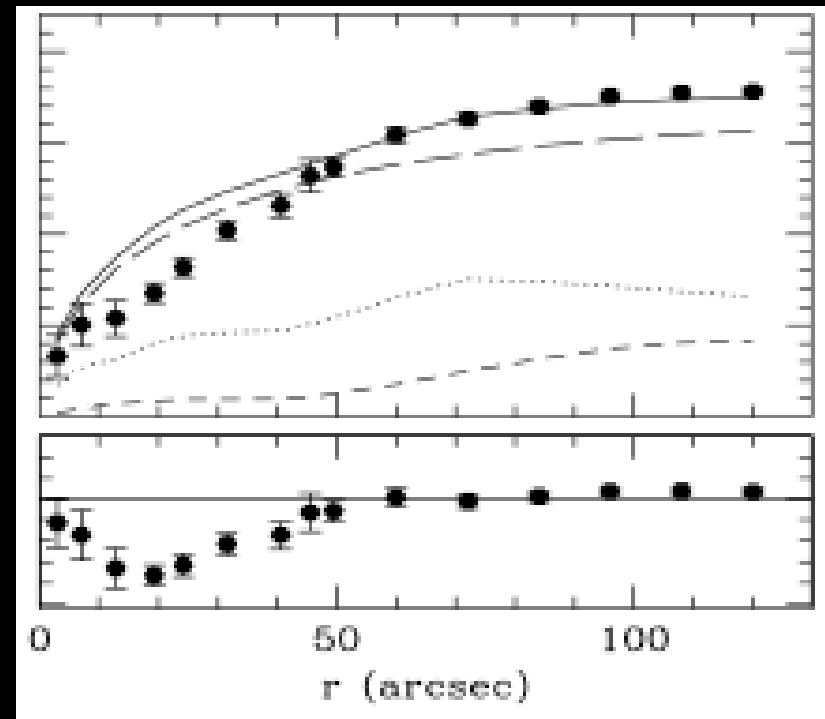




The cusp problem

- Simulations of clustering CDM halos (e.g. Diemand et al) predict a central cusp $\rho \propto r^{-\gamma}$, with $\gamma > 1$
- Feedback from the baryons makes the problem worse
- Angular momentum transfer from the bar not enough
- Bulk gas motions?
- Accretion of substructures?
- Other solutions?
- Hiding cusps by triaxiality of the halo? No

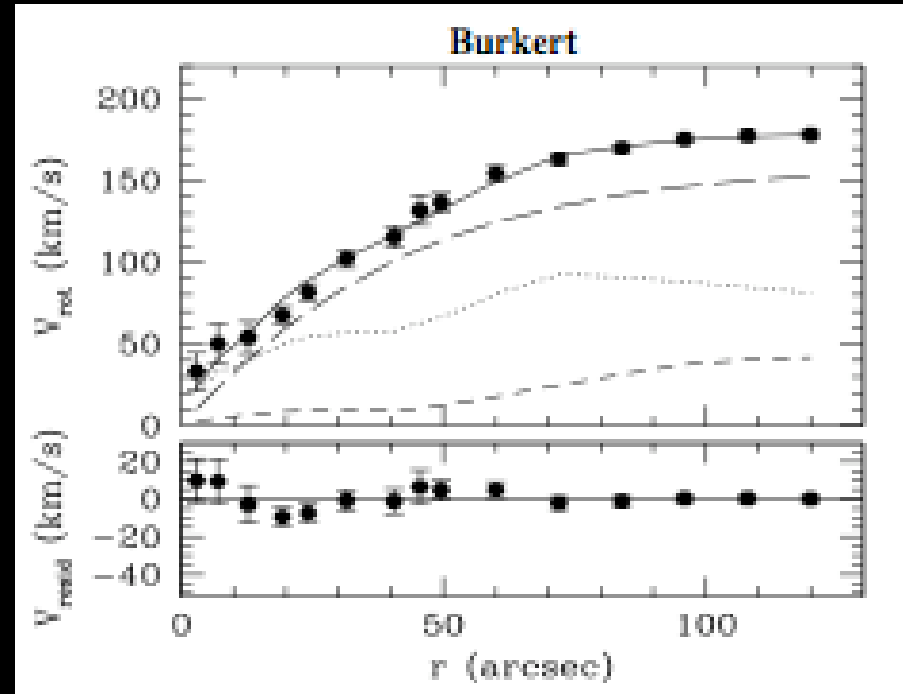


ESO79-G14 (Gentile et al. 2004)

The Burkert halo

- A halo with a **central constant density core**
- 2 parameters: a central density ρ_0 and a core radius r_0 at which the DM density reaches 1/4 of its central value
- Zero slope at the center and -3 log slope in the outskirts

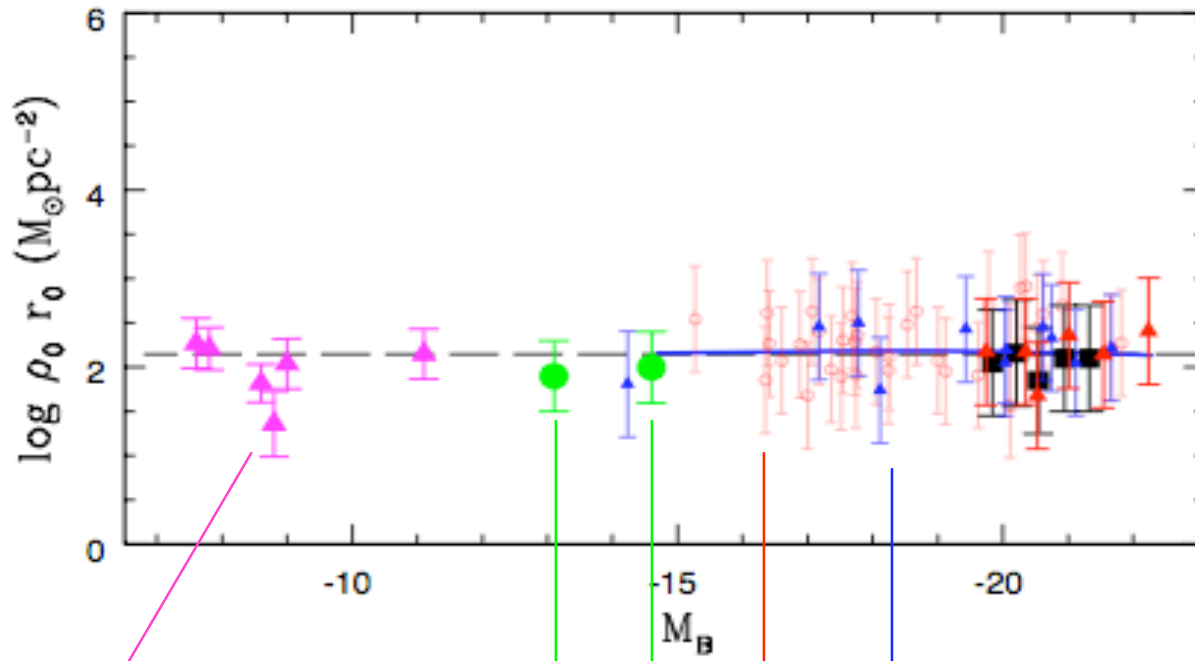
$$\rho_{\text{dm}} = \rho_0 r_0^3 / [(r + r_0)(r^2 + r_0^2)]$$



A scaling relation for DM

A constant dark matter halo surface density in galaxies

F. Donato^{1*}, G. Gentile^{2,3}, P. Salucci⁴, C. Frigerio Martins⁵, M. I. Wilkinson⁶,
G. Gilmore⁷, E. K. Grebel⁸, A. Koch⁹, R. Wyse¹⁰



dSphs (Umi Draco
Carina Sextans Leo I II)

NGC3741

DDO47

GHASP

THINGS

What does it mean?

- The parameters are degenerate with the stellar M/L ratio but this is taken into account in the error bars: difficult to lower them without a better knowledge of stellar pops

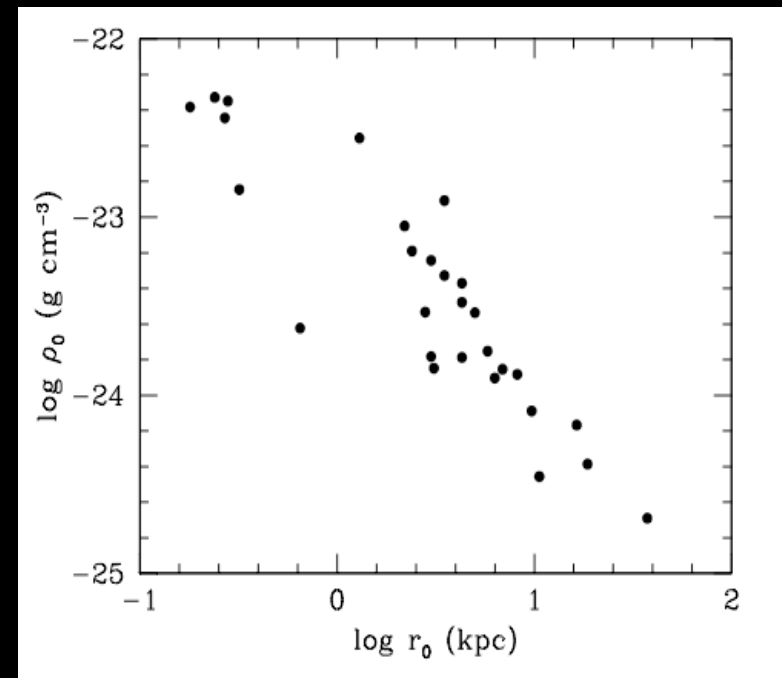
- The product

$$\rho_0 r_0 = 141^{+82}_{-52} M_{*}/\text{pc}^2$$

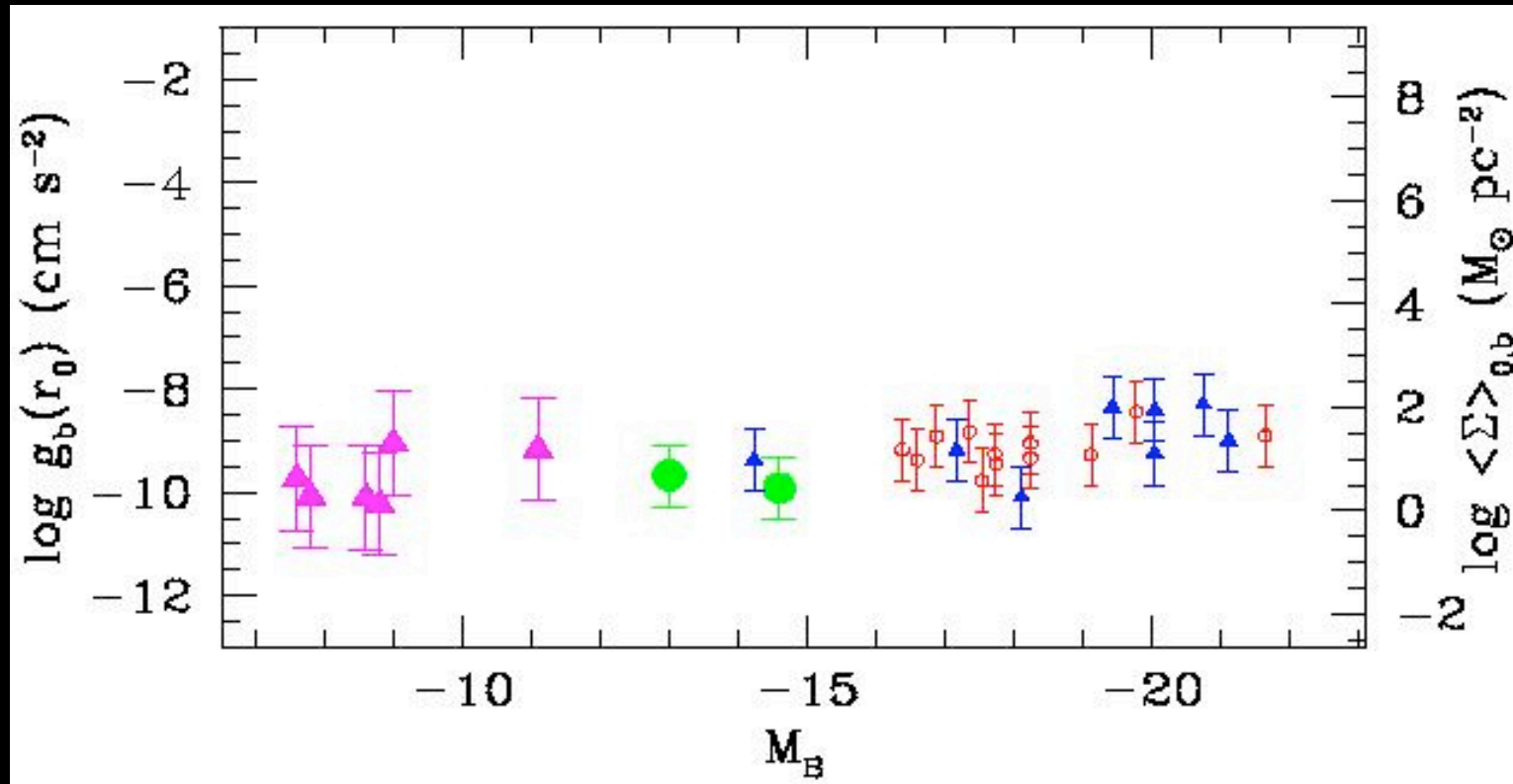
- The mean DM surface density inside $r_0 = 72^{+42}_{-27} M_{*}/\text{pc}^2$

- The gravity due to DM at $r_0 = 3.2^{+1.8}_{-1.2} 10^{-9} \text{ cm/s}^2$

- Very intriguing... (see also [Kormendy & Freeman 2004](#))



A similar relation for baryons!

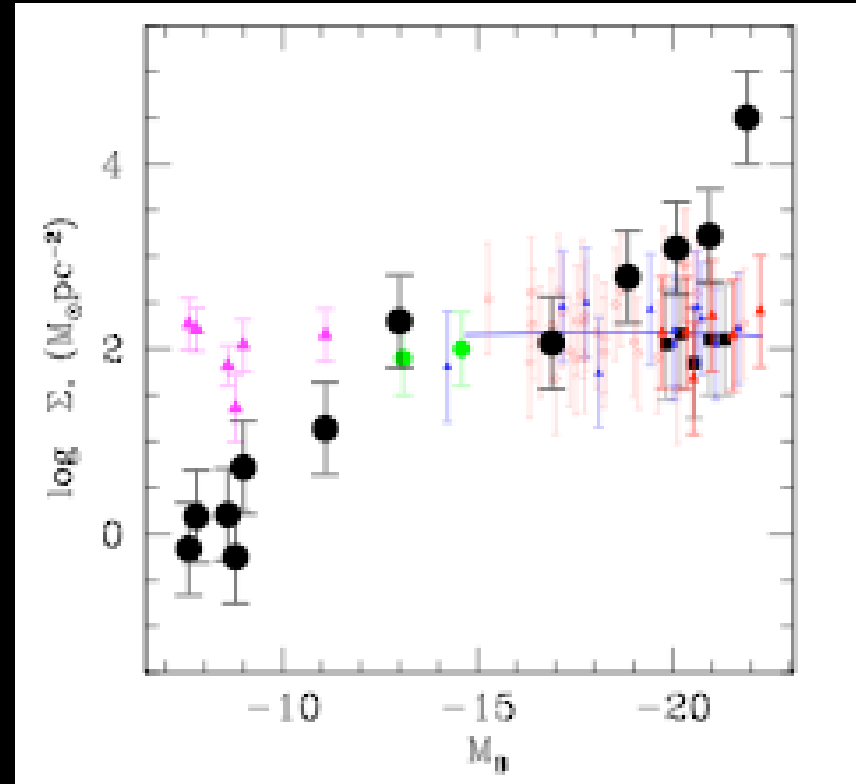


The gravity due to *baryons* at $r_0 = 5.7^{+3.8}_{-2.8} 10^{-10} \text{ cm/s}^2$
or $\log g_b(r_0) = -9.24^{+0.3}_{-0.22}$

Gentile, Famaey, Zhao & Salucci, *Nature*, 461, 627

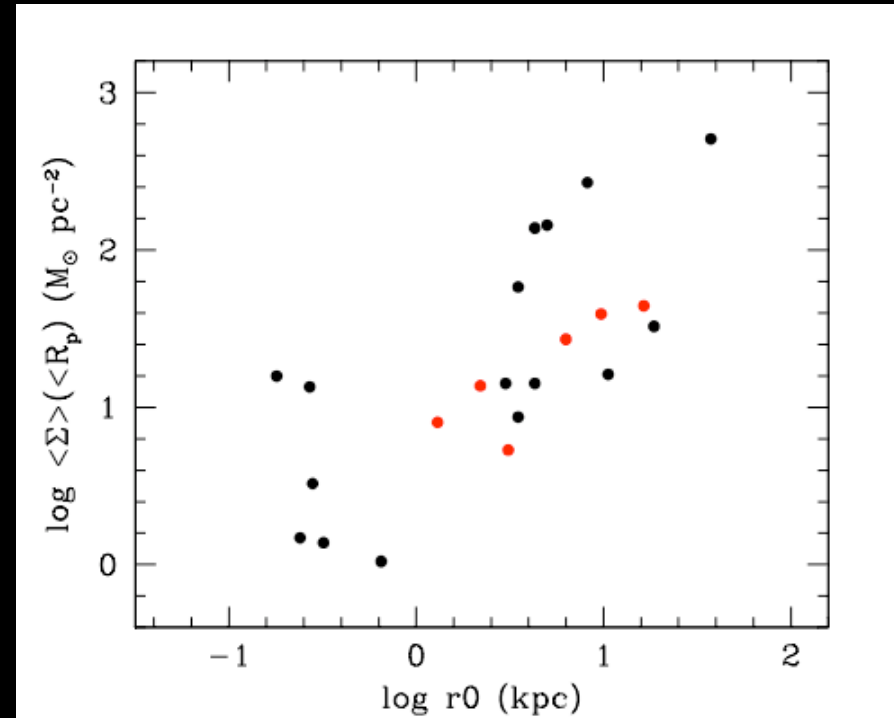
What does it mean?

- The **DM-to-baryonic ratio is universal within r_0**
- It does **not** mean that the total ratio is universal
- It does **not** mean that the baryonic surface density is constant (misconception known as Freeman's law): **the central surface density of baryons varies by 4 orders of magnitude**



What does it mean?

- The larger r_0 of larger and more luminous galaxies compensate for their larger baryonic surface densities
- For a galaxy of a given « baryonic scale-length », the central baryonic surface density is *correlated* with r_0 and *anti-correlated* with the central DM volume density ρ_0
- Unknown fine-tuned process in galaxy formation?



R_p = maximum of the baryonic rot curve

An example

UGC 9179

$$V_c = 90 \text{ km/s}$$

Baryonic surf. den. within R_p

$$= 8.7 M_{\star} / \text{pc}^2$$

$$r_0 = 3.5 \text{ kpc} \Rightarrow \log g_b(r_0) = -9.27$$

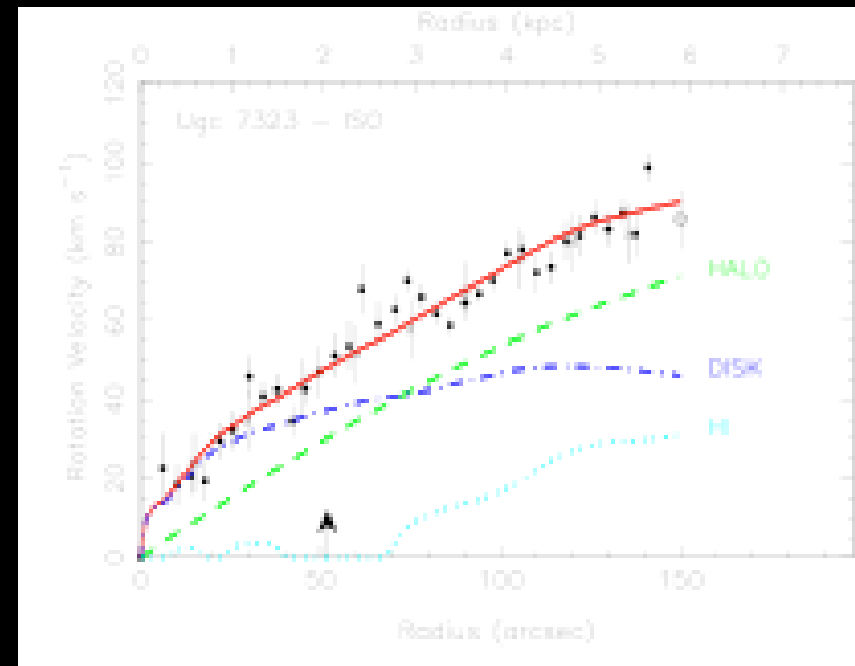
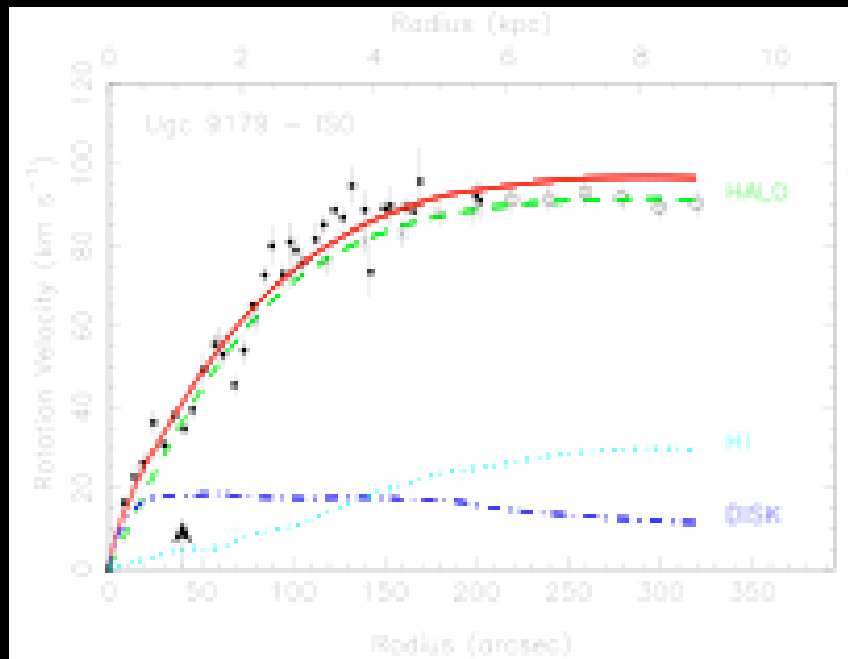
UGC 7323

$$V_c = 90 \text{ km/s}$$

Baryonic surf. den. within R_p

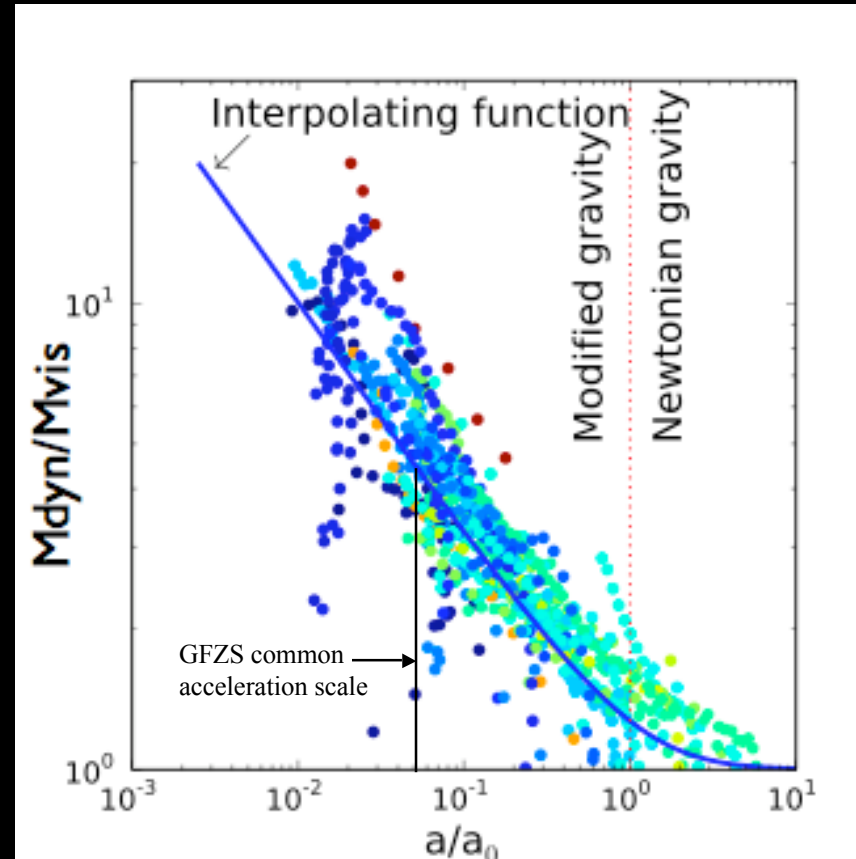
$$= 38.9 M_{\star} / \text{pc}^2$$

$$r_0 = 9.7 \text{ kpc} \Rightarrow \log g_b(r_0) = -9.05$$



Mass Discrepancy vs Acceleration

- At r_0 , the acceleration from the DM is always the same: it is a **natural consequence** of the Mass Discrepancy-Acceleration relation that the acceleration from baryons is then the same and vice-versa



McGaugh 2004; Tiret & Combes 2008

$$a_0 = 1.2 \times 10^{-8} \text{ cm/s}^2$$

MOND

$$\mu(g/a_0) g = g_{\text{N bar}} \quad \text{where } a_0 \sim cH_0 \sim c\Lambda^{1/2}$$

$$\mu(V^2/ra_0) V^2/r = g_{\text{N bar}}$$

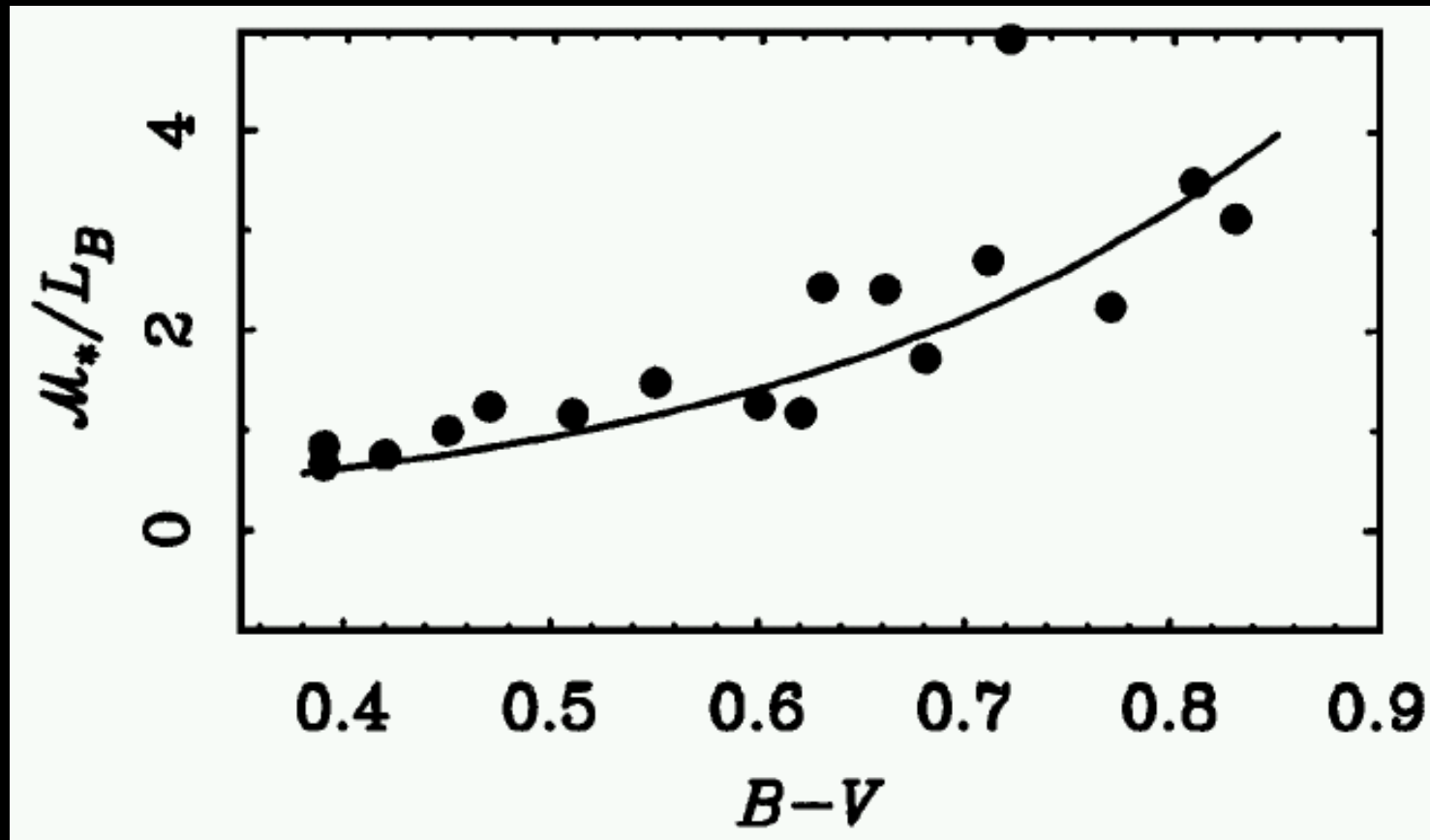
with $\mu(x) = x$ for $x \ll 1$

$$\mu(x) = 1 \text{ for } x \gg 1$$

MOND

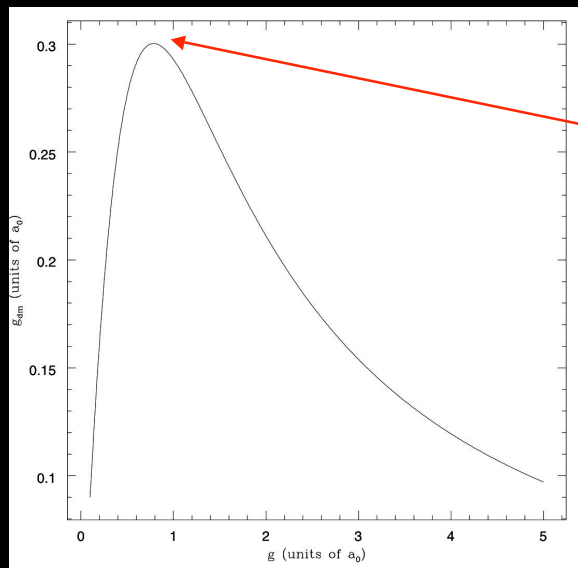
- OK for the Milky Way TVC (Famaey & Binney 2005, McGaugh 2008)
- No cusp problem + explains the RC wiggles following the baryons
- Tully-Fisher relation (observed with small scatter): $V_{\infty}^4 = GM_{\text{bar}} a_0$
- Predicts that the discrepancy always appear at $V^2 / r \sim a_0$
=> in LSB where $\Sigma \ll a_0/G$
- Explains why young Tidal Dwarf Galaxies exhibit a Mass Discrepancy in NGC 5291 (Bournaud et al. 2007, Gentile et al. 2007)
- Predicts the correct order of magnitude for the local galactic escape speed (Famaey, Bruneton & Zhao 2007)
 - Could be:
 - a) fundamental property of DM (e.g. Blanchet, Zhao)
 - b) modification of « inertia » (Milgrom 1994)
 - c) modification of gravity
 - d) all of the above

MOND



MOND => acceleration due to the « dark matter » is :

$g_{\text{dm}} = [1 - \mu] g$ with typically a *maximum* acceleration of the order of $0.3a_0$ (depends on μ)

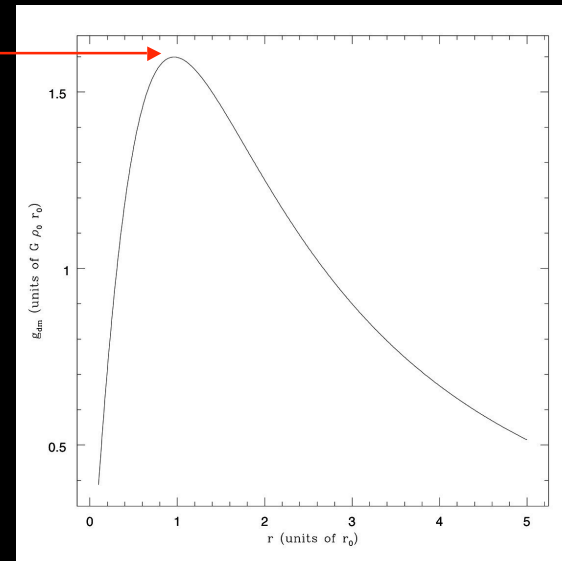


Milgrom

$1.6 G \rho_0 r_0$
 $= 0.3 a_0$

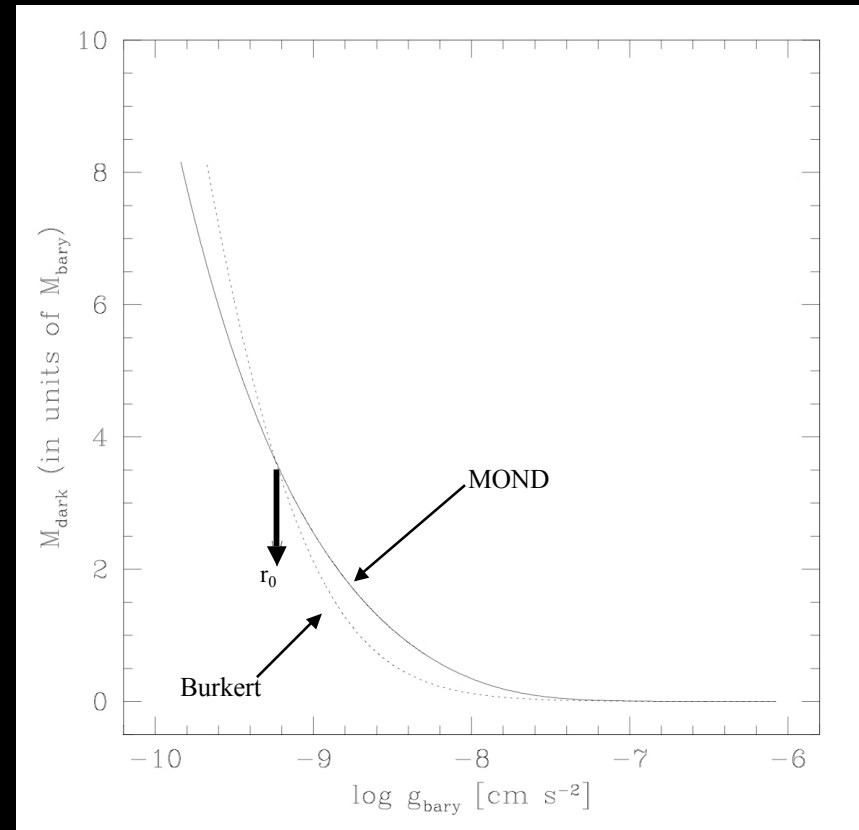


$\rho_0 r_0 = 130 M_* \text{pc}^{-2}$
 $(\log \rho_0 r_0 = 2.1)$



Burkert

- For a Burkert halo to produce the same maximum acceleration as MOND, one gets naturally the Donato scale $g_{\text{DM}}(r_0) \sim 3 \times 10^{-9} \text{ cm/s}^2$
- However, the MOND « DM » profile \neq the Burkert profile, so this doesn't happen at the same baryonic gravity
- Fixing a Burkert halo such that the maximum acceleration due to DM happens at the GFZS scale $g_{\text{bar}}(r_0) \sim 6 \times 10^{-10} \text{ cm/s}^2$ and such that the MOND mass discrepancy is reproduced at r_0 yields a **very similar profile to the MOND one**



Conclusion

- The core radius in any galaxy = the radius where the mass discrepancy is of the order of 5
- This always happens at the same gravity produced by the baryonic component $g_{\text{bar}} \sim 6 \times 10^{-10} \text{ cm/s}^2$
- This is linked with the success of the MOND phenomenology on galaxy scales
- The MOND phenomenology has to be understood (one way or the other: baryon-DM interactions, modified gravity) in order to get a better understanding of the dark sector in galaxies