

A TRIPTYCH AROUND CMB B-MODES

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- **An example of theoretical predictions** : bouncing cosmology induced by LQC

Collaborateurs: Mielczarek (Cracaw), Barrau, Gorecki & Cailleteau (Grenoble)

- **Power spectrum estimation** : pure pseudo-spectrum

Collaborateurs: Stompor (APC-Paris) & Tristram (LAL-Orsay)

- **Component Separation** : parametric approach

Collaborateurs: Stivoli (INRIA-Orsay), Tristram (LAL-Orsay), Leach & Baccigalupi (SISSA-Trieste), Stompor (APC-Paris)

POLARIZED ANISOTROPIES OF THE CMB

CMB plays a *keyrole* in setting cosmology in the ages of *precise science*
(geometry of the Universe, matter content, neutrinos total mass)

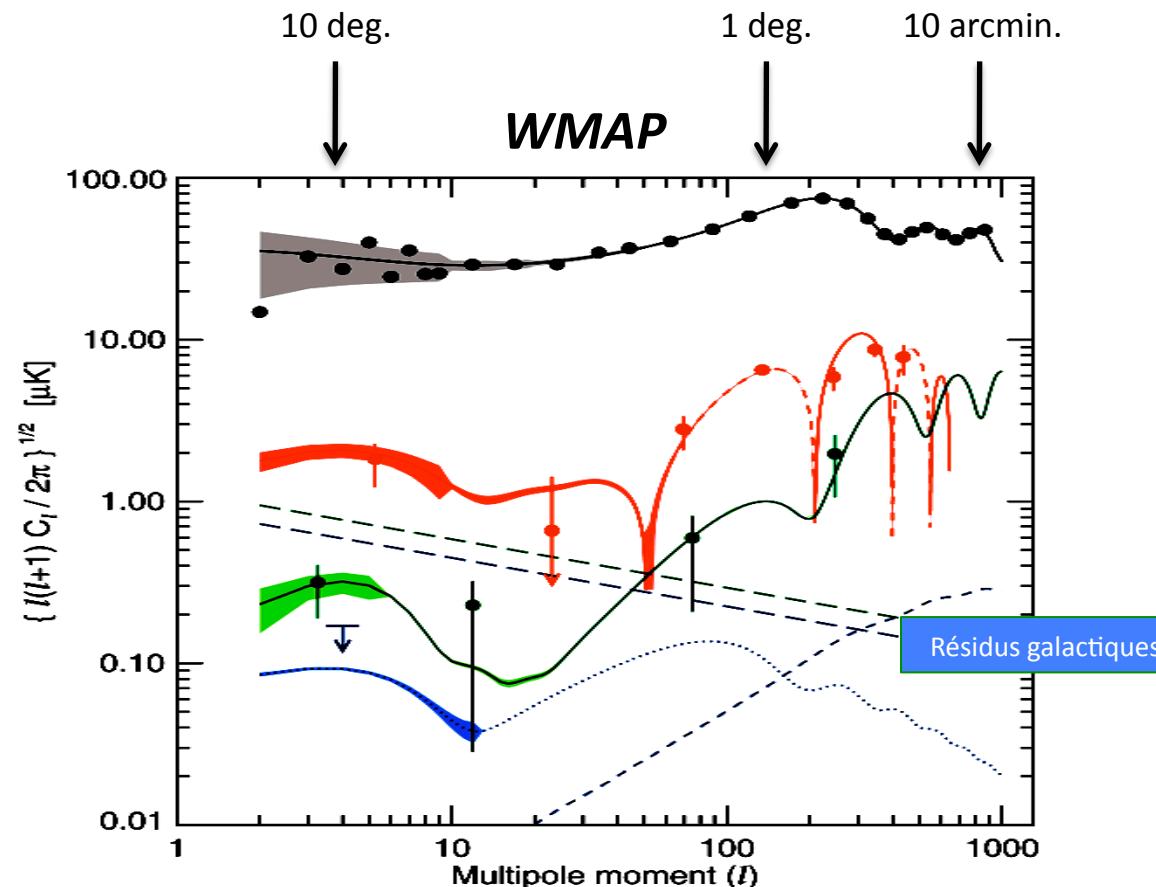
- Statistics of its anisotropies

- Temperature **T** (scalar & tensor)
- Polarization **E** (scalar & tensor)
- Polarization **B** (tensor)

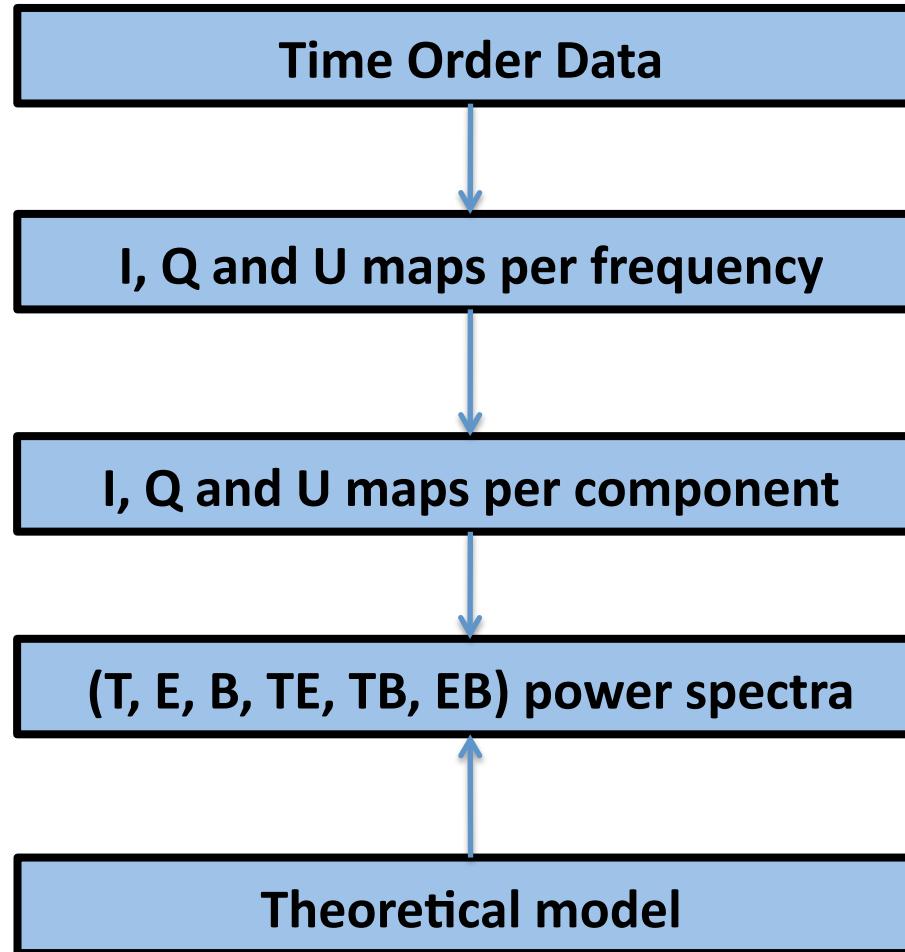
- **B-mode**

Open window on inflation/alternatives/new theories

Gravitational lensing



CMB DATA ANALYSIS



A RAPID SKETCH OF LOOP QUANTUM GRAVITY (LQG)

« Can we construct a quantum theory of spacetime based only on the experimentally well confirmed principles of general relativity and quantum mechanics ? » L. Smolin, hep-th/0408048

GR classically re-written with Ashtekar variables :

$$\text{densitized triad } E_i^a = \left| \det(e_j^b) \right|^{-1} e_i^a$$

$$\text{Ashtekar connection } A_a^i = \Gamma_a^i + \gamma K_a^i$$

Quantization by use of holonomies and fluxes (background independence)

$$F(E) \propto \int_S \tau^i E_i^a n_a d^2 s$$

$$h(A) \propto \exp \left(\int_C \tau_i A_a^i u^a d\lambda \right)$$

- The area, volume and length operators have a discrete spectrum
- The horizon entropy is completely explained.
- Singularities are eliminated.
- Ultraviolet divergences of QFT are not present.
- Loop quantum cosmology is on the way....

LQG IN THE COSMOLOGICAL FRAMEWORK : BACKGROUND

FLRW-reduced formulation of LQG : Loop Quantum Cosmology (LQC)

$$ds^2 = a^2(\eta) \left(d\eta^2 - \delta_{ij} dx^i dx^j \right)$$

Background equation : classical results

$$H^2 = \frac{8\pi G}{3} \rho$$

$$\ddot{\Phi} + 3H\dot{\Phi} + \frac{\delta V}{\delta \Phi} = 0$$

SEE WORKS OF: ASHTEKAR, BOJOWALD, LEWANDOWSKI, PAWLICKI, SINGH, CORICHI, MIELCZAREK, VANDERSLOOT, ETC.

FOR A REVIEW, SEE: CALCAGNI & HOSSAIN, ADV. SCI. LETT. 2, 184 (2009)

Background equation : quantum corrected results

$$H^2 = \frac{8\pi G}{3} \rho \left[1 - \frac{\rho}{\rho_c} \right]$$

$$\ddot{\Phi} + 3H\dot{\Phi} + \frac{\delta V}{\delta \Phi} = 0$$

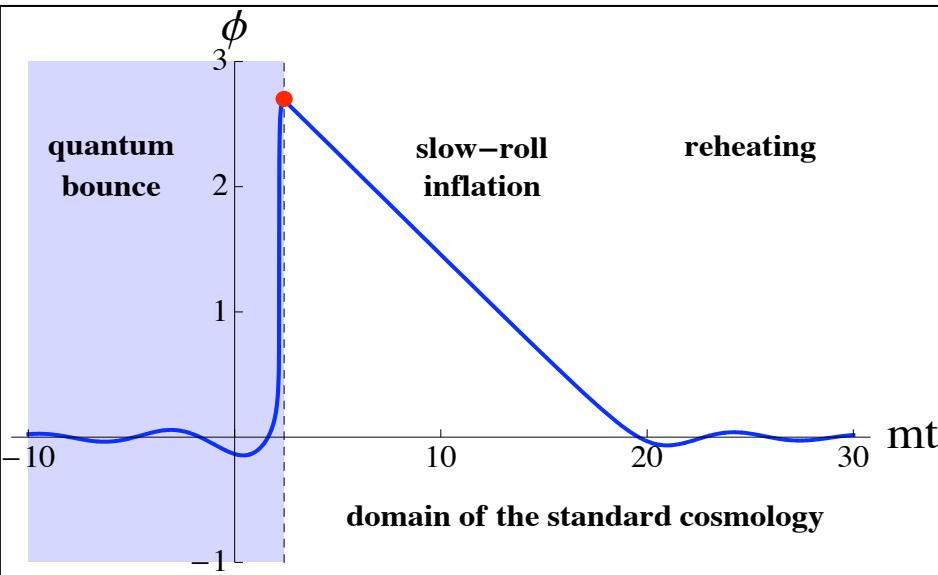
bouncing cosmology

BACKGROUND WITH HOLONOMIES

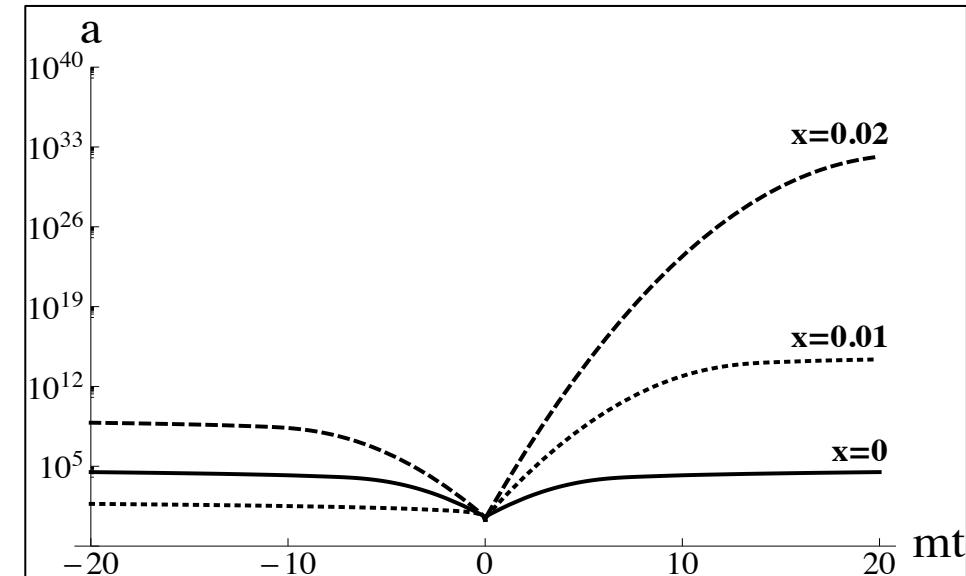
$$H^2 = \frac{8\pi G}{3} \rho \times \left[1 - \frac{\rho}{\rho_c} \right]$$

$$\ddot{\Phi} + 3H\dot{\Phi} + m_\Phi^2\Phi = 0$$

Scalar field



Scale factor



✓ A sufficient amount of e-folds: $\underline{\rho_c = m_{Pl}^4}$:

for $m_\Phi = 10^{-6} m_{Pl}$, $x = 0$: $\Phi_{\max} \approx 2.1 m_{Pl}$ and $N \approx 28$

for $m_\Phi = 10^{-3} m_{Pl}$, $x = 0.01$: $\Phi_{\max} \approx 3 m_{Pl}$ and $N \approx 60$

✓ A maximum amount of e-folds: $N_{\max} = \frac{4\pi\rho_c}{m_\Phi^2 m_{Pl}^2} \left(\approx 4\pi \frac{m_{Pl}^2}{m_\Phi^2} \text{ for } \rho_c \approx m_{Pl}^4 \right)$

LQG IN THE COSMOLOGICAL FRAMEWORK : TENSOR PERTURBATIONS

Perturbed FLRW metric

$$ds^2 = a^2(\eta) \left(d\eta^2 - (\delta_{ij} + h_{ij}) dx^i dx^j \right)$$

Gravity waves equation : classical results

$$\frac{d^2 \phi_k}{d\eta^2} + \left(k^2 - \frac{a''}{a} \right) \phi = 0 \quad \text{with} \quad \phi_k \equiv a(\eta) h_{ij}^{(k)}$$

Gravity waves equation : quantum corrected results

$$\frac{d^2 \phi_k}{d\eta^2} + \left(k^2 - \frac{a''}{a} - V_{holo}(a, \rho_c) \right) \phi_k = 0 \quad \text{with} \quad \phi_k \equiv a(\eta) h_{ij}^{(k)}$$

- Modified background
- Modified «Dispersion relation»

FOR THE EQUATION: Bojowald & Hossain, Phys. Rev. D 77 023508 (2008)

APPLIED TO INFLATION:

J. Grain, A. Barrau , Phys. Rev. Lett. **102** 081301 (2009)

J. Grain, A. Barrau & A. Gorecki, Phys. Rev. D **79** 084015 (2009)

J. Grain, T. Cailleteau, A. Barrau & A. Gorecki, Phys. Rev. D **81** 024040 (2010)

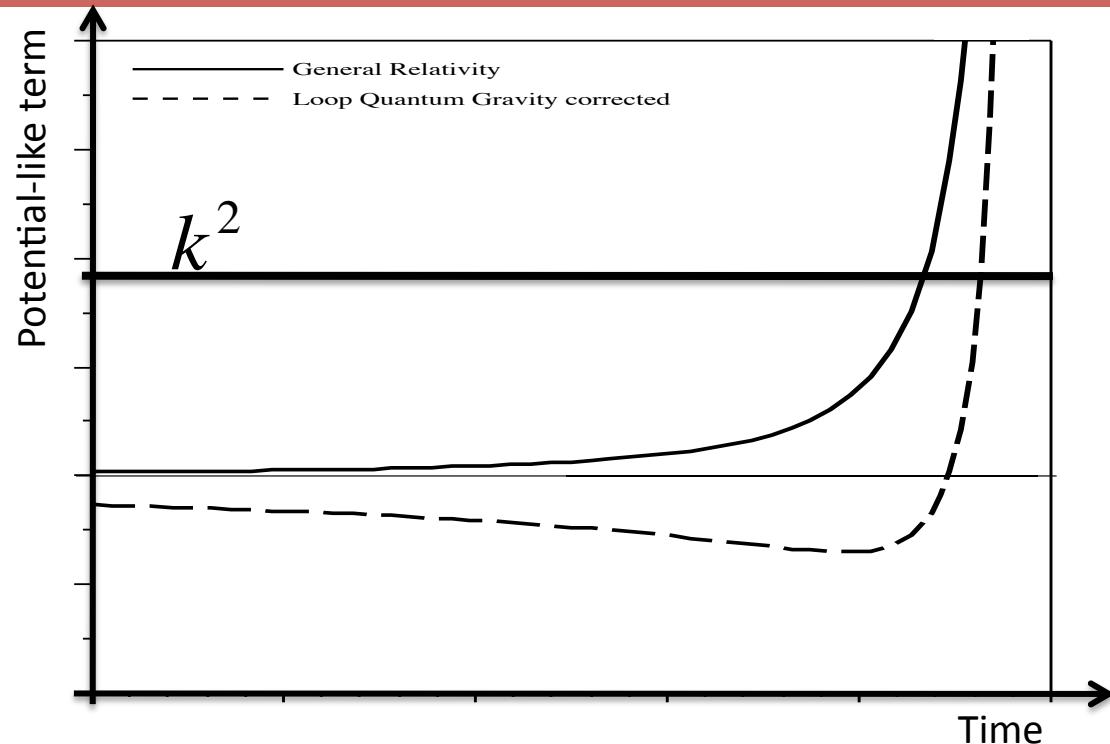
AND WORKS OF: MIELCZAREK, COPELAND, NUNES, MULRYNE, ETC.

TENSOR PERTURBATIONS : POWER SPECTRA AND IMPACT ON B-MODES

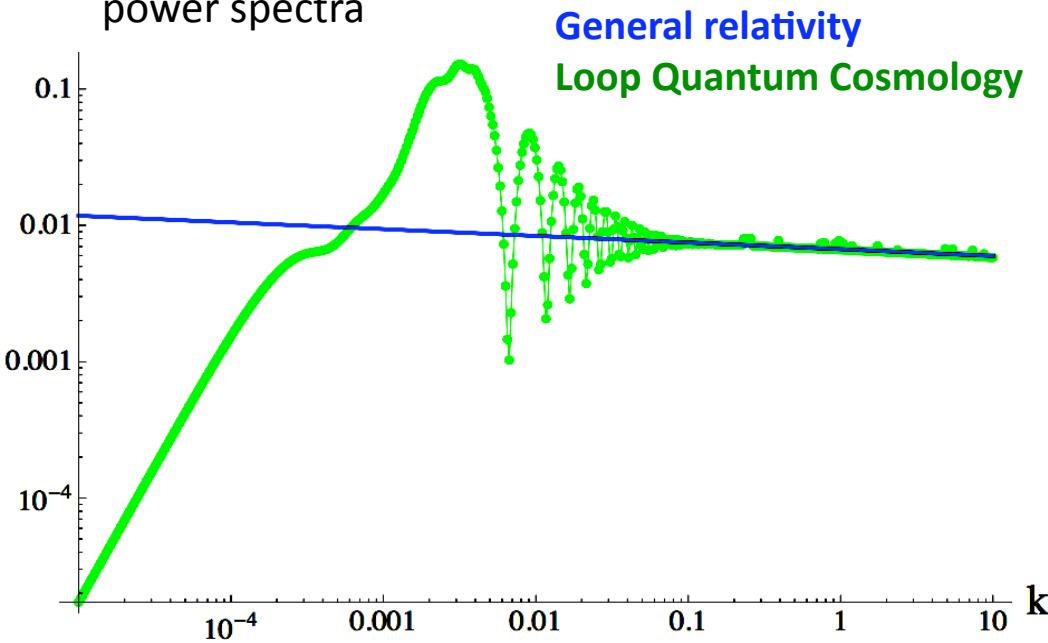
J. MIELCZAREK, T. CAILLETEAU, J. GRAIN & A. BARRAU, SUBMITTED TO
PHYS. REV. D

$$\frac{d^2\phi_k}{d\eta^2} + [k^2 - V(\eta)]\phi_k = 0$$

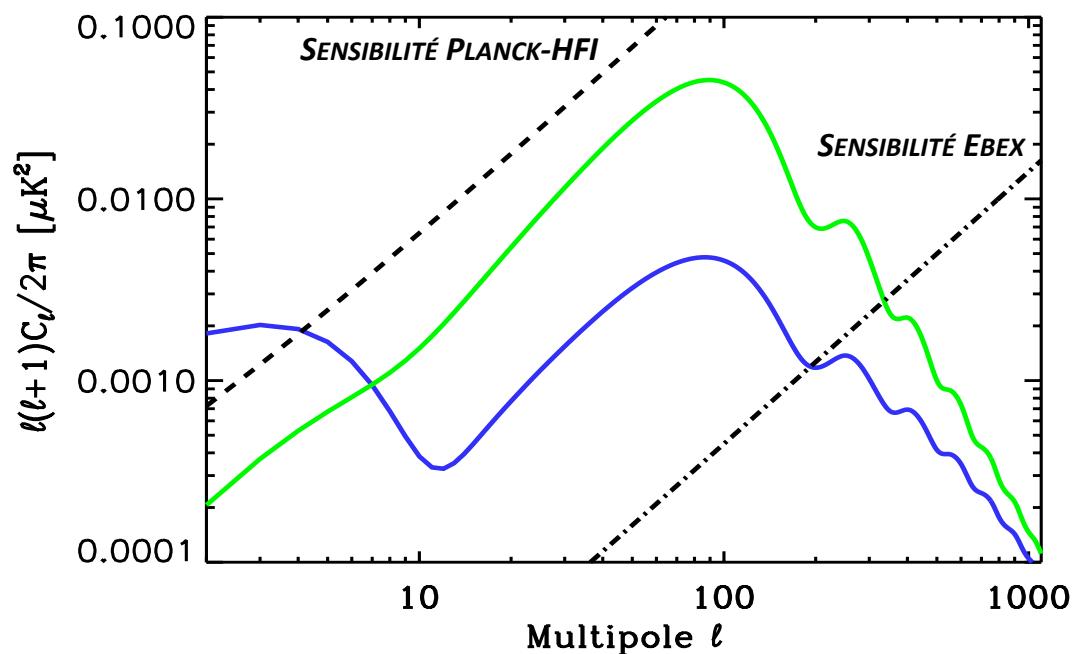
$$\text{with } V_{GR}(\eta) = V_{LQC}(\eta) = 4\pi Ga^2 \left(\frac{\rho_\Phi}{3} - p_\Phi \right)$$



Tensor perturbations
power spectra



General relativity
Loop Quantum Cosmology



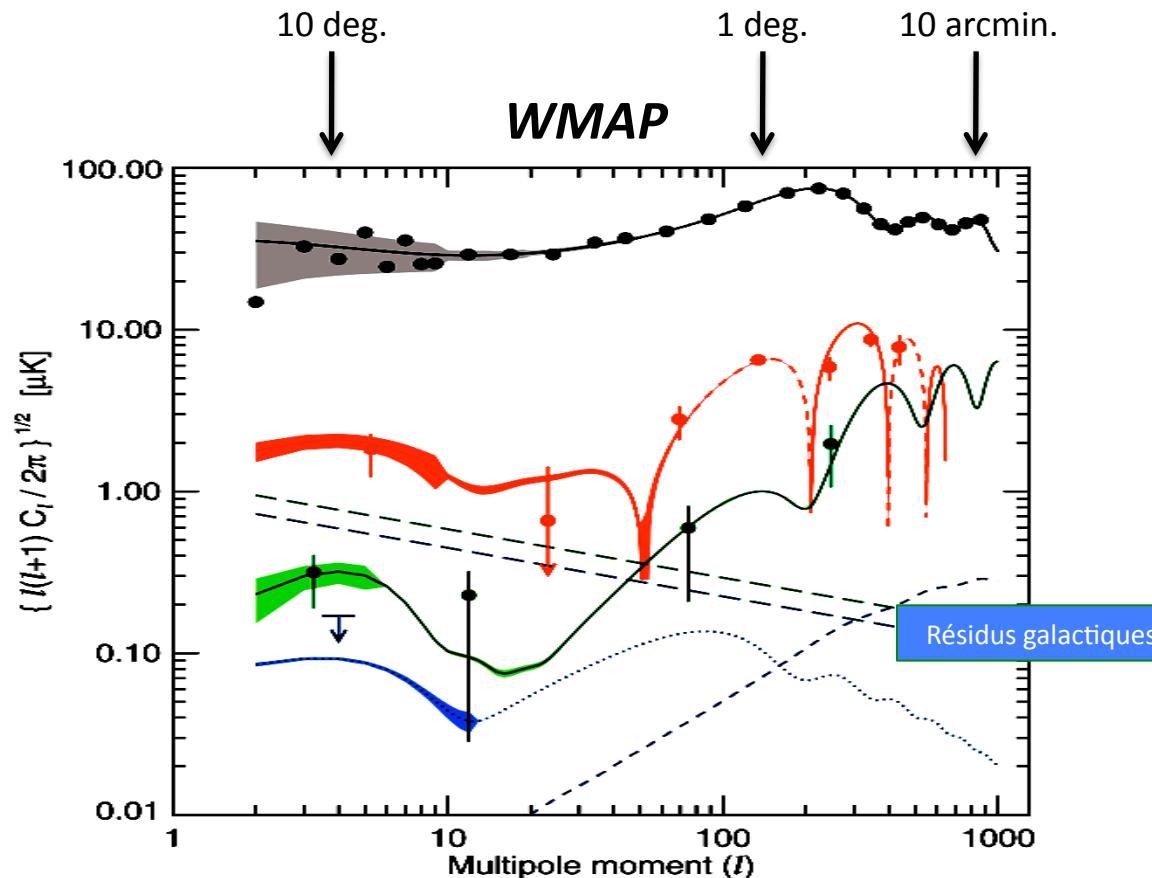
POLARIZED ANISOTROPIES OF THE CMB

- Statistics of its anisotropies

Temperature **T** (scalar & tensor)
Polarization **E** (scalar & tensor)
Polarization **B** (tensor)

- **B-mode**

Open window on inflation
Gravitational lensing
Open window on tentative new theories



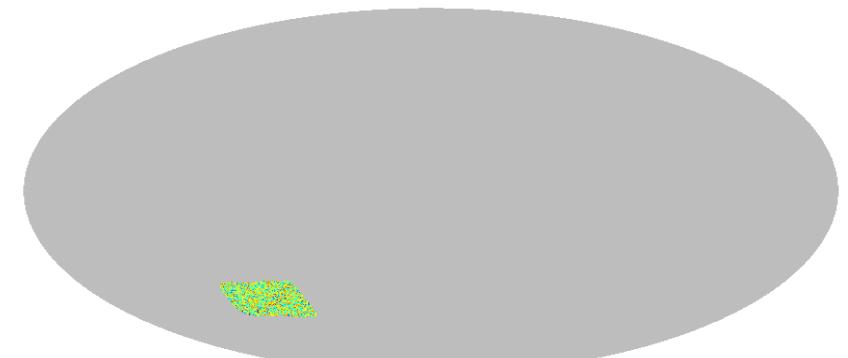
- Observational challenges

- ➔ instrumental sensitivity
- ➔ systematic effects
- ➔ *Foregrounds >> CMB* : component separation
- ➔ *E >> B* : E-to-B leakages to be corrected

POLARIZED POWER SPECTRUM ESTIMATION WITH *PURE* PSEUDO SPECTRUM

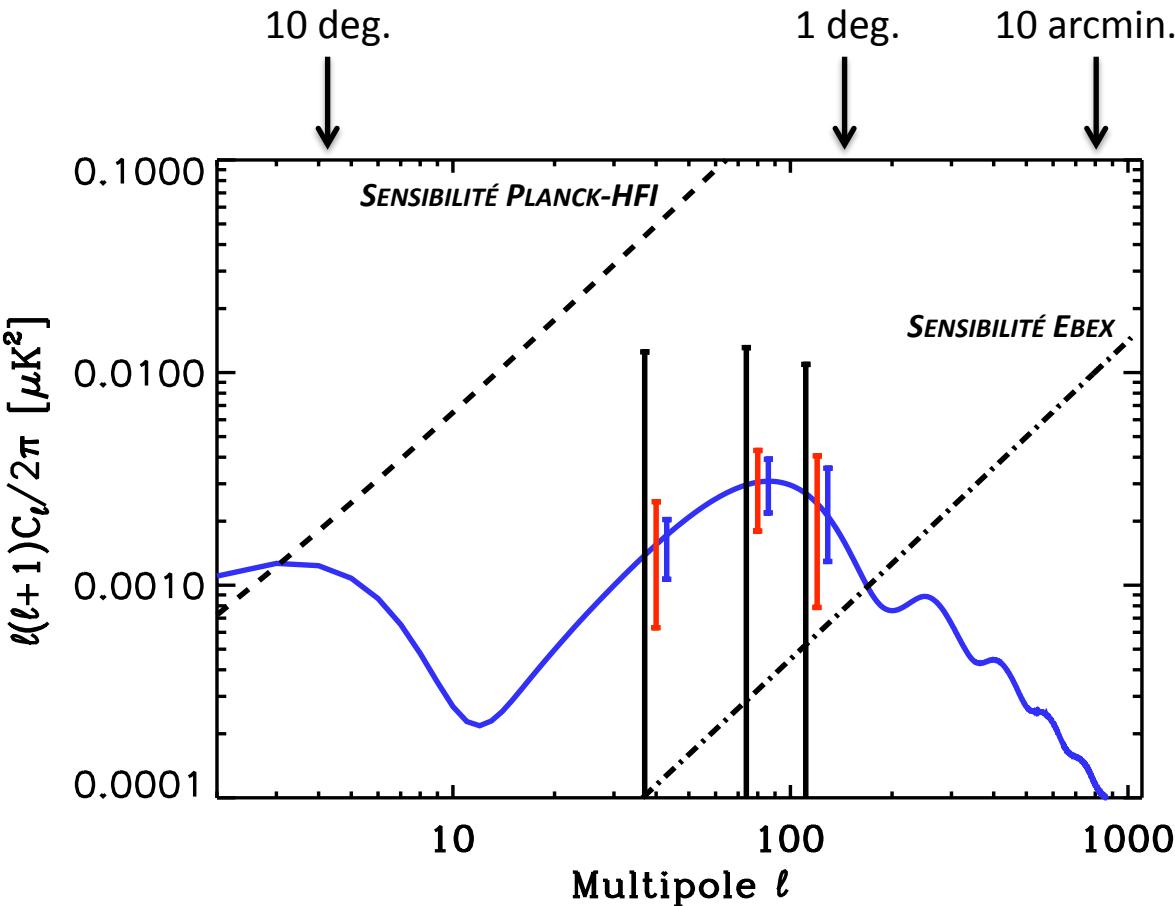
J. GRAIN, M. TRISTRAM & R. STOMPOR, PHYS. REV. D 79, 123515 (2009)

Q and *U* maps



EBEX (balloon)
 $f_{\text{sky}} \approx 1\%$

B-mode power spectrum



REMOVING E-MODES LEAKING INTO B-MODES

$$\begin{pmatrix} Q(\vec{n}) \\ U(\vec{n}) \end{pmatrix} = \mathbf{D}^E E(\vec{n}) + \mathbf{D}^B B(\vec{n}) \text{ with } \mathbf{D}^E \cdot \mathbf{D}^B = \mathbf{D}^B \cdot \mathbf{D}^E = 0$$

The standard way

$$a_{\ell m}^B = \int_{4\pi} (Q, U) \cdot \mathbf{D}^B Y_{\ell m} \times M$$

T. BUNN, M. ZALDARRIAGA, M. TEGMARK & A. DE OLIVEIRA-COSTA, PHYS. REV. D 67 023501 (2003)

K. SMITH, PHYS. REV. D 74 083002 (2006)

K. SMITH & M. ZALDARRIAGA, PHYS. REV. D 76 043001 (2007)

$$a_{\ell m}^B = \int_{S<4\pi} \mathbf{D}^B \cdot (Q, U) \times Y_{\ell m} + \oint_{C_S} (Q, U) \partial Y_{\ell m} + \oint_{C_S} \partial (Q, U) Y_{\ell m}$$

B-modes only

B-modes and E-modes

E-to-B mixing and L-to-L' mixing

$$\begin{pmatrix} \tilde{E}_{\ell m} \\ \tilde{B}_{\ell m} \end{pmatrix} = \sum_{\ell' m'} \begin{pmatrix} W_{\ell m, \ell' m'}^+ & iW_{\ell m, \ell' m'}^- \\ -iW_{\ell m, \ell' m'}^- & W_{\ell m, \ell' m'}^+ \end{pmatrix} \begin{pmatrix} a_{\ell' m'}^E \\ a_{\ell' m'}^B \end{pmatrix}$$

✓ E-B and L-L' separation on average
BUT
✓ for any realization : E variance leaks into B variance

$$\begin{pmatrix} \langle \tilde{C}_\ell^E \rangle \\ \langle \tilde{C}_\ell^B \rangle \end{pmatrix} = \frac{1}{2\ell+1} \sum_m \begin{pmatrix} \langle |\tilde{E}_{\ell m}|^2 \rangle \\ \langle |\tilde{B}_{\ell m}|^2 \rangle \end{pmatrix} = \sum_{\ell'} \begin{pmatrix} M_{\ell, \ell'}^+ & M_{\ell, \ell'}^- \\ M_{\ell, \ell'}^- & M_{\ell, \ell'}^+ \end{pmatrix} \begin{pmatrix} C_{\ell'}^E \\ C_{\ell'}^B \end{pmatrix}$$

REMOVING E-MODES LEAKING INTO B-MODES

$$\begin{pmatrix} Q(\vec{n}) \\ U(\vec{n}) \end{pmatrix} = \mathbf{D}^E E(\vec{n}) + \mathbf{D}^B B(\vec{n}) \text{ with } \mathbf{D}^E \cdot \mathbf{D}^B = \mathbf{D}^B \cdot \mathbf{D}^E = 0$$

The standard way

$$a_{\ell m}^B = \int_{4\pi} (Q, U) \cdot \mathbf{D}^B Y_{\ell m} \times M$$

$$a_{\ell m}^B = \int_{S < 4\pi} \mathbf{D}^B \cdot (Q, U) \times Y_{\ell m} + \oint_{C_S} (Q, U) \partial Y_{\ell m} + \oint_{C_S} \partial (Q, U) Y_{\ell m}$$

B-modes only

B-modes and E-modes

The pure way

$$a_{\ell m}^B = \int_{4\pi} (Q, U) \cdot \mathbf{D}^B (W Y_{\ell m})$$

$$a_{\ell m}^B = \int_{S < 4\pi} \mathbf{D}^B \cdot (Q, U) \times W Y_{\ell m}$$

B-modes only

$$+ \oint_{C_S} (Q, U) \partial (W Y_{\ell m}) + \oint_{C_S} \partial (Q, U) \times W Y_{\ell m}$$

Vanish if $W=0$ and $dW=0$ on C_S

REMOVING E-MODES LEAKING INTO B-MODES

$$\begin{pmatrix} Q(\vec{n}) \\ U(\vec{n}) \end{pmatrix} = \mathbf{D}^E E(\vec{n}) + \mathbf{D}^B B(\vec{n}) \text{ with } \mathbf{D}^E \cdot \mathbf{D}^B = \mathbf{D}^B \cdot \mathbf{D}^E = 0$$

The *pure* way

$$a_{\ell m}^B = \int_{4\pi} (Q, U) \cdot \mathbf{D}^B (WY_{\ell m})$$

$$a_{\ell m}^B := \int_{S < 4\pi} \mathbf{D}^B \cdot (Q, U) \times WY_{\ell m}$$

B-modes only

$$+ \oint_{C_S} (Q, U) \partial(WY_{\ell m}) + \oint_{C_S} \partial(Q, U) \times WY_{\ell m}$$

Vanish if $W=0$ and $dW=0$ on C_S

ONLY L-to-L' mixing

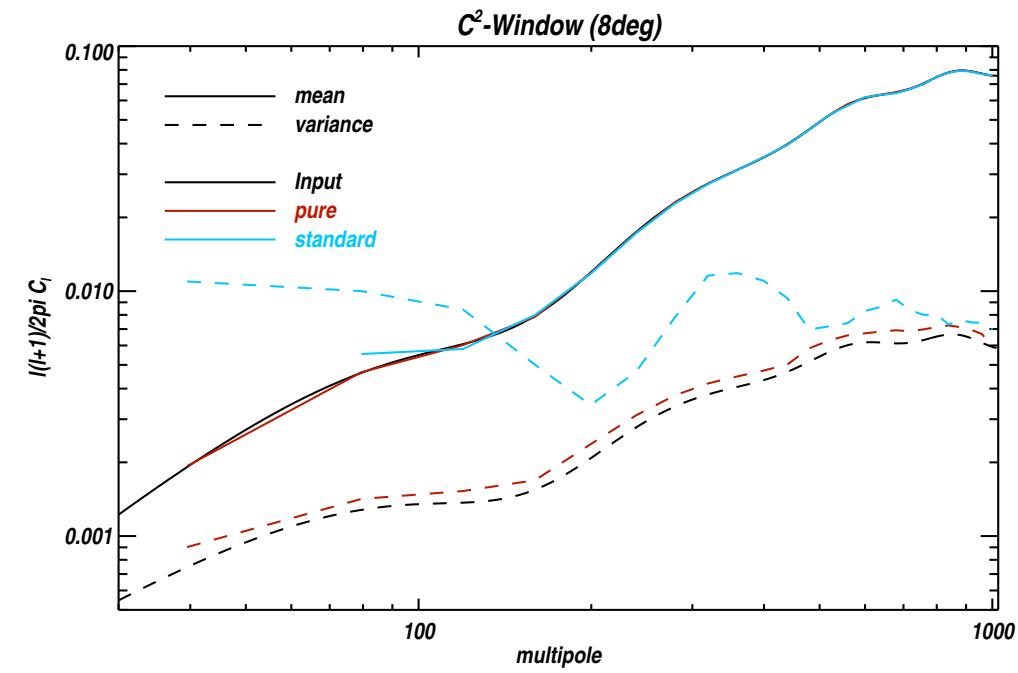
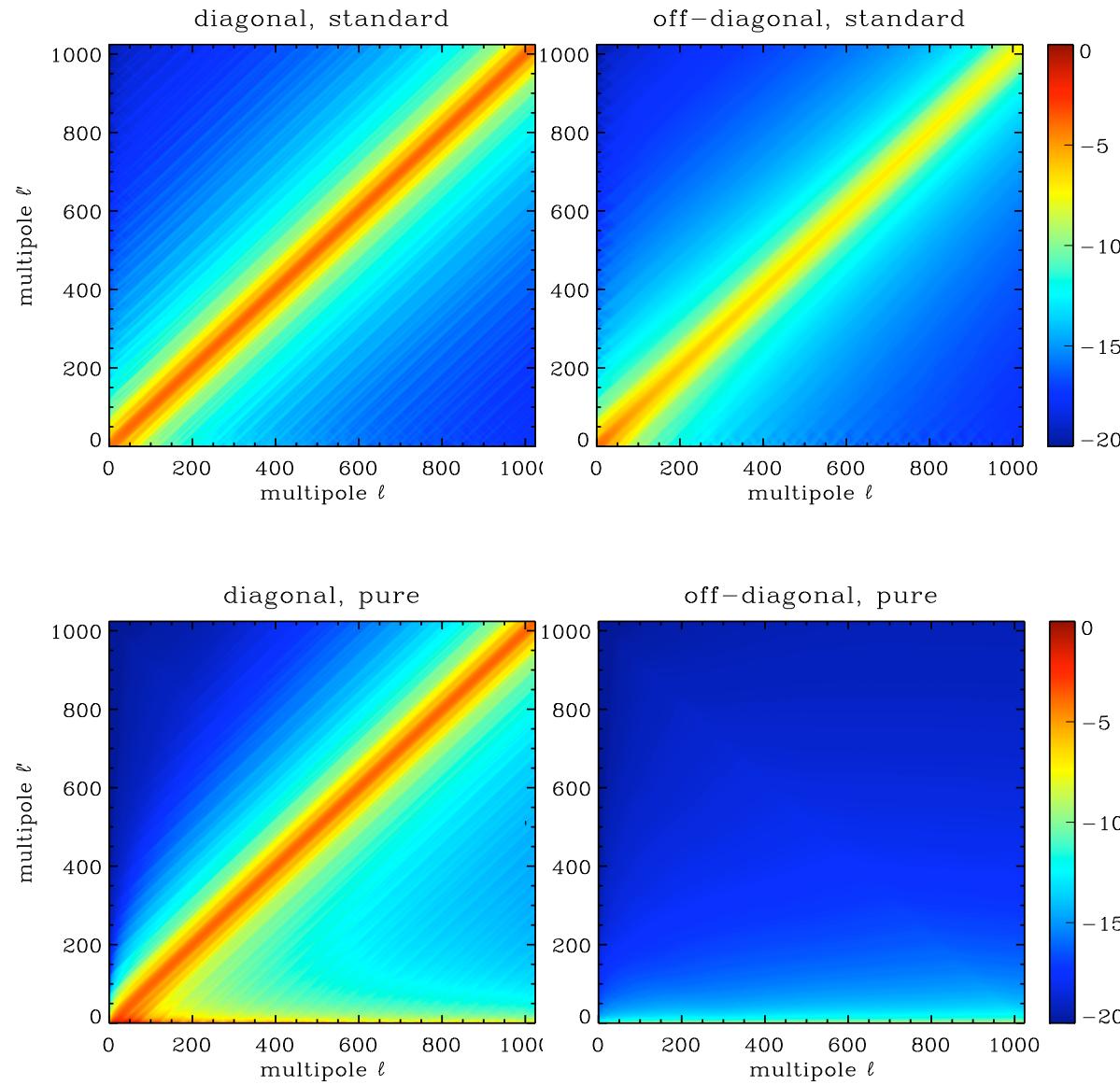
$$\begin{pmatrix} \tilde{E}_{\ell m} \\ \tilde{B}_{\ell m} \end{pmatrix} = \sum_{\ell' m'} \begin{pmatrix} W_{\ell m, \ell' m'}^+ & 0 \\ 0 & W_{\ell m, \ell' m'}^+ \end{pmatrix} \begin{pmatrix} a_{\ell' m'}^E \\ a_{\ell' m'}^B \end{pmatrix}$$

✓ E-B separation for any realizations :
E variance **DOES** leaks into B variance

✓ L-L' separation on average

$$\begin{pmatrix} \langle \tilde{C}_\ell^E \rangle \\ \langle \tilde{C}_\ell^B \rangle \end{pmatrix} = \frac{1}{2\ell+1} \sum_m \begin{pmatrix} \langle |\tilde{E}_{\ell m}|^2 \rangle \\ \langle |\tilde{B}_{\ell m}|^2 \rangle \end{pmatrix} = \sum_{\ell'} \begin{pmatrix} M_{\ell, \ell'}^+ & 0 \\ 0 & M_{\ell, \ell'}^+ \end{pmatrix} \begin{pmatrix} C_{\ell'}^E \\ C_{\ell'}^B \end{pmatrix}$$

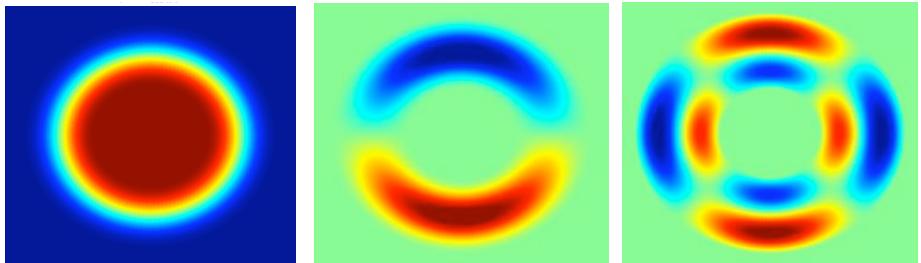
INDEED, THE LEAKAGE IS UNDER CONTROL



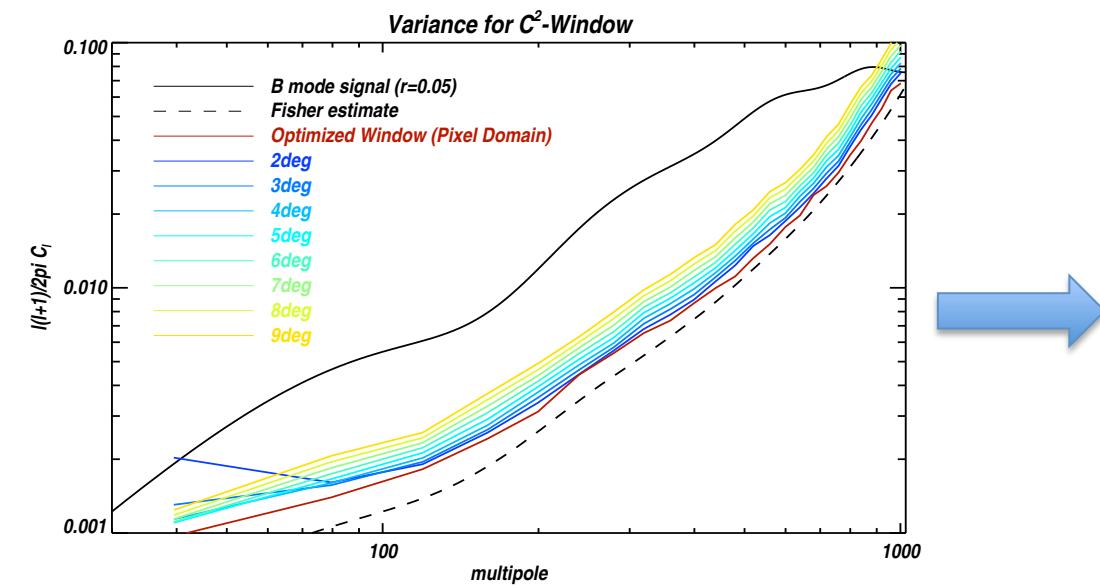
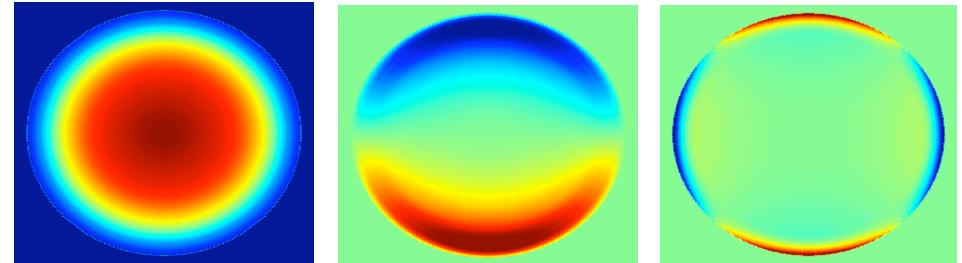
POWER SPECTRA UNCERTAINTIES : IDEAL CASE

$f_{sky}=1\%$ and $\sigma=5,75\mu\text{K-arcmin}$.

Analytic weighting



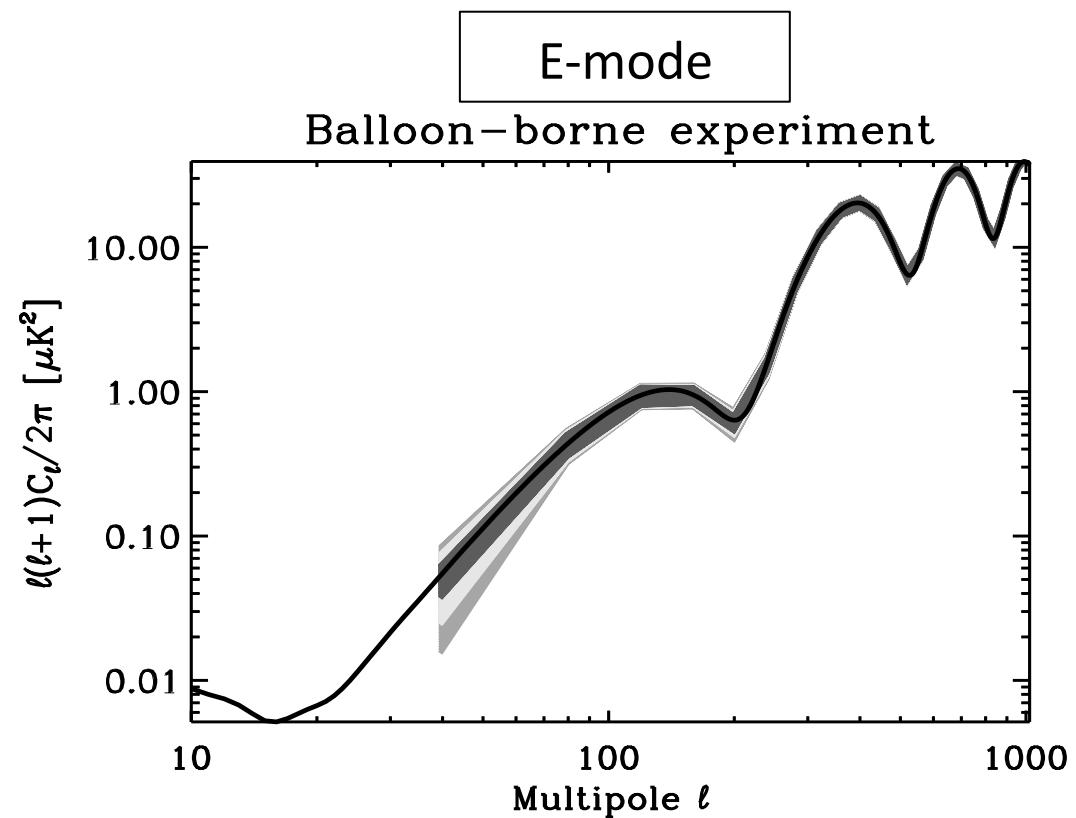
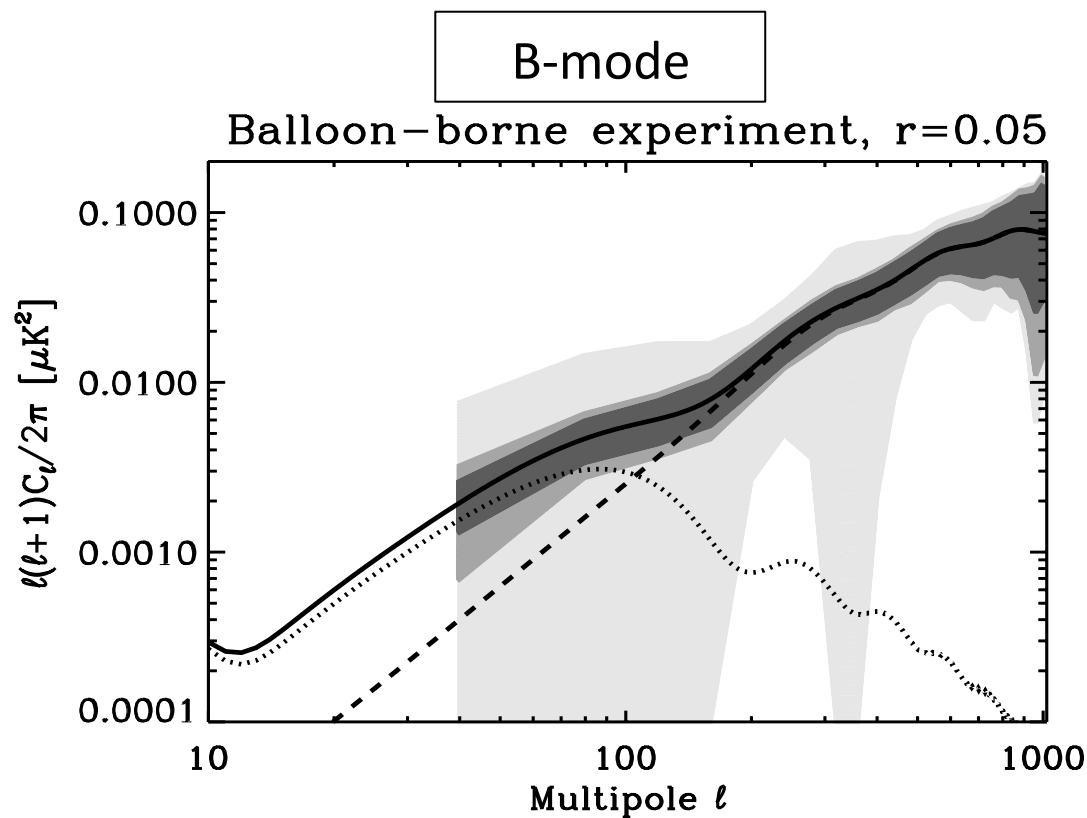
Optimal weighting



Optimization is reached
→ needed for all type of weighting

TO RECAP...

- **Fast** approach: $(N_{pix})^{3/2}$ au lieu de $(N_{pix})^3$
- **Precise** approach : $Var(C_\ell^B) \approx 2 \times Var_{optimal}(C_\ell^B)$
- Efficient alternative to optimal methods and a Monte-Carlo tool



FOREGROUND CLEANING

Performances of parametric ML component separation method for B-mode detection

STOMPOR, LEACH, STIVOLI, BACCIGALUPI, MNRAS 392, 216 (2009)

Comparison : foreground residual vs. CMB

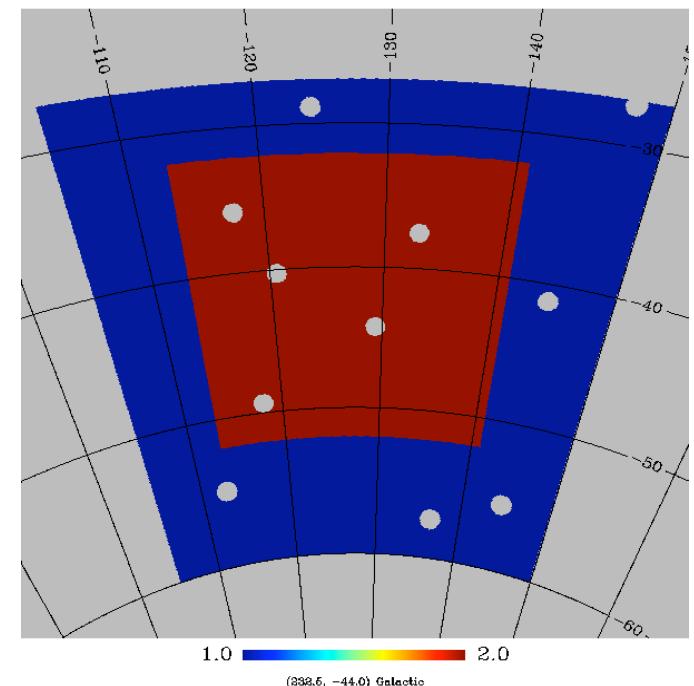
- Pixel space : $B \ll E$ for CMB (Q, U maps dominated by E) and $E \sim B$ for foregrounds residuals
→ $(Q, U)_{\text{CMB}} \gg (Q, U)_{\text{residuals}}$ implies $E_{\text{CMB}} \gg E_{\text{residual}}$ (eventually $E_{\text{CMB}} \gg E_{\text{residual}} \sim B_{\text{residual}} \gg B_{\text{CMB}}$)
- E/B harmonic space : $C_{\ell, E}^{(CMB)} \gg C_{\ell, E}^{(\text{residual})}$ and $C_{\ell, B}^{(CMB)} \gg C_{\ell, B}^{(\text{residual})}$

Balloon-borne experiment

- Frequencies : 150, 250 & 410 GHz
- Sky coverage : ~1 %
- Homogeneous noise : ~ $5.75 \mu K\text{-arcmin}^2$

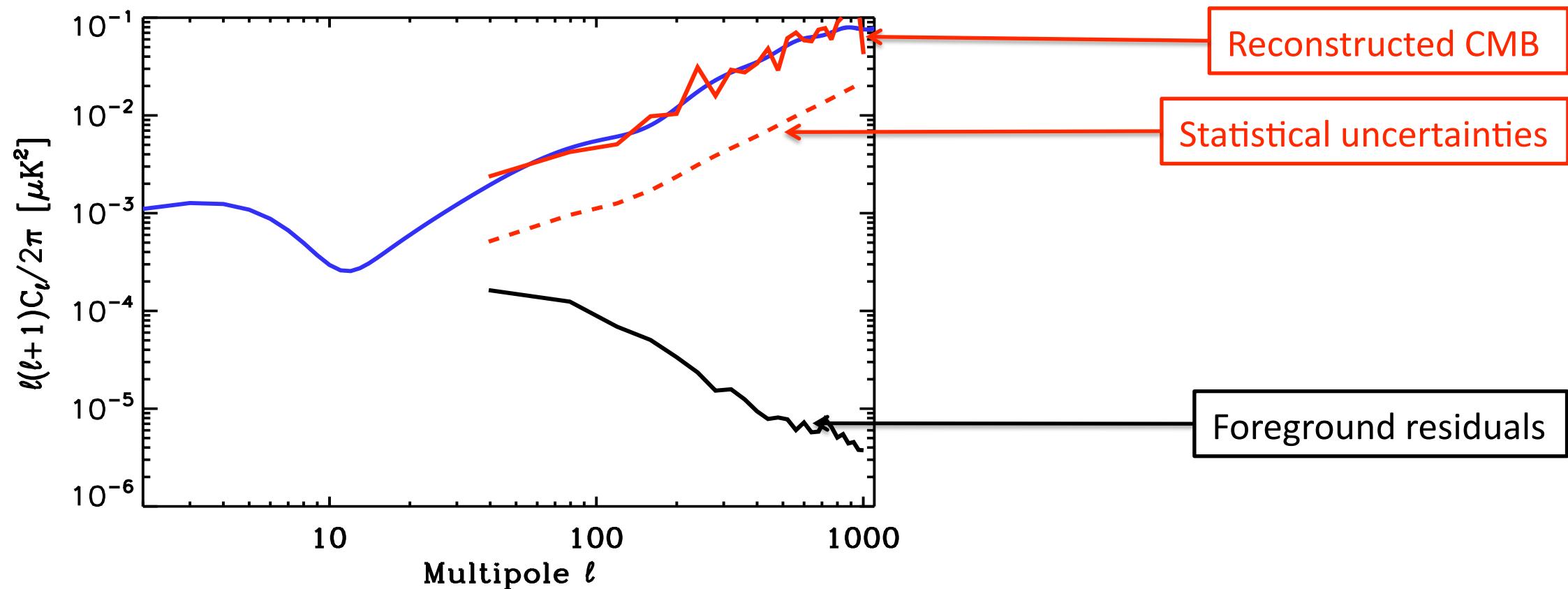
Ground-based experiment

- Frequencies : 90, 150 & 220 GHz
- Sky coverage : ~2 %
- Homogeneous noise : ~ $10 \mu K\text{-arcmin}^2$



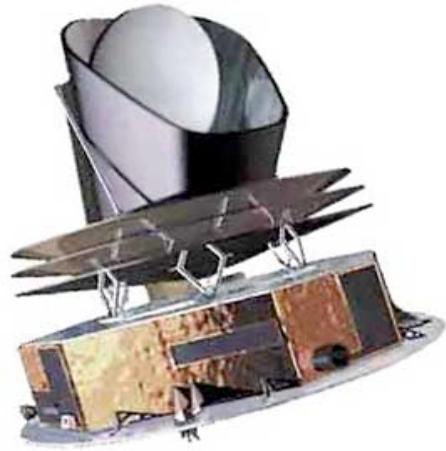
FOREGROUND CLEANING : RESULTS FOR BALLOON-BORNE EXPERIMENT

- Simulated sky : **CMB + synchrotron + dust** (different frequency scaling,different spatial scaling)
-
- Component Separation : **MIRAMARE** STOMPOR, LEACH, STIVOLI, BACCIGALUPI, MNRAS 392, 216 (2009)
- Power spectrum : **Xpure** GRAIN, TRISTRAM, STOMPOR, PRD 79, 123515 (2009)

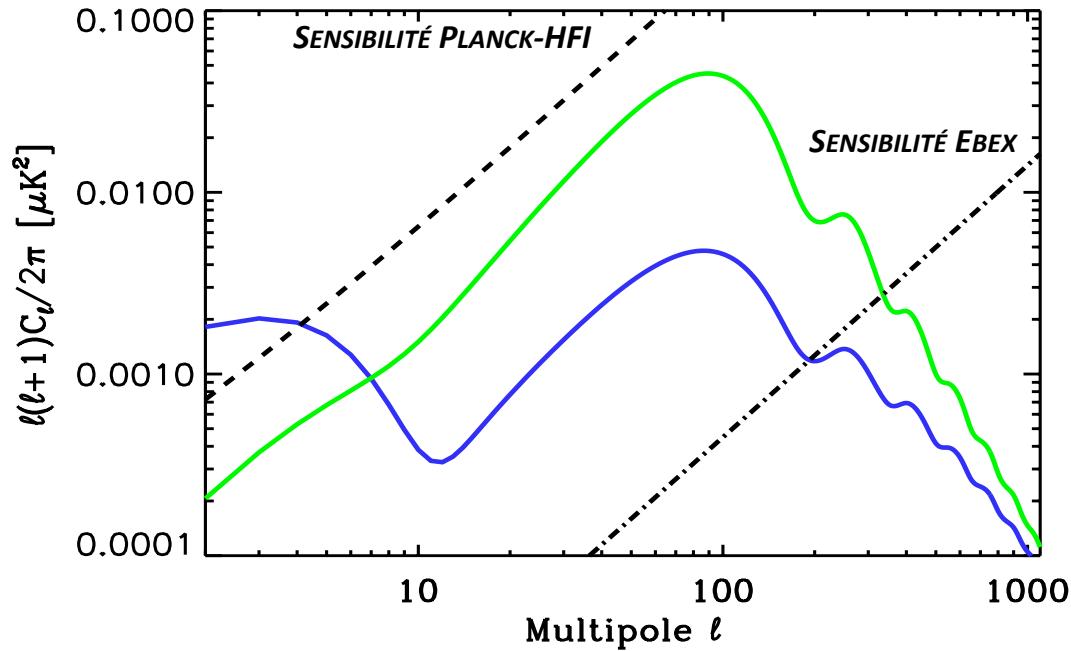


PLANCK-HFI, EBEX AND B-MODE

Planck-HFI



EBEX



- ✓ **Angular scale coverage:**
constraints on B-mode
- ✓ **EM frequency coverage:**
understanding of the foreground

- ✓ Estimation de $C_l^{E/B}$
- ✓ Fluctuations du CIB
- ✓ Contraintes sur 'l'inflation'

- ✓ Estimation de $C_l^{E/B}$
- ✓ Soustraction des avant-plans
- ✓ Effets systématiques