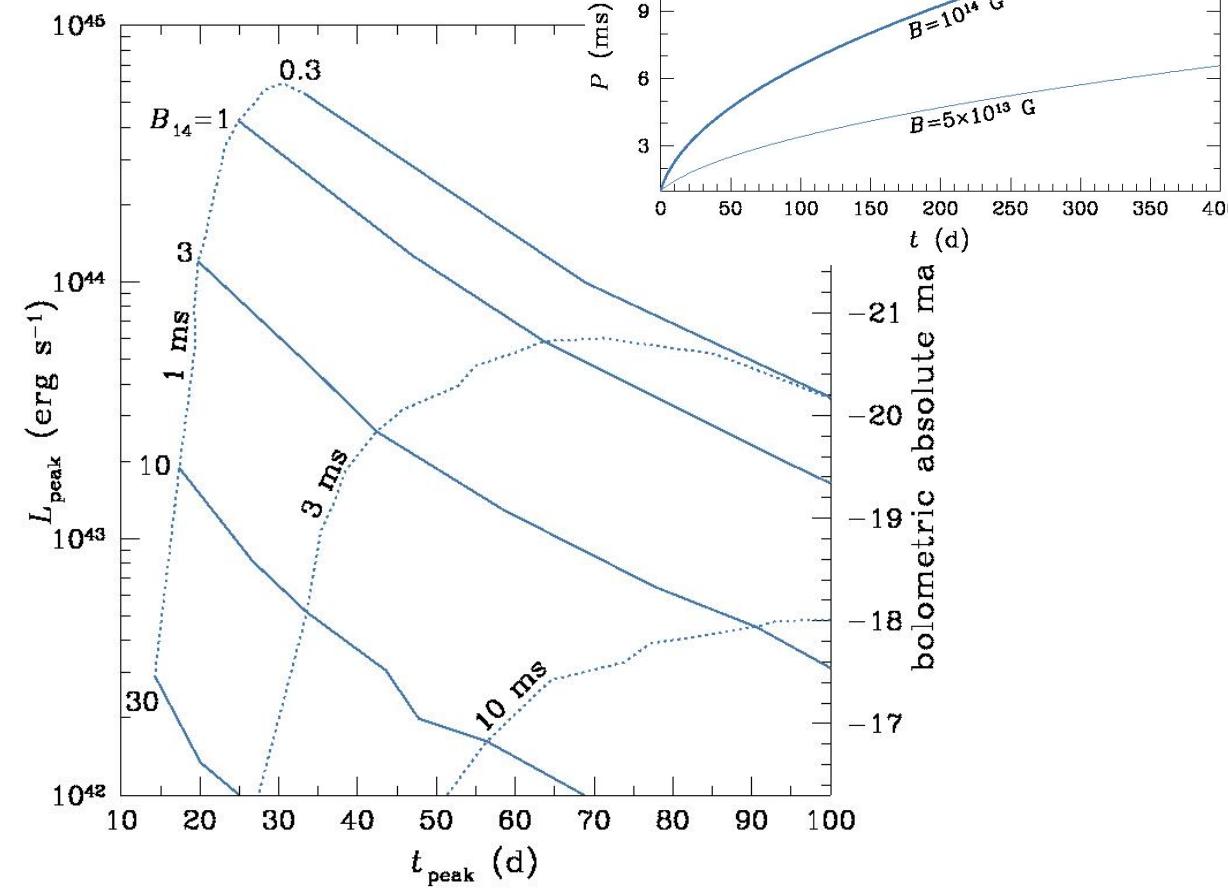
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$$\frac{\partial(tE)}{\partial t} = t (L_{\text{mag}} - L_{\text{rad}})$$

see also talk by Nissanke

$$\text{where radiative diffusion } L_{\text{rad}} = 4\pi r^2 \frac{c}{3\kappa\rho} \frac{\partial(E/V)}{\partial r} \approx tE/t_{\text{diff}}^2$$

- Coupled evolution of E and Ω (eg Kasen+Bildsten 2010)
 - light curve $L_{\text{rad}}(t)$
 - peak luminosity L_{peak} ($\equiv \max L_{\text{rad}}$) and peak time t_{peak}

Using millisecond magnetars to power SLSNe and GRBs

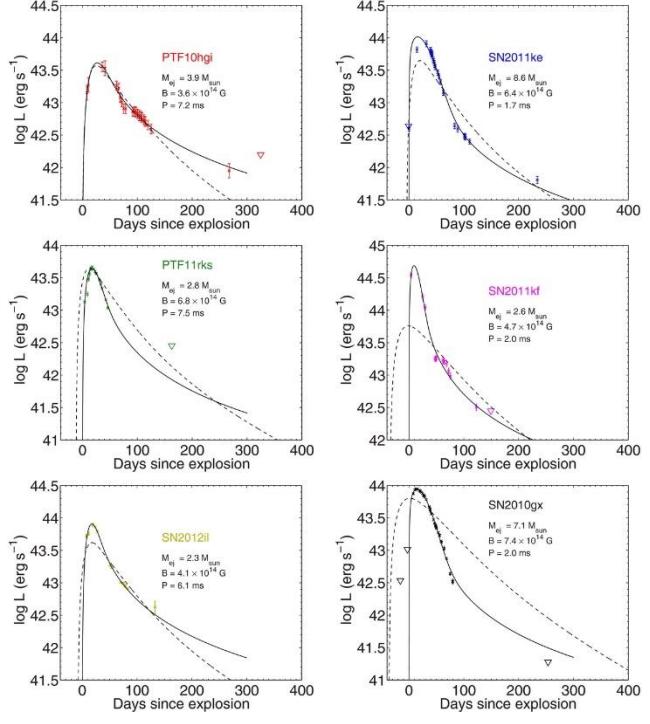


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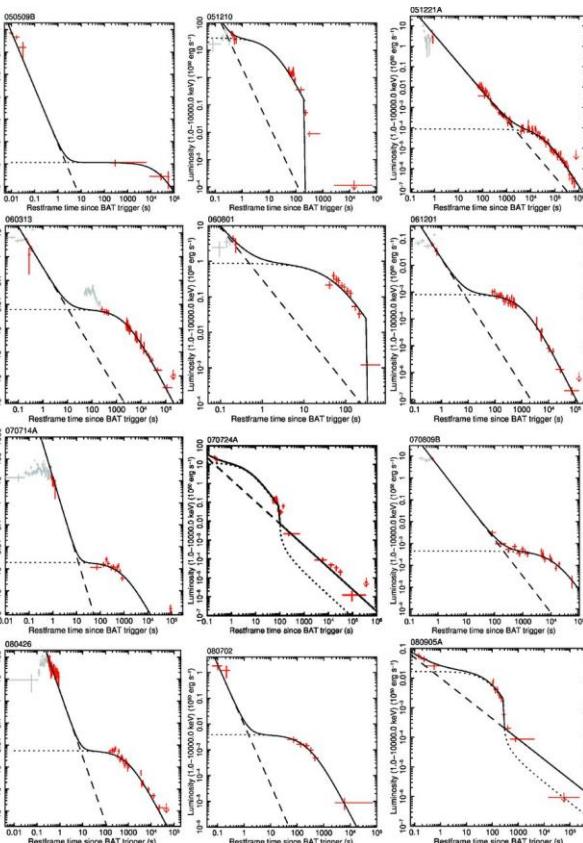
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SLSNe



Inserra+2013

short GRBs



Rowlinson+2013

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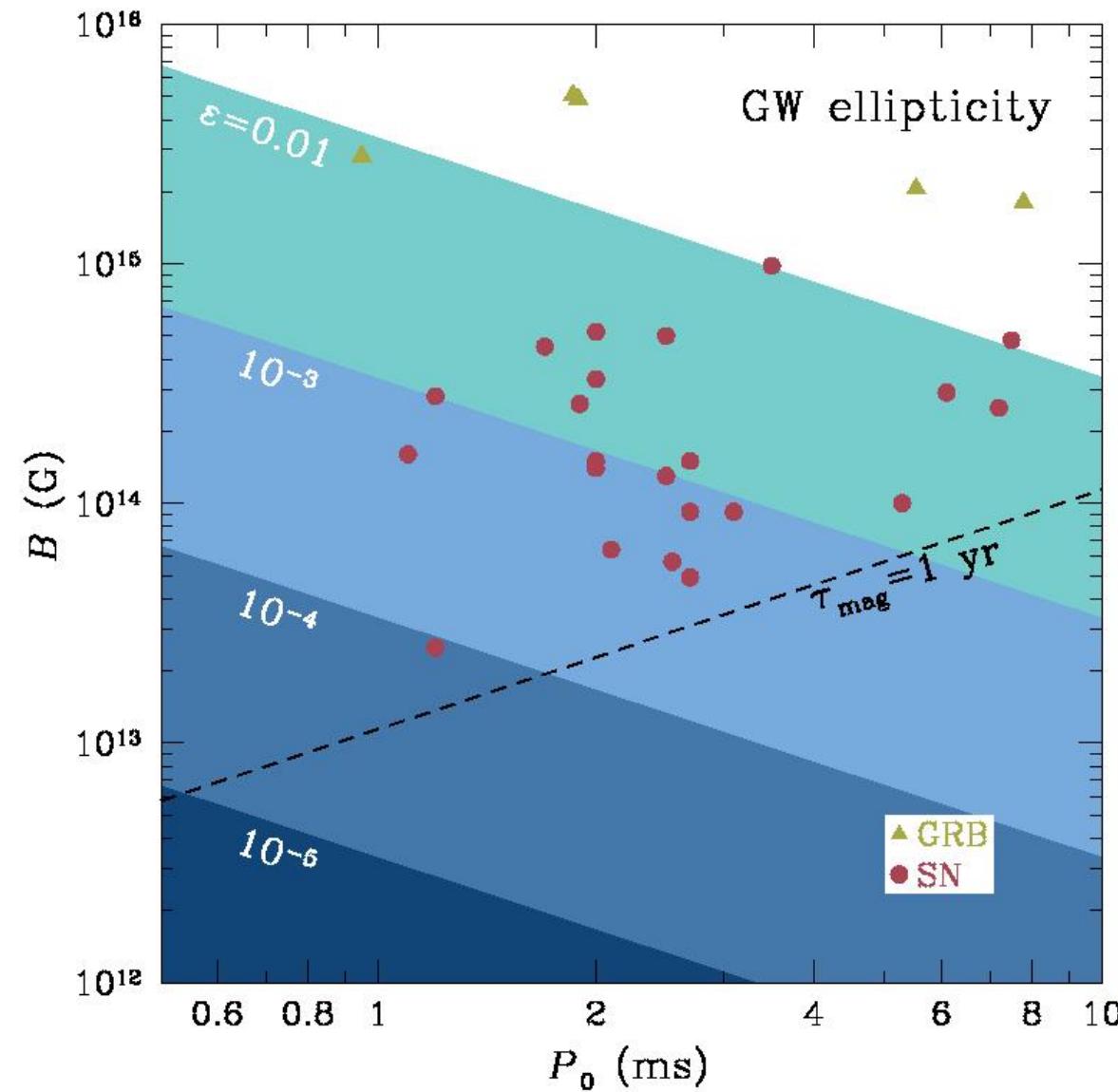
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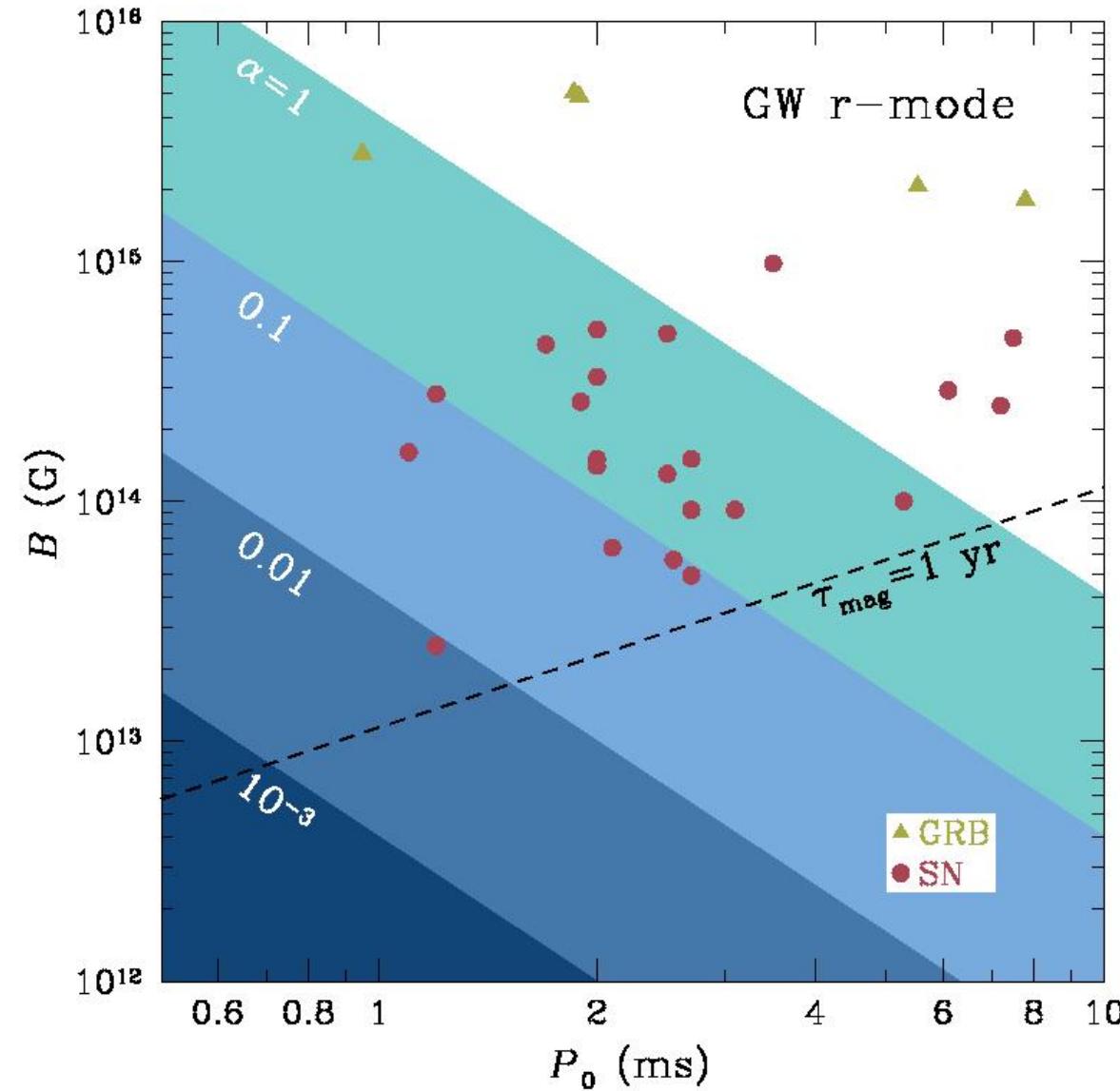
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Simple constraints on amplitudes of ellipticity and r-mode



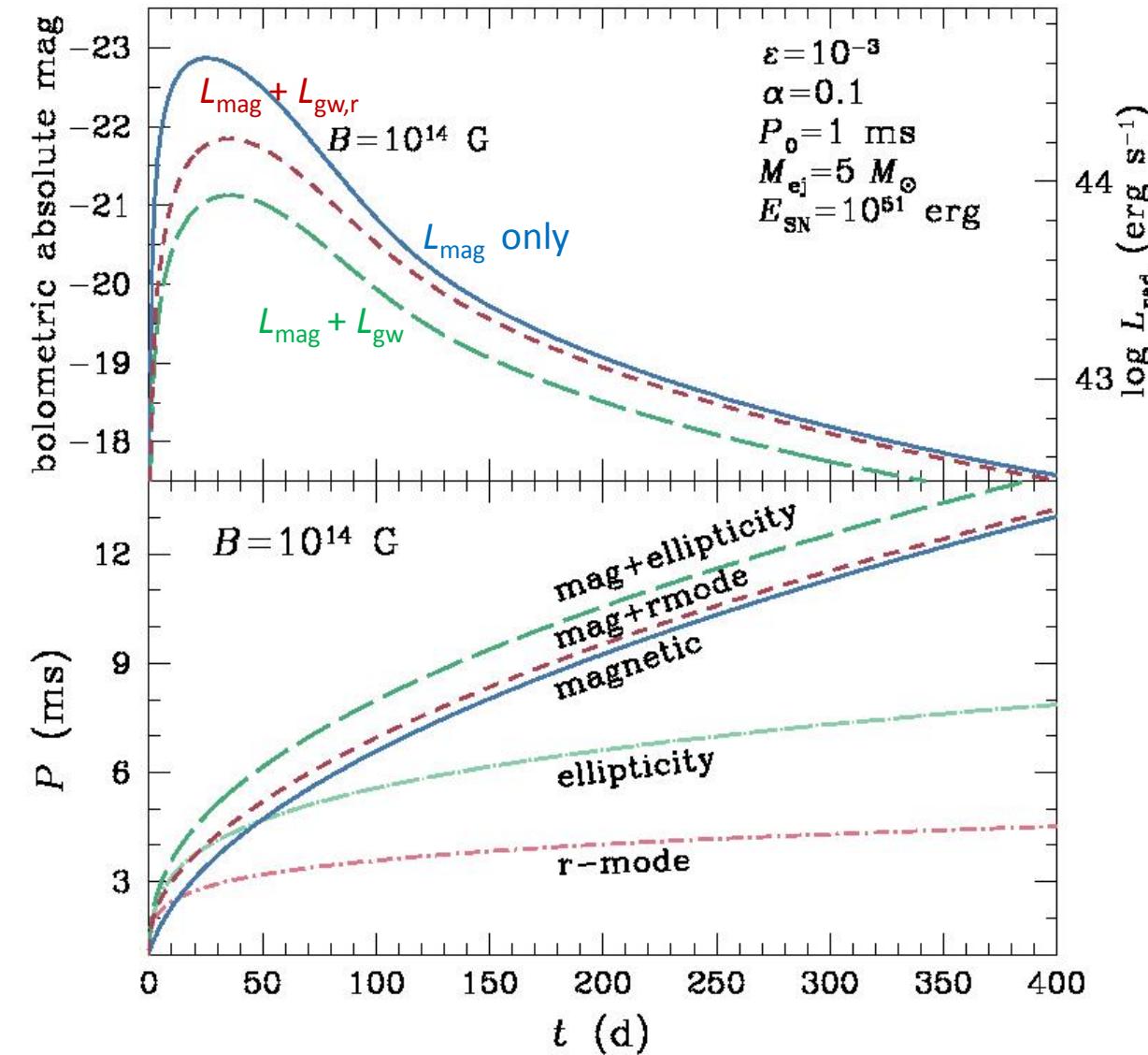
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$$t_{\text{gw,r}} = |E_{\text{rot}} / L_{\text{gw,r}}| = 1 \times 10^5 \text{ s } (\alpha/0.03)^{-2} (P/1 \text{ ms})^6$$
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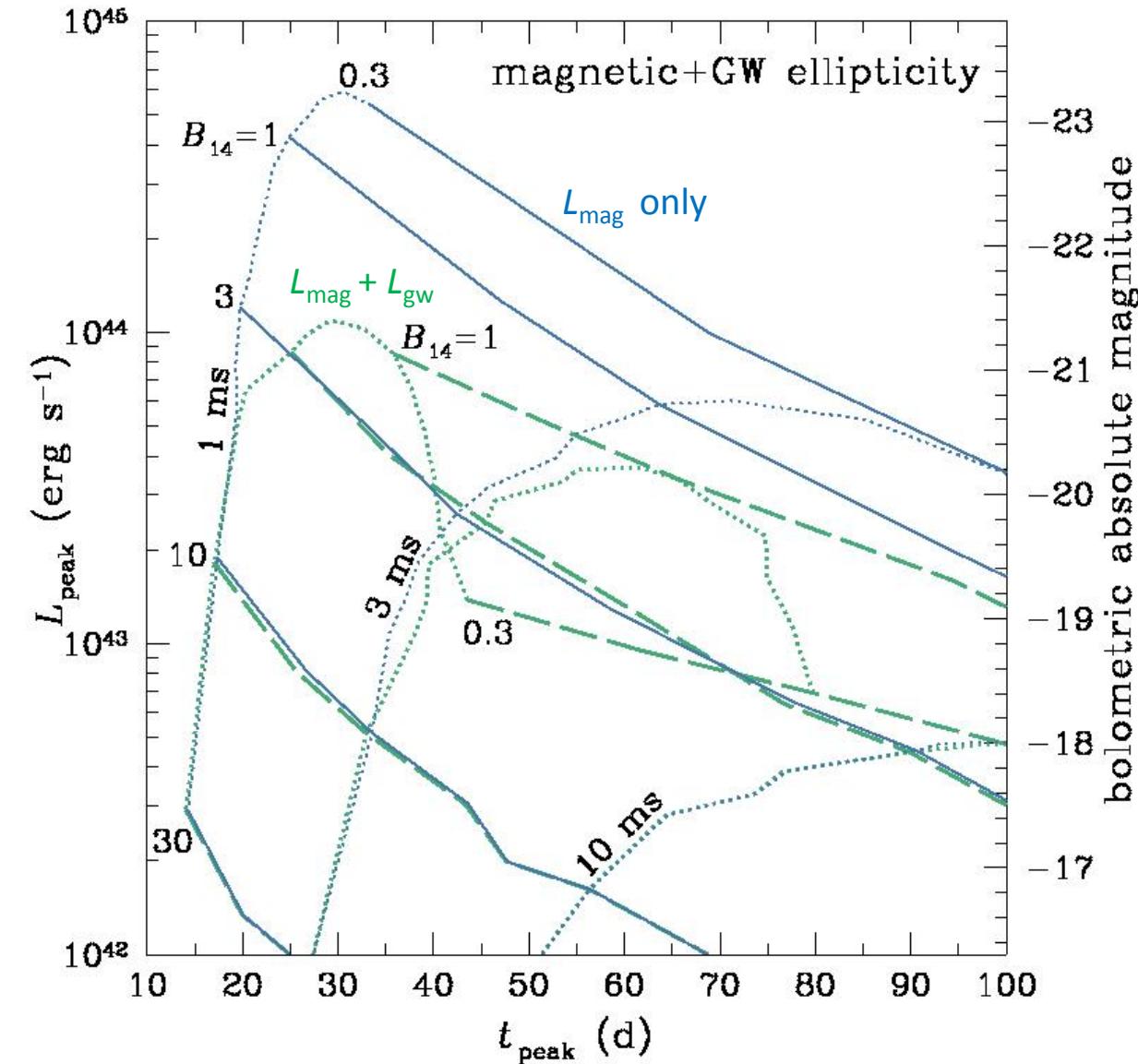
Effect of GWs on SN/GRB light curve



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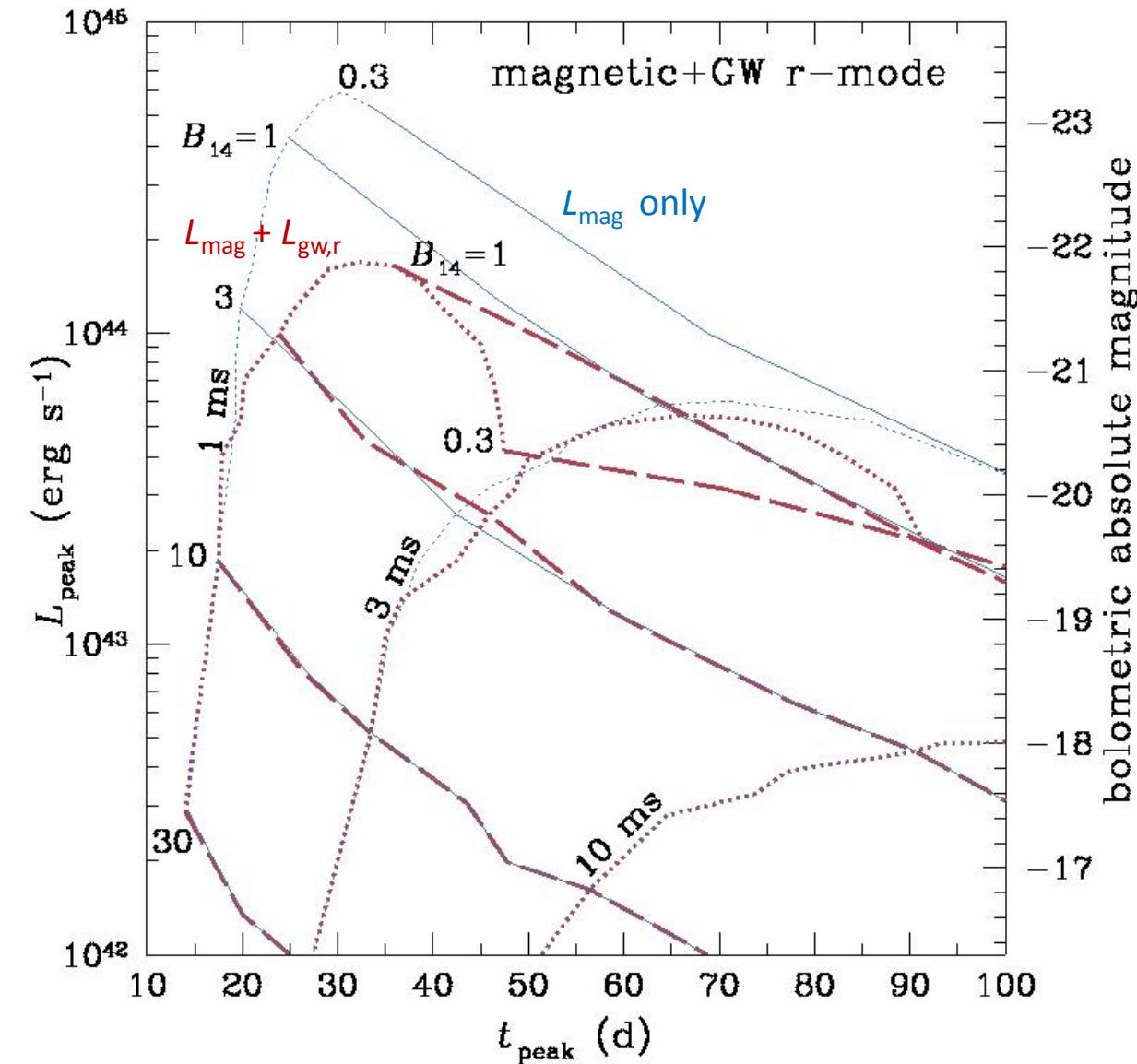
see Kashiyama et al 2016, for more detailed calculation with GW constraints

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Conclusions

GW effect on magnetar model of SNe/GRBs if

- ellipticity $\varepsilon > 10^{-4}$, but theory/observation $< 10^{-3}$
- r-mode $\alpha > 0.01$, but theory/observation $< 10^{-3}/0.1$
(see also talk by Andersson)

⇒ magnetar model is ok for SNe/GRBs without GWs

