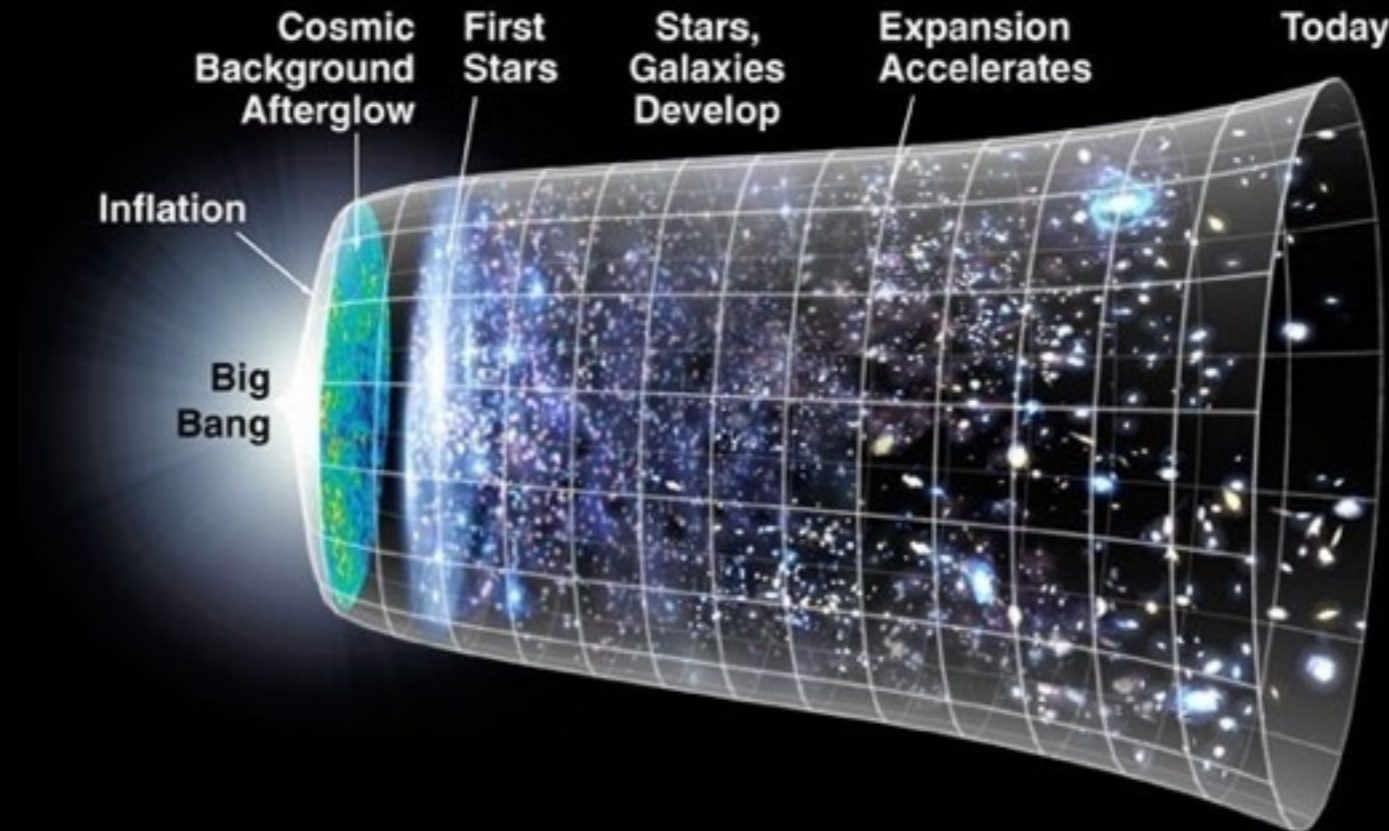


# Probing Inflation with Primordial Messengers



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IFT Madrid

October 25th 2020, IAP

# Inflation

- Inflation, the idea
- Single-field slow-roll scenario: successes and signatures
- The importance of upcoming-observations
- Axion inflation as a case study
- The “cosmological collider”
- Conclusions & Future work

# Inflation

$$3M_{\text{P}}^2 H^2 \simeq \rho_X$$

must satisfy:  $w_X \equiv p_X / \rho_X < -1/3$

What we learn

$$\frac{\ddot{a}}{a} = -\frac{1}{2M_{\text{P}}^2} (\rho + 3p)$$

acceleration!

$$\dot{\rho} + 3H(\rho + p) = 0$$

special case

$$p \simeq -\rho$$

# Inflation

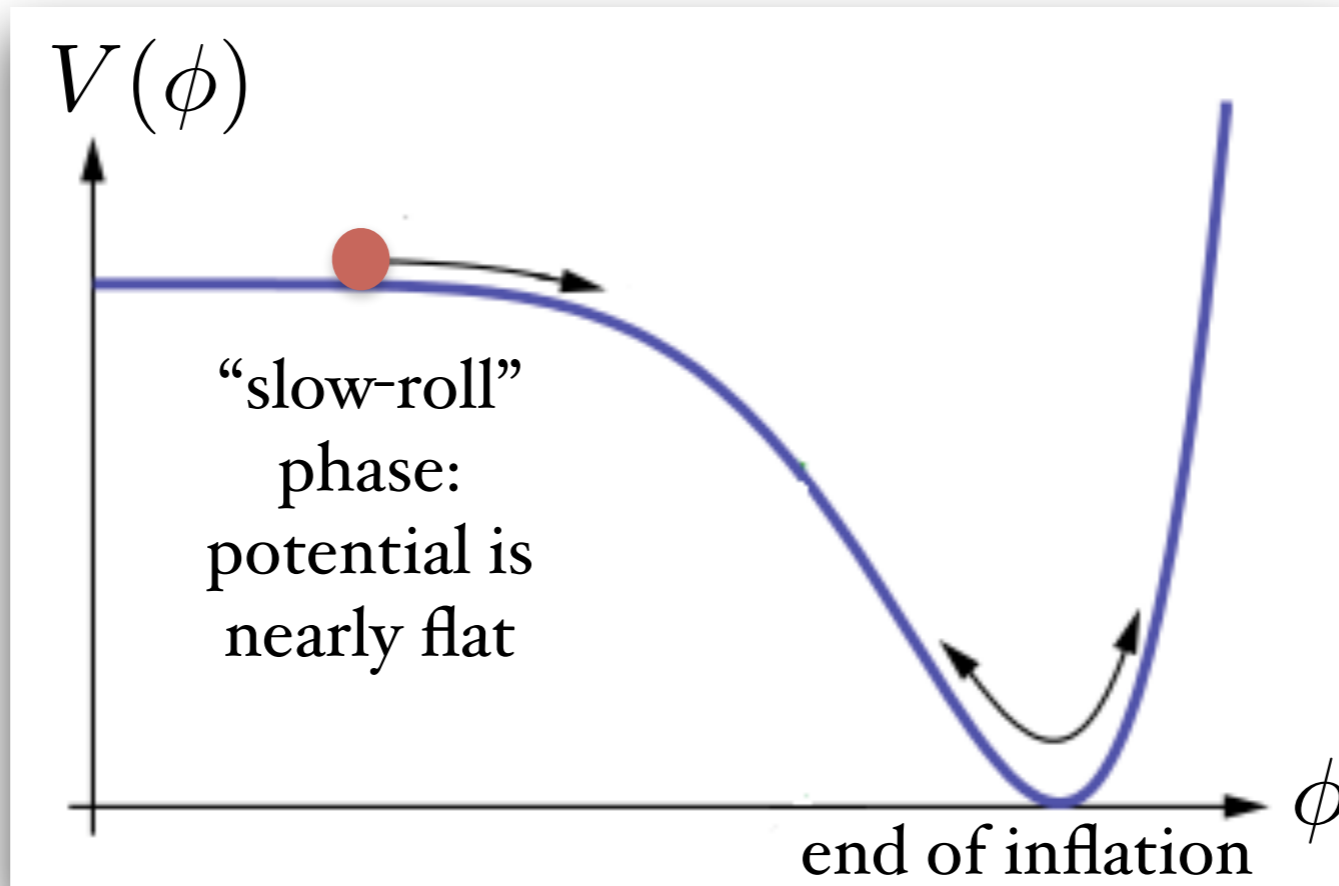
Simplest realization: single-scalar field in slow-roll

- Scalar field :

$$p_\phi = \frac{\dot{\phi}^2}{2} - V(\phi) \approx -V(\phi)$$
$$\rho_\phi = \frac{\dot{\phi}^2}{2} + V(\phi) \approx V(\phi)$$

$$\dot{\phi}^2 \ll V$$

$$p_\phi \approx -\rho_\phi$$



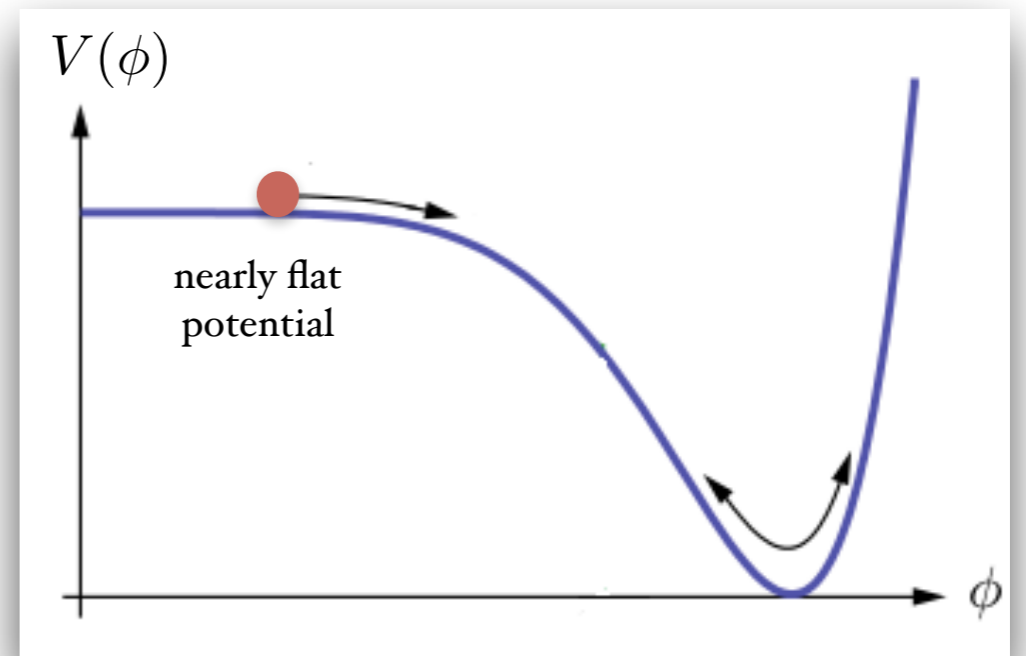
# Slow-roll

start flat

$$\epsilon \equiv -\frac{\dot{H}}{H^2} \simeq \frac{M_{\text{P}}^2}{2} \left( \frac{V'}{V} \right)^2 \simeq \frac{3}{2} \frac{\dot{\phi}^2}{V} \ll 1$$

stay flat

$$|\eta| \equiv \frac{|\dot{\epsilon}|}{H\epsilon} \simeq -\frac{2}{3} \left( \frac{V''}{H^2} \right) + 4\epsilon \ll 1$$



# Background + Fluctuations

$$\phi(\vec{x}, t) = \bar{\phi}(t) + \delta\phi(\vec{x}, t)$$



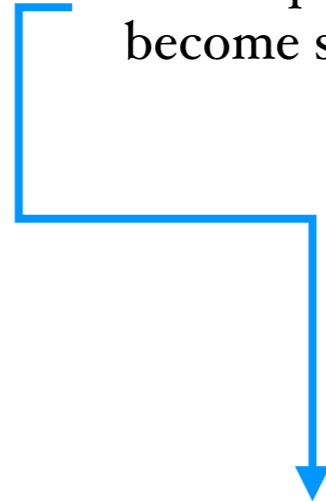
classical  
homogeneous  
background



quantum  
fluctuations



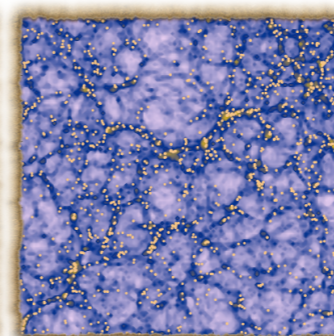
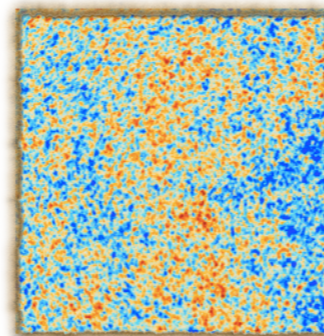
perturbation modes are stretched by the expansion,  
become super horizon and freeze out to their value at horizon exit



cosmological  
perturbations

$\Delta T$

$\delta\rho$



# Metric Fluctuations

$$ds^2 = (-dt^2 + a(t)^2 [e^{2\zeta} \delta_{ij} + \gamma_{ij}] dx^i dx^j)$$

scalar fluctuations

tensor perturbations

# Primordial power spectra

(minimal scenario)

scalar fluctuations

$$\mathcal{P}_\zeta(k) = \frac{1}{8\pi^2} \frac{1}{\epsilon} \frac{H^2}{M_{\text{pl}}^2} \left( \frac{k}{k_*} \right)^{n_s - 1}$$

$0.9649 \pm 0.0042$   
 $2.2 \times 10^{-9}$   
[ $k_* = 0.05 \text{ Mpc}^{-1}$ , 68% C.L.]  
from Planck measurements  
of CMB anisotropies

$$n_s - 1 \simeq -2\epsilon - \eta$$



# Primordial power spectra

(vacuum fluctuations)

tensor fluctuations

energy scale of inflation

**red tilt**

$$\mathcal{P}_\gamma^{\text{vacuum}}(k) = \frac{2}{\pi^2} \frac{H^2}{M_{\text{pl}}^2} \left( \frac{k}{k_*} \right)^{n_T}$$

$n_T$

$$n_T \simeq -2\epsilon \simeq -r/8$$

$$r \equiv \frac{\mathcal{P}_\gamma}{\mathcal{P}_\zeta} \quad \text{tensor-to-scalar ratio}$$

bounds

**current**

$$r < 0.056 \text{ (95\%CL, Planck}^{\text{+}})$$

**future**

$$r < 0.01 \text{ (CMB-S3)}$$

$$r < 0.001 \text{ (CMB-S4)}$$

# Crossing Qualitative Thresholds

agnostic/naive

$$n_s - 1 \simeq -2\epsilon - \eta$$

$$\epsilon \sim \eta$$

$\implies$

$$r \gtrsim 10^{-2}$$

compelling  
models  
e.g. Starobinsky

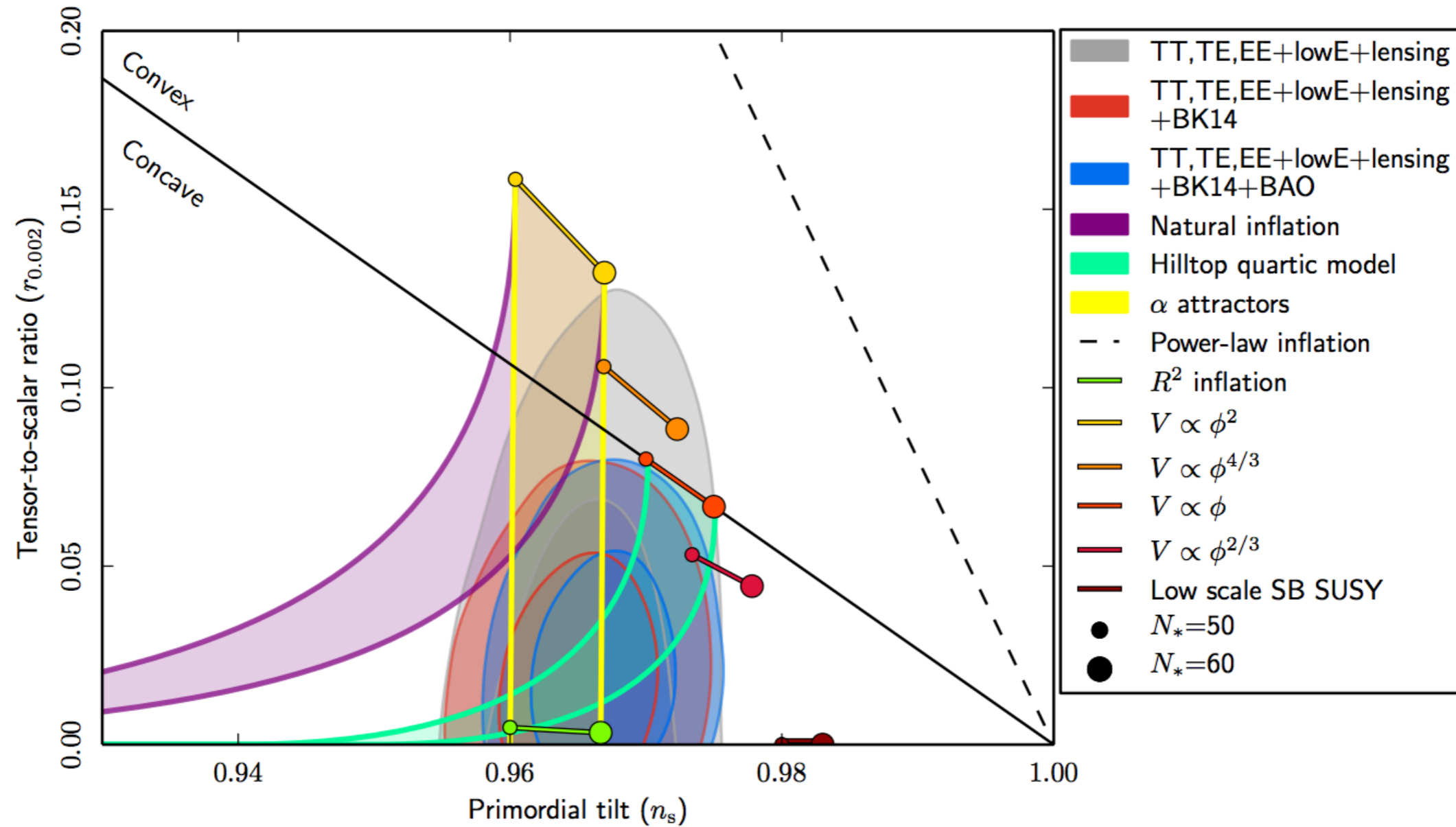
$$1 - n_s \simeq \frac{2}{N}, \quad r \simeq \frac{12}{N^2}$$

$\implies$

$$r \gtrsim 10^{-3}$$

# Single-field Inflation is doing well

Planck Collaboration: Constraints on Inflation



# Why go beyond the single-field scenario?

**interpreting observations**

what to infer from GW detection?  
e.g.  $r \leftrightarrow H$  relation

**likely**

string theory

|

flux compactifications

|

4D EFT with many moduli fields

**interesting**

signatures of new content  
on GW spectrum:  
PS: scale-dependence, chirality,  
n-G: (amplitude, shape, angular..)

# Focus

1 (class of) model(s): axion inflation

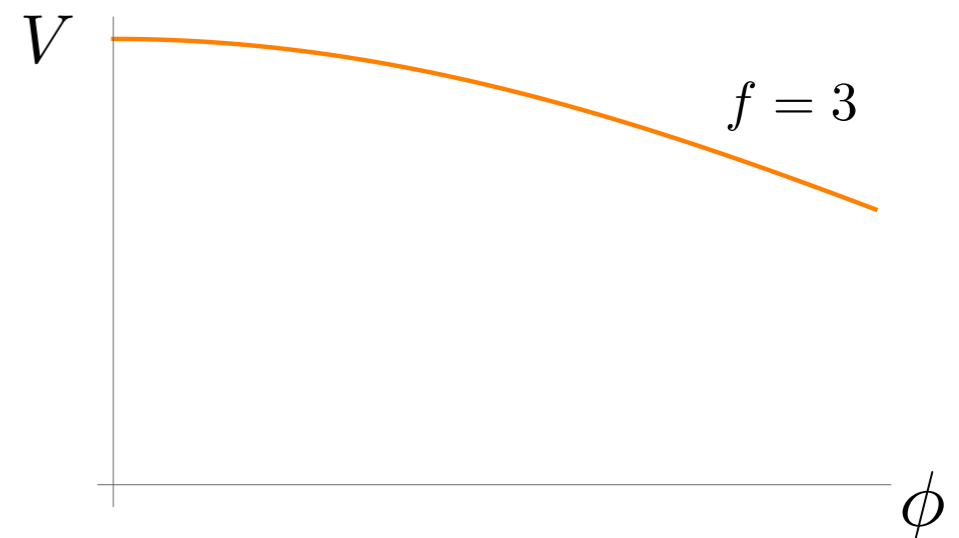
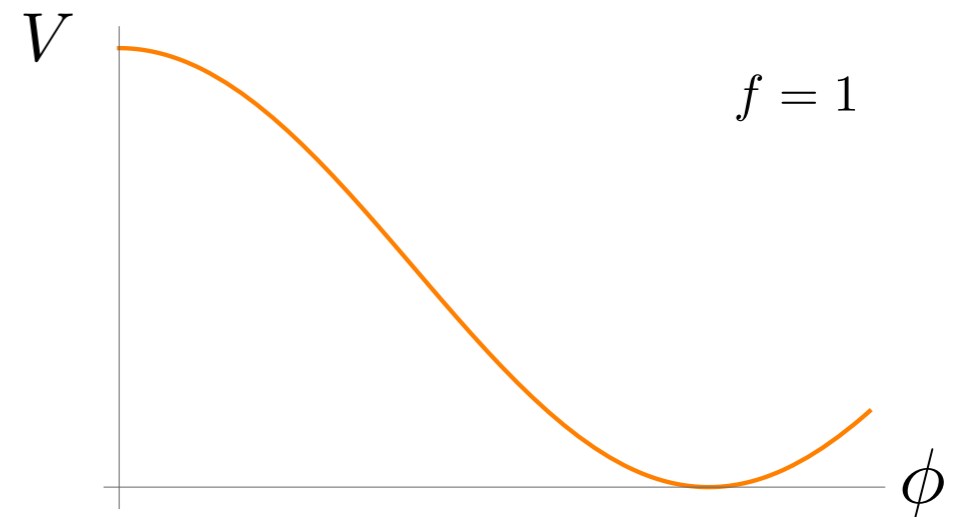
1 probe: primordial gravitational waves

# Natural Inflation

$$\mathcal{L} = \sqrt{-g} \left[ R[g] - (\partial\phi)^2 - \mu^4 (1 + \text{Cos}[\phi/f]) \right]$$

[Freese, Frieman, Olinto]

axion-like potential



simple

(technically) natural: shift symmetry

viable for  $f \gtrsim M_{\text{P}}$

# Chromo Natural Inflation

[Adshead, Wyman]  
[Dimastrogiovanni, **MF**, Tolley]  
[...]

$$\mathcal{L} \supset -\frac{1}{4}F^2 + \frac{\lambda\phi}{4f}F\tilde{F} - (\partial\phi)^2 - U_{\text{axion}}(\phi)$$

[Freese, Frieman, Olinto]  
[...]

◆  $\left\{ \begin{array}{l} f \ll M_{\text{P}} \quad \text{realization} \\ \text{very interesting GW signatures!} \end{array} \right.$

# Extension of Chromo Natural Inflation

[Dimastrogiovanni, MF, Fujita]

$$\mathcal{L} \supset \mathcal{L}_{\text{inflaton}} - \frac{1}{4} F^2 + \frac{\lambda \chi}{4f} F \tilde{F} - (\partial \chi)^2 - U_{\text{axion}}(\chi)$$

- ◆  $f \ll M_{\text{P}}$  realization
- same interesting GW spectrum
- observationally viable

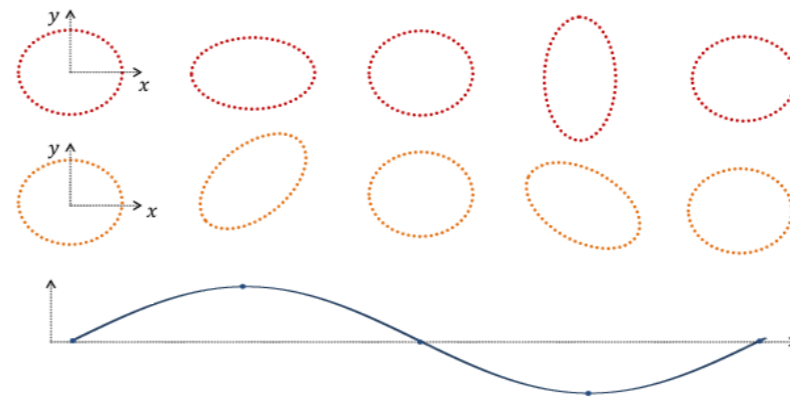


# (Primordial) Gravitational Waves

$$G_{\mu\nu} = 8\pi G T_{\mu\nu}$$

$$ds^2 = -dt^2 + a^2(t) (\delta_{ij} + \gamma_{ij}) dx^i dx^j$$

$$\gamma_i^i = \partial_i \gamma_{ij} = 0 \quad \text{two polarization states}$$



$$\ddot{\gamma}_{ij} + 3H\dot{\gamma}_{ij} + k^2\gamma_{ij} = 16\pi G \Pi_{ij}^{TT}$$

anisotropic stress-energy tensor

# Primordial GW in our Model

$$\mathcal{L} \supset \mathcal{L}_{\text{inflaton}} - \frac{1}{4} F^2 + \frac{\lambda \chi}{4f} F \tilde{F} - (\partial \chi)^2 - U_{\text{axion}}(\chi)$$

$$\text{SU}(2) \begin{cases} A_0^a = 0 \\ A_i^a = a Q \delta_i^a \\ \delta A_i^a = t_{ai} + \dots \end{cases}$$

$$\ddot{\gamma}_{ij}^\lambda + 3H \dot{\gamma}_{ij}^\lambda + k^2 \gamma_{ij}^\lambda \propto t_{ij}^\lambda + \dots + \dots$$

[Dimastrogiovanni, **MF**, Fujita]

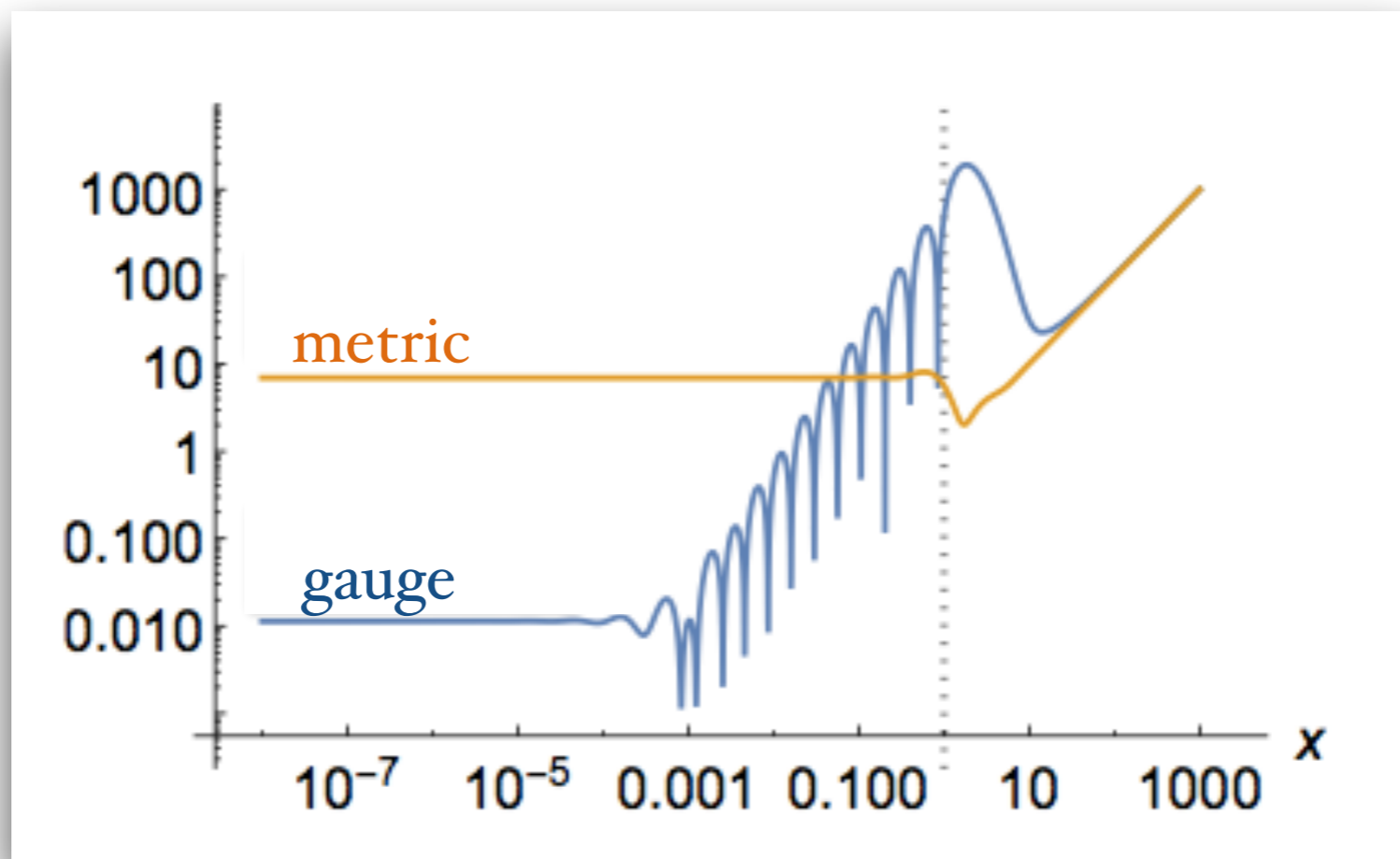
$$P_\lambda^{\text{sourced}} \gtrsim P_\lambda^{\text{vacuum}}$$

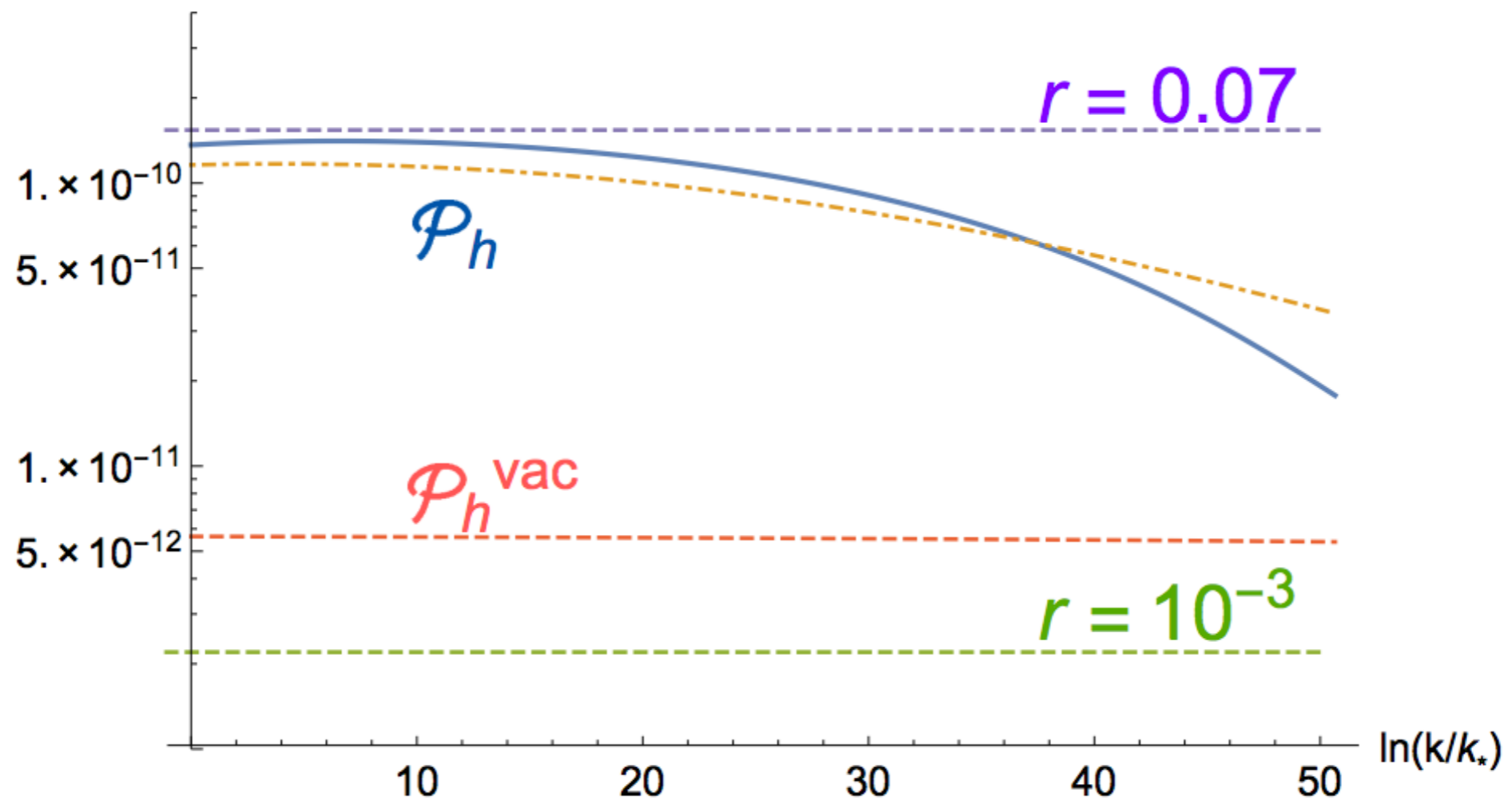
now possible!

$$\left\{ \begin{array}{l} \text{metric} \\ \text{gauge} \end{array} \right. \left\{ \begin{array}{l} \Psi''_{R,L} + \left(1 - \frac{2}{x^2}\right) \Psi_{R,L} = \mathcal{O}^{(1)}(t_{R,L}) \\ t''_{R,L} + \left[1 + \frac{2m_Q \xi}{x^2} \mp \frac{2}{x} (m_Q + \xi)\right] t_{R,L} = \tilde{\mathcal{O}}^{(1)}(\Psi_{R,L}) \end{array} \right.$$

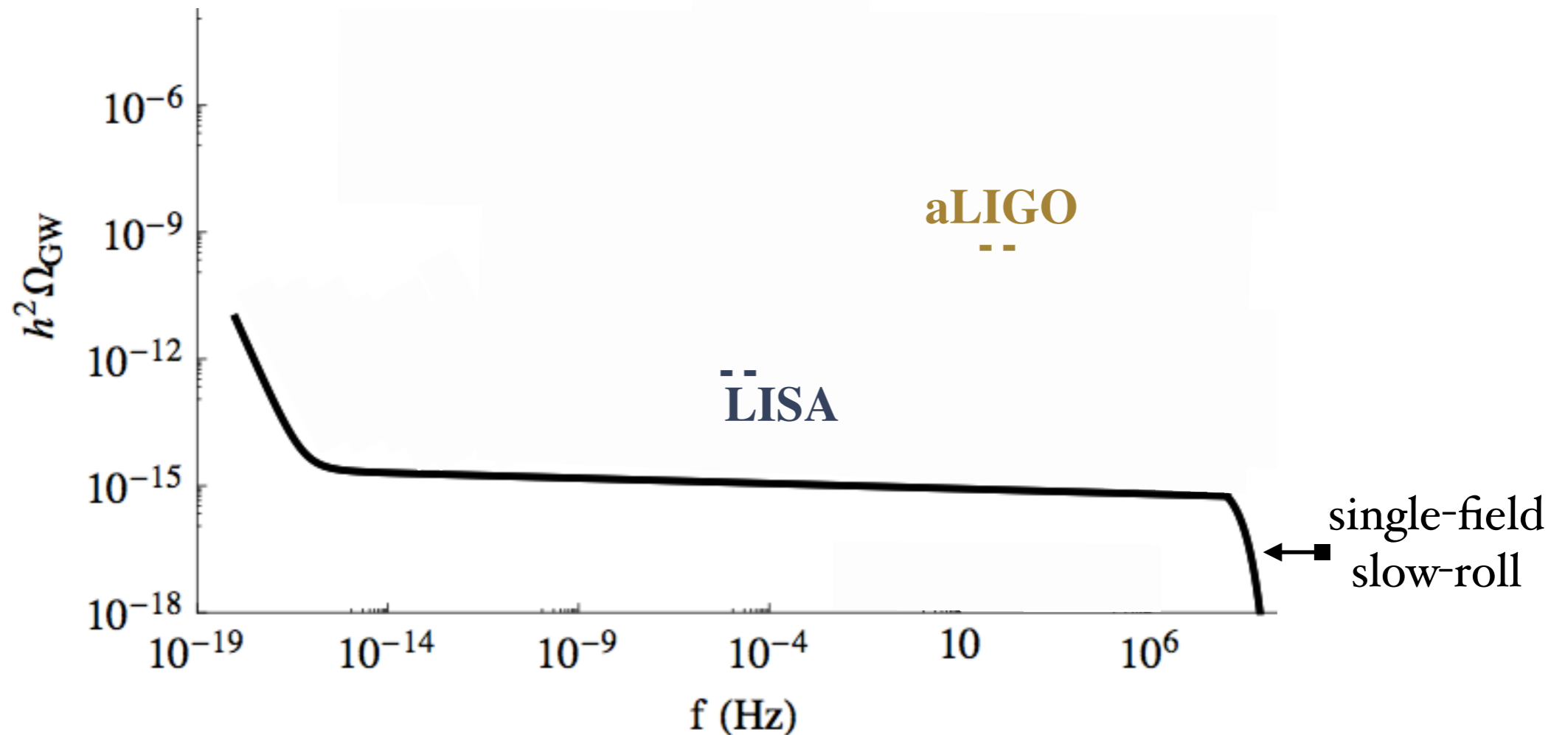
$$\xi = \frac{\lambda \dot{\chi}}{2fH}$$

$$x \sim -k\tau$$





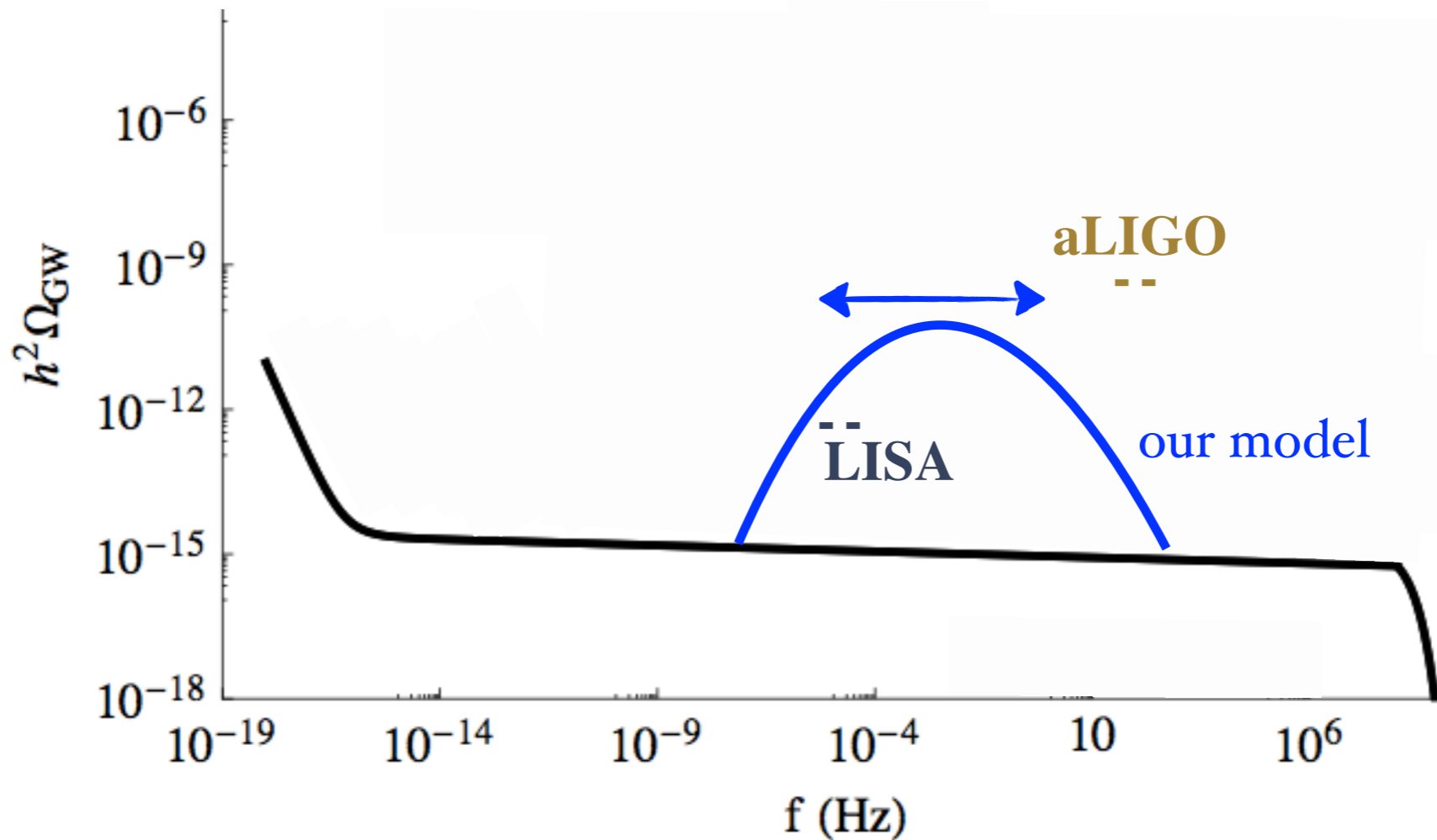
# Testing Amplitude & Scale Dependence



Laser Interferometers: new frontier to test primordial physics (GW) at small scales

LISA:  $10^{-4}\text{Hz} \lesssim f \lesssim 10^{-1}\text{Hz}$  ; LIGO+:  $1\text{Hz} \lesssim f \lesssim 10^3\text{Hz}$

# Testing Amplitude & Scale Dependence



“  ” freedom in parameter space

# Chirality

(background +) Chern-Simons coupling  $\frac{\lambda\chi}{4f} F \tilde{F}$

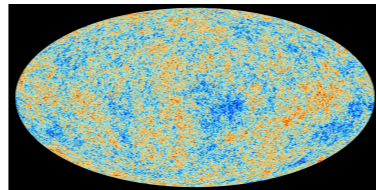
$$\ddot{t}_{ij}^{L/R} \pm \lambda(\dots) t_{ij}^{L/R} + \dots = 0$$

$$\gamma_{ij}^L \neq \gamma_{ij}^R$$

chiral spectrum

$$\mathcal{P}_{\gamma}^L \neq \mathcal{P}_{\gamma}^R$$

# Chirality



CMB tests

single-field  
slow-roll inflation

no chirality

$$\langle BT \rangle = 0 = \langle EB \rangle$$

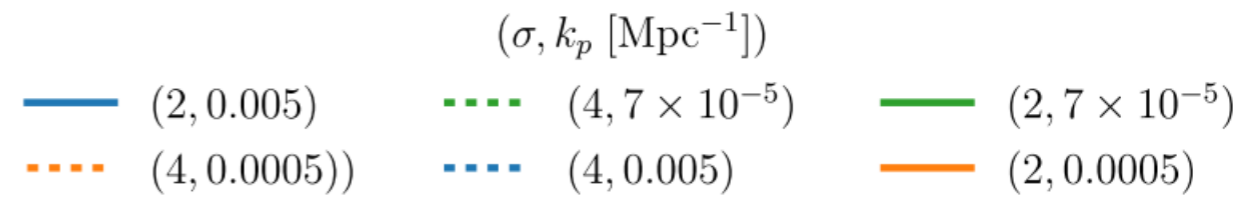
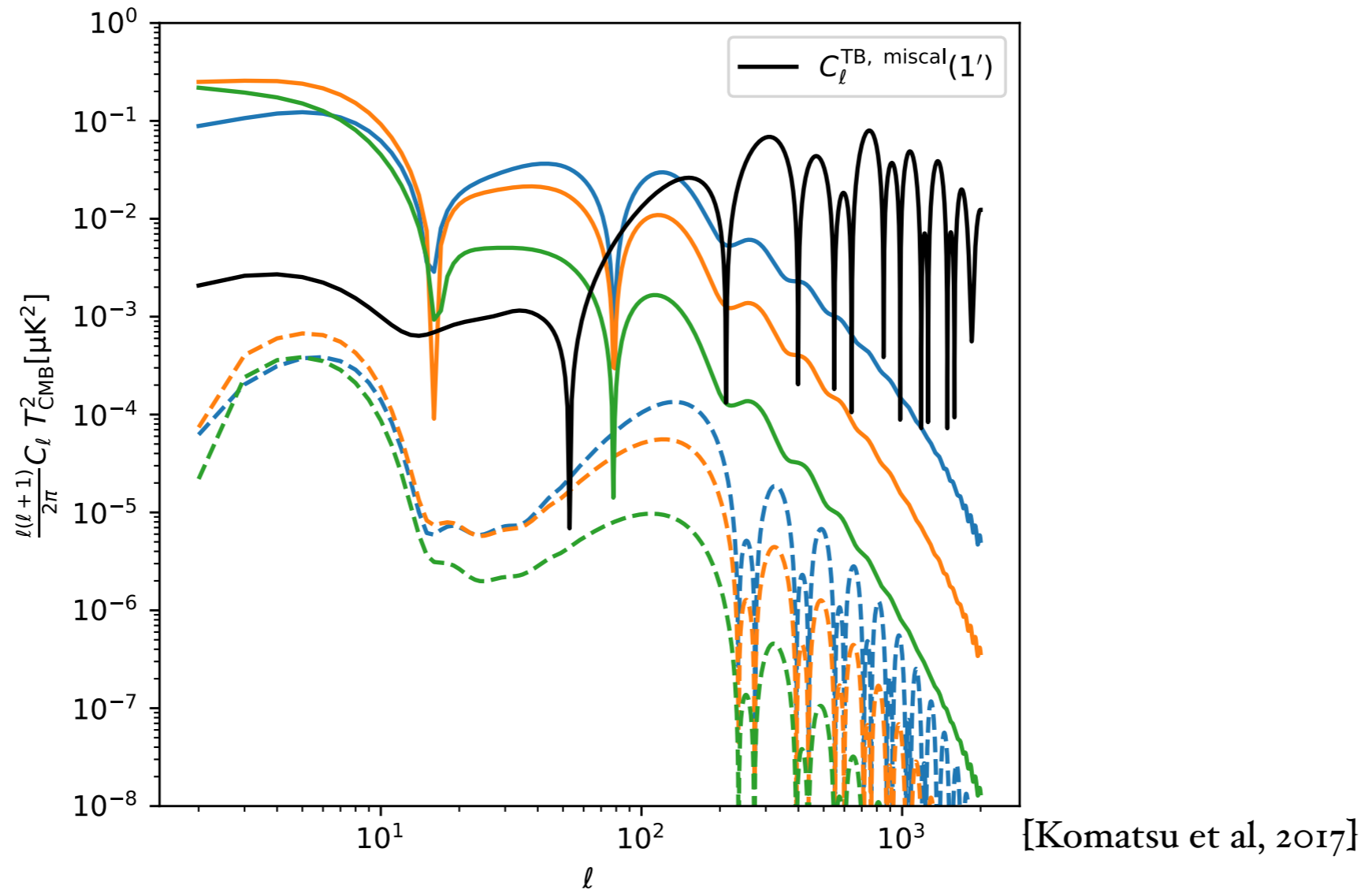
Chern-Simons  
coupling

chirality

$$\langle BT \rangle \neq 0 \neq \langle EB \rangle$$



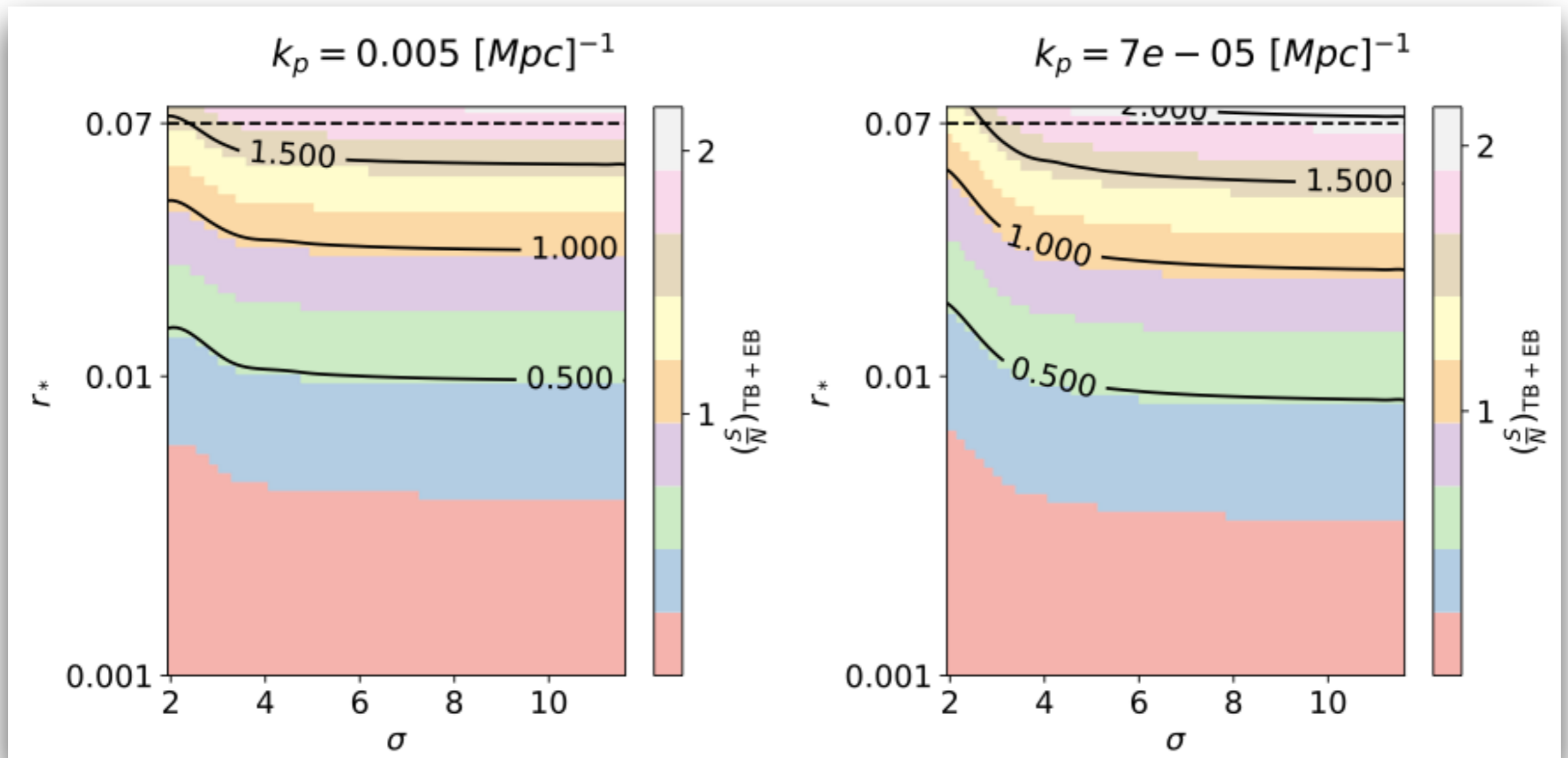
# LiteBIRD



$$\mathcal{P}_h^{\text{sourced}} = r_* \mathcal{P}_\zeta \text{Exp} \left[ -\frac{1}{2\sigma^2} \ln^2 \left( \frac{k}{k_p} \right) \right]$$

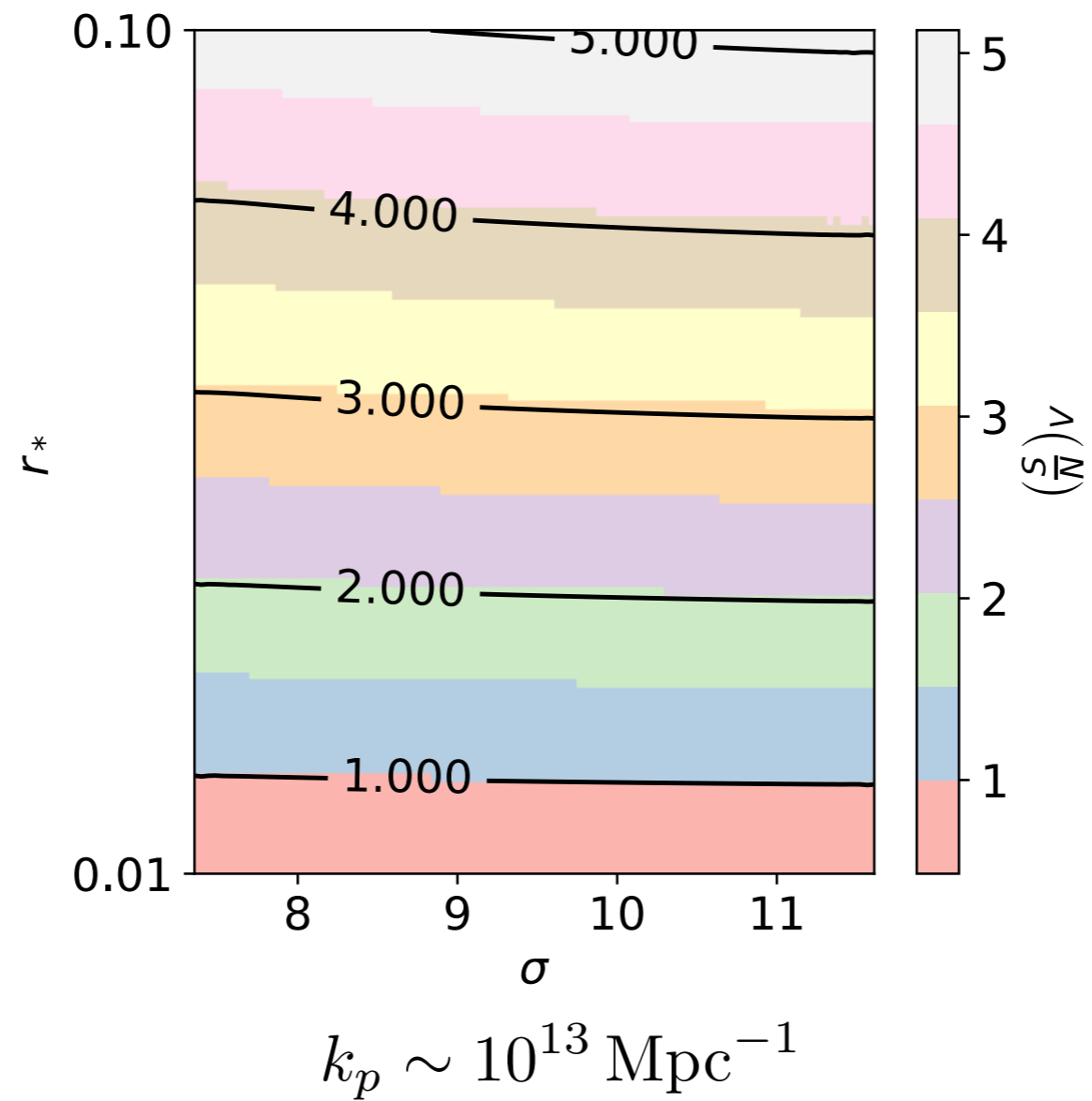
# Extended Chromo-Natural

gravitational waves forecast: LiteBIRD

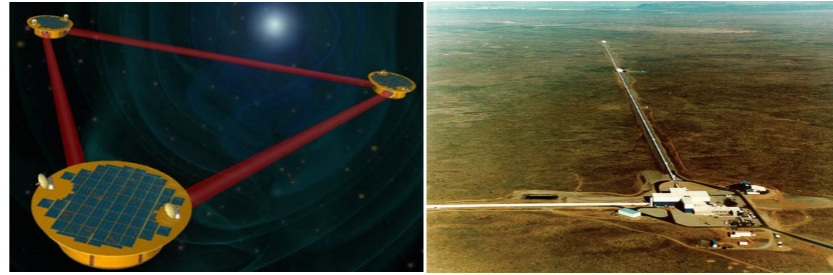


# Extended Chromo-Natural

## Big Bang Observer



# Chirality

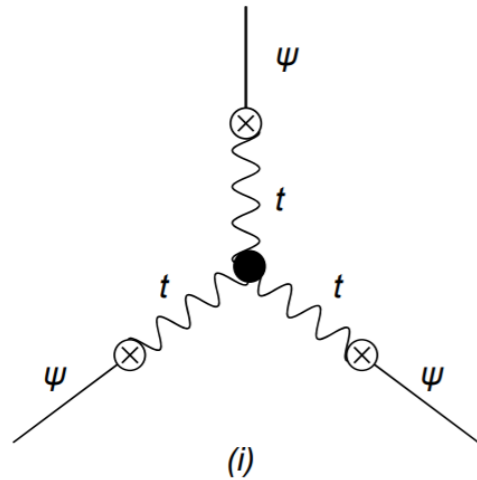


## Interferometers tests

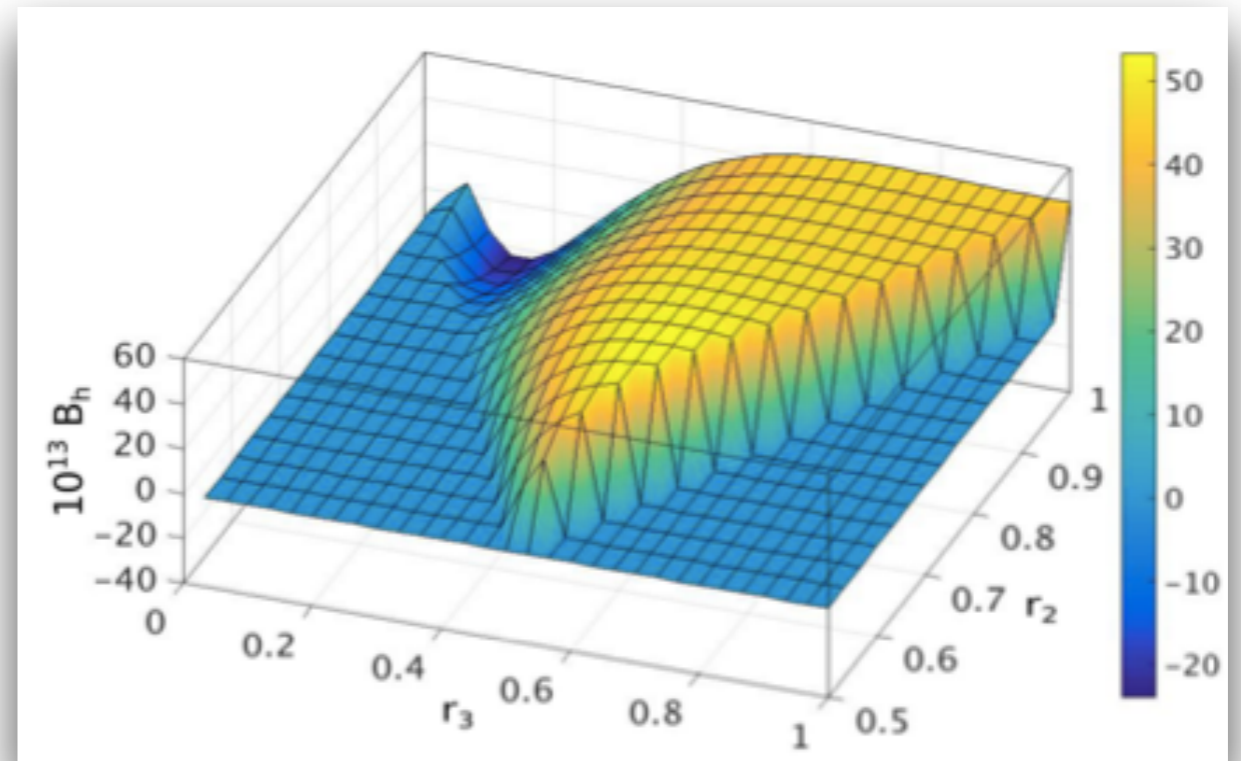
- ◆ cross-correlation between interferometers at different locations  
[Smith, Caldwell 2017]
- ◆ recent work on LISA: use kinematically induced dipole  
[Seto 2006]  
[Domcke et al 2019]

# n-G in Axion-Gauge Field Model

$$\text{n-G} \quad \langle h_R(\vec{k}_1) h_R(\vec{k}_2) h_R(\vec{k}_3) \rangle = (2\pi)^3 \delta^{(3)} \left( \sum_{i=1}^3 \vec{k}_i \right) B_h(k_1, k_2, k_3)$$



$\Psi = \text{GW}$   
 $t = \text{tensor SU}(2)$



$$\frac{B_h}{P_\zeta^2} \lesssim r^2 10^6$$

sourced nG tensors  
 much larger than in SFSR

$m_Q = 3.45$   
 $\epsilon_B \simeq 10^{-5}$   
 $H \simeq 10^{13} \text{ GeV}$   
 $r_{\text{vac}} \simeq 0.002$   
 $r_{\text{sourced}} \simeq 0.04$

# Primordial GW to test inflationary particle content

scale-dependence

...non-Gaussianity

*more later*

chirality



Axion-gauge field models

general approach: inflationary particle content

# Organizing Principles for extra particle content: **the mass**



(effective) mass range

$$m \gg H$$

fields integrated out, some remnants

{  
Achucarro et al 2012  
Burgess et al 2013  
MF et al 2013  
Silverstein 2017

$$m \lesssim H$$

immediate and detectable effects



# Organizing Principles for particle content: the spin



## consequences on the mass range

Particles as unitary irr. rep of spacetime isometry group, dS

[Wigner]

principal series

$$\frac{m^2}{H^2} \geq \left(s - \frac{1}{2}\right)^2$$

complementary

$$s(s - 1) < \frac{m^2}{H^2} < \left(s - \frac{1}{2}\right)^2$$

discrete series

$$\frac{m^2}{H^2} = s(s - 1) - t(t - 1)$$

$$s \geq t ; s, t, = 0, 1, 2, \dots$$

# Mass & Spin

spin-2 example can source tensors linearly!

$$m^2 = 0 \checkmark \quad m^2 \geq 2H^2$$

+

interactive spin-2 fields  $\implies$  at most 1 is massless

[Boulanger, Damour, Gualtieri, Hennaux (2000)]

# Extra spin-2 field is a massive graviton

know how to write it non-linearly

$$S_{\text{tot}} = S_{\phi} + \int d^4x \left[ \sqrt{-g} M_P^2 R[g] + \sqrt{-f} M_f^2 R[f] - m^2 M^2 \sqrt{-g} \beta_n \mathcal{E}_n(\sqrt{g^{-1} f}) \right]$$

[de Rham, Gabadadze, Tolley (2011)]

[Hassan, Rosen (2011)]

ghost-free

+

well-known use for late-time acceleration,  $m \sim H_0$

check the unitarity bound

&

use in inflationary context

# Unitarity bound

$$\tilde{m}^2 \left[ 1 + \left( \frac{H_f/M_f}{H/M_P} \right)^2 \right] \geq 2H^2$$

[MF, Tolley (2012&2013)]

somewhat weakened constraint but

$$m \sim H$$

extra spin-2 fields tend to decay quickly

*not the end of the story!*

[Biagetti, Dimastrogiovanni, MF (2017)]

[Dimastrogiovanni, MF, Tasinato (2018)]

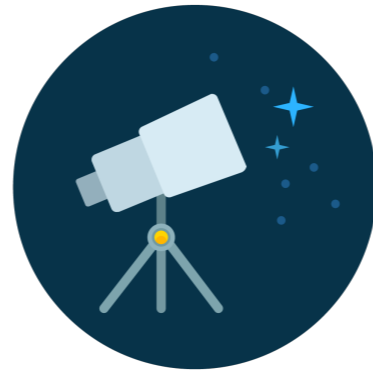
partially massless: [Goon, Hinterbichler, Joyce, Trodden (2018)]

but see also

[Lin, Sasaki (2015)]

[Fujita, Kuroyanagi, Mizuno, Mukohyama (2018)]

How can we probe info on Mass & Spin?



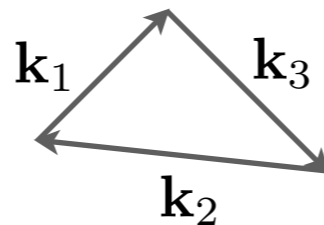
# non-Gaussianities

so far

$$\langle \zeta_{k_1} \zeta_{k_2} \rangle \equiv \frac{2\pi}{k^3} \mathcal{P}(k) \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2)$$

n>2-point functions probe interactions

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle \equiv (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B(k_1, k_2, k_3)$$



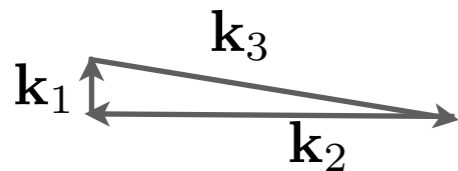
Amplitude

$$f_{\text{NL}} \sim B/P^2$$

# Squeezed Bispectrum: single-field inflation

$$\lim_{k_1 \rightarrow 0} \frac{1}{P_\zeta(k_1)} \langle \zeta_{\mathbf{k}_1} \zeta_{\mathbf{k}_2} \zeta_{\mathbf{k}_3} \rangle = -\mathbf{k}_2 \cdot \frac{\partial}{\partial \mathbf{k}_2} \langle \zeta_{\mathbf{k}_2} \zeta_{\mathbf{k}_3} \rangle$$

[Maldacena, 2003]



standard consistency relation  
for single-field inflation

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle \Big|_{k_1 \ll k_3} \propto \frac{1}{k_1^3 k_3^3} \sum_{n=0} b_n \left( \frac{k_1}{k_3} \right)^n \propto f_{\text{NL}}$$

physical information from n=2

qualitative threshold for LSS surveys  $f_{\text{NL}} \sim 1$

# Squeezed Bispectrum: new physics

extra particle content ==> non-analytical scaling ==> directly probe new physics

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle \Big|_{k_1 \ll k_3} \propto \underbrace{\frac{1}{k_1^3 k_3^3}}_{\text{standard}} \left( \frac{k_1}{k_3} \right)^{3/2 - \nu_s} P_s(\hat{k}_1 \cdot \hat{k}_3)$$

[Noumi et al 2012]

[Arkani-Hamed, Maldacena 2015]

[Kehagias, Riotto 2015]

non-analytical scaling

extra angular dependence

$$i\nu_s = \mu_s = \sqrt{\frac{m^2}{H^2} - \left(s - \frac{1}{2}\right)^2}$$

info on mass & spin!



# Squeezed Bispectrum: new physics

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle \Big|_{k_1 \ll k_3} \propto \underbrace{\frac{1}{k_1^3 k_3^3}}_{\text{standard}} e^{-\pi \mu_s} \left( \frac{k_1}{k_3} \right)^{3/2} P_s(\hat{\mathbf{k}}_1 \cdot \hat{\mathbf{k}}_3) \cos \left[ \mu_s \ln \left( \frac{k_1}{k_3} \right) \right]$$

direct mass suppression
non-analytical scaling
 $m \geq \frac{3}{2} H$

crucial fact for  $s \geq 2$  spinning fields

$$m \gtrsim H$$

# Tensor-scalar-scalar Bispectrum

$$\langle \gamma_{k_L} \zeta_{k_S} \zeta_{k_S} \rangle \Big|_{k_L \ll k_S} \propto \frac{1}{k_L^3 k_S^3} \left( \frac{k_L}{k_S} \right)^{3/2 - \nu_s} \mathcal{E}_2^\lambda(\hat{\mathbf{k}}_L \cdot \hat{\mathbf{k}}_S) P_s^\lambda(\hat{\mathbf{k}}_L \cdot \hat{\mathbf{k}}_S)$$

non-analytical scaling, CRs breaking

$$\nu_s = \sqrt{\left(s - \frac{1}{2}\right)^2 - \frac{m^2}{H^2}}$$

extra angular dependence

Connections with “tensor fossils”  
as diagnostic of new physics

$$P_\zeta(\mathbf{k}, \mathbf{x}_c) \Big|_{\gamma_L} = P_\zeta(k) \left( 1 + \mathcal{Q}_{\ell m}(\mathbf{x}_c, \mathbf{k}) \hat{k}_\ell \hat{k}_m \right)$$

[Dimastrogiovanni, MF, Jeong, Kamionkowski 2014]

[Dimastrogiovanni, MF, Kamionkowski 2016]

# Crucial for non-Gaussianity at small scales (e.g. LISA)

$$P_{\gamma}^{\text{tot}}(\mathbf{k}, \mathbf{x}_c) \Big|_{\gamma_L} = P_{\gamma}(k) \left( 1 + Q_{lm}(\mathbf{x}_c, \mathbf{k}) \hat{k}_l \hat{k}_m \right)$$

[Dimastrogiovanni, MF, Tasinato, PRL 2020]

$$Q_{lm}(\mathbf{x}_c, \mathbf{k}) \equiv \int \frac{d^3 q}{(2\pi)^3} e^{i\mathbf{q} \cdot \mathbf{x}_c} \sum_{\lambda} \left[ \frac{\tilde{B}^{\text{sq}}(\mathbf{k}, \mathbf{q})}{2 P_{\gamma}(k) P_{\gamma}^{\lambda}(q)} \right] \epsilon_{lm}^{\lambda}(-\hat{q}) \gamma_{-\mathbf{q}}^{*\lambda}$$

# Caveat: only squeezed non-G

- propagation effects typically de-correlate primordial non-Gaussianities

[Bartolo, De Luca, Franciolini, Lewis, Peloso, Riotto, 2019]

- an important exception is the ultra-squeezed regime (e.g. long mode horizon-size)

[Dimastrogiovanni, MF, Tasinato]

- ◆ application: correlate STT-sourced GW anisotropies with CMB anis. to test primordial origin

[Adshead, Afshordi, Dimastrogiovanni, MF, Lim, Tasinato]

$$\delta F_{NL}^{\text{sq}} \simeq \frac{2.8 \times 10^3}{\text{SNR}_{\text{SGWB}}}$$

# Recap

extra fields can be probed via squeezed bispectrum  
because they break consistency relations

&

spinning  $\Rightarrow$  richer set of signatures

but, typically

spinning  $\Rightarrow$  mass bounds  $\Rightarrow$  suppression

[Biagetti, Dimastrogiovanni, **MF** 2017]

# One crucial ingredient

the mass, the spin... **the coupling**

$\exists$  1 field that doesn't decay: the inflaton

**non-minimal** coupling to the inflaton!

## Effective Field Theory Approach

[Iacconi, **MF** et al, 2019]

*GW at interferometers*

[Dimastrogiovanni, **MF**, Tasinato, Wands 2018]

*large non-Gaussianity*

[Bordin, Creminelli, Khmelnitsky, Senatore 2018] *spinning fields*

# Examples

quasi-single-field

$$S_m = \int d^4x \sqrt{-g} \left[ -\frac{1}{2} (R + \sigma)^2 (\partial_\mu \theta)^2 - \frac{1}{2} (\partial_\mu \sigma)^2 - V_{\text{sr}}(\theta) - V(\sigma) \right]$$

[Chen, Wang 2009]+...



scalar sector

inflaton

extra

(gauge) vector field

$U(1), SU(2)$ ...

$$I(\phi) F^2 \quad \text{or} \quad I(\phi) F \tilde{F}$$

strongly affects tensor sector ==> chiral GW at LISA scales

# The EFT approach

## philosophy and cooking instructions

● unitarity bounds on spinning particles masses are dictated by dS isometries ●

● inflation needs to end  $\longleftrightarrow$  dS iso are broken by inflaton ●

[Cheung et al 2007]

● couple directly to the inflaton any otherwise massive field ●  
that you want to make effectively lighter

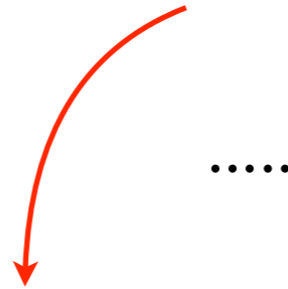
● non-linearly realized symmetries prescribe ●  
inflaton  $\longleftrightarrow$  extra field(s) coupling(s)



# The EFT approach

can be implemented for generic extra spin

it is an EFT of fluctuations around FLRW



$$S[\sigma] = \frac{1}{4} \int d^4x a^3 \left[ (\dot{\sigma}^{ij})^2 - c_2^2 (\partial_i \sigma^{jk})^2 / a^2 - \frac{3}{2} (c_0^2 - c_2^2) (\partial_i \sigma^{ij})^2 / a^2 - m^2 (\sigma^{ij})^2 \right]$$

spin-2

$$S_{\text{int}} = \int d^4x \sqrt{-g} \left[ -\frac{\rho}{2\epsilon H a^2} \partial_i \partial_j \pi_c \sigma^{ij} + \frac{1}{2} \rho \dot{\gamma}_{c\,ij} \sigma^{ij} \right. \\ \left. - \frac{\rho}{2\epsilon H^2 M_P a^2} (\partial_i \pi_c \partial_j \pi_c \dot{\sigma}^{ij} + 2H \partial_i \pi_c \partial_j \pi_c \sigma^{ij}) + \frac{\tilde{\rho}}{\epsilon H^2 M_P a^2} \dot{\pi}_c \partial_i \partial_j \pi_c \sigma^{ij} - \mu (\sigma^{ij})^3 \right]$$

[Bordin et al 2018]

# Power Spectrum

Extra spin-2 case

$$S_{\text{int}} = \int d^4x \sqrt{-g} \left[ -\frac{\rho}{2\epsilon H a^2} \partial_i \partial_j \pi_c \sigma^{ij} + \frac{1}{2} \rho \dot{\gamma}_{c\,ij} \sigma^{ij} \right. \\ \left. - \frac{\rho}{2\epsilon H^2 M_P a^2} (\partial_i \pi_c \partial_j \pi_c \dot{\sigma}^{ij} + 2H \partial_i \pi_c \partial_j \pi_c \sigma^{ij}) + \frac{\tilde{\rho}}{\epsilon H^2 M_P a^2} \dot{\pi}_c \partial_i \partial_j \pi_c \sigma^{ij} - \mu (\sigma^{ij})^3 \right]$$



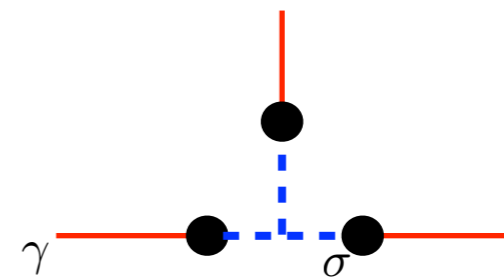
$$P_\gamma(k) = \frac{4H^2}{M_p^2 k^3} \left[ 1 + \frac{C_\gamma(\nu)}{c_\sigma^{2\nu}} \left( \frac{\rho}{H} \right)^2 \right]$$

[Bordin et al 2018]

- $\frac{\rho}{H} \ll 1$       perturbative treatment of quadratic mixing
- $\frac{\mu}{H} \ll 1$        $L_{-3} < L_{-2}$
- $\frac{\rho}{\sqrt{\epsilon}H} \ll 1$       small radiative corrections to sigma mass
- $c_\sigma \gtrsim 10^{-2}$       tensor nG limits as well



## Bispectrum



$$f_{\text{nl}}^{\text{eq}} \simeq \begin{cases} \frac{77782}{\sqrt{r}} r^2 \simeq 1143 & \text{for } c_\sigma = 0.1 \\ \frac{155563}{\sqrt{r}} r^2 \simeq 2286, & \text{for } c_\sigma = 0.05 \\ \frac{777817}{\sqrt{r}} r^2 \simeq 11431 & \text{for } c_\sigma = 0.01 \end{cases}$$

Small scales signatures?

*time-dependent* sound speeds  $\{c_0, c_1, c_2\}$ ,  $s_i = \frac{\dot{c}_i}{Hc_i}$

[Iacconi et al 2019]

Why? Integrating out heavy fields may result  
into  $c_s < 1$  for the remaining light field(s)

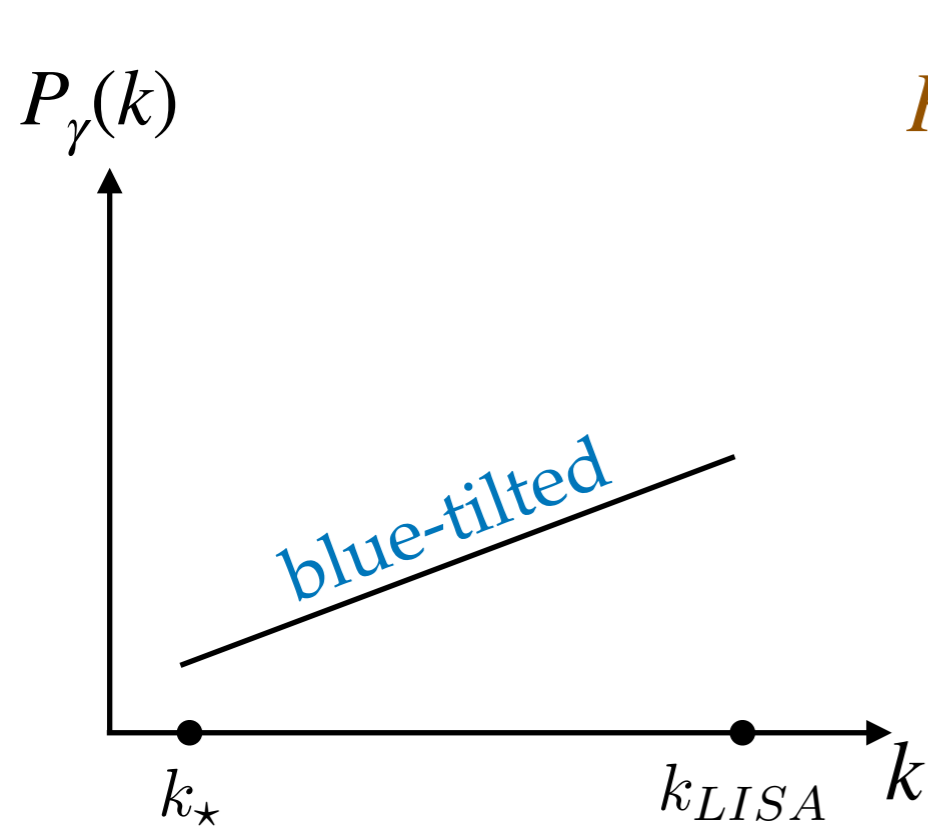
{1201.6342 - Achucarro et al., ...}

- $c_1^2 = \frac{1}{4}c_2^2 + \frac{3}{4}c_0^2$

- $s_0 = \frac{4}{3} \frac{c_1^2}{c_0^2} s_1 - \frac{1}{3} \frac{c_2^2}{c_0^2} s_2$

- perturbativity bound:  $c_2 > 10^{-4}$ , sets a bound on  $s_2 = \frac{\dot{c}_2}{Hc_2}$

Consequence: scale dependent  $P_\zeta$  &/or  $P_\gamma$



$$P_\gamma(k) \propto \frac{1}{c_2^{2\nu}} \left( \frac{k}{k_\star} \right)^{-2\nu s_2}$$

if  $s_2 < 0$  the sourced contribution is **blue-tilted**:

can this signal be detected ?

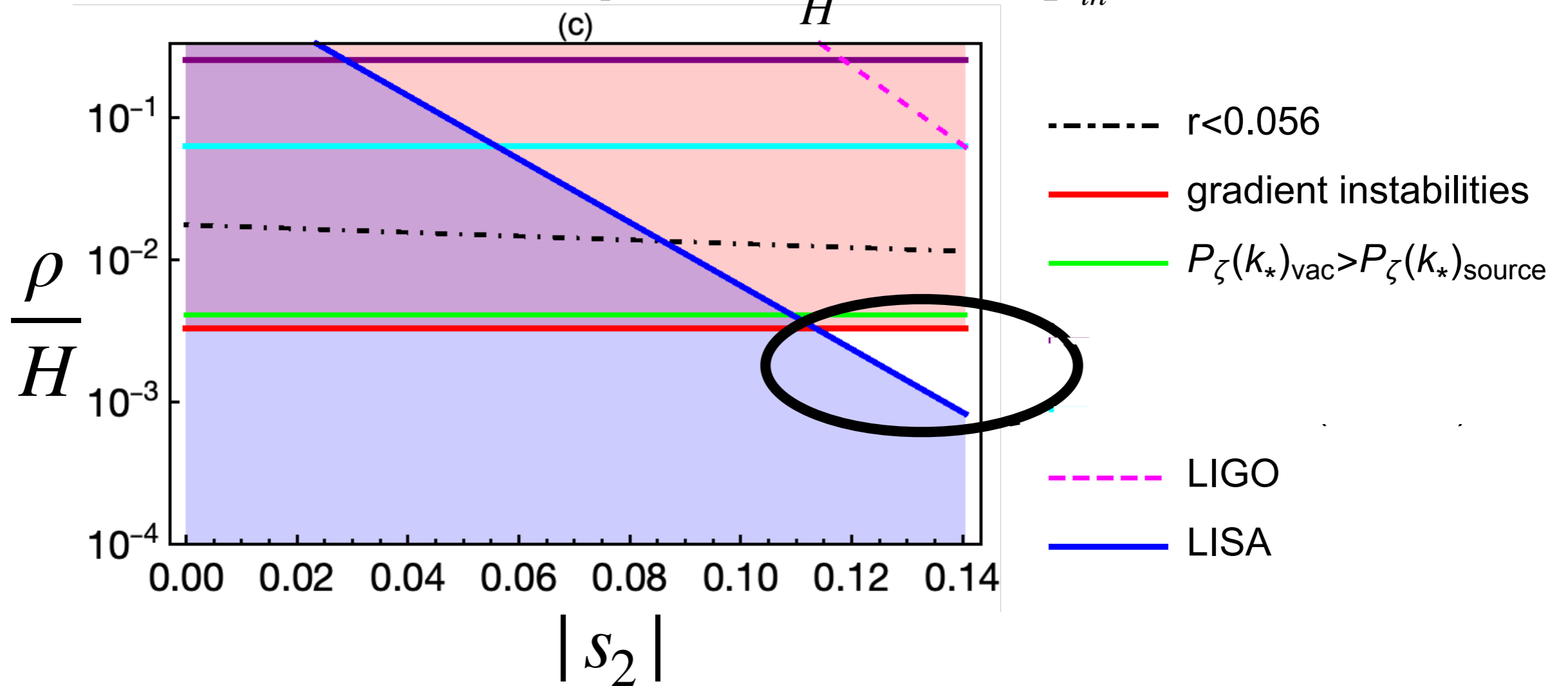
Example:  $\{s_2 < 0, s_1 = 0, s_0 > 0\}$

$$\left\{ \begin{array}{l} c_2(k) = c_2|_{in} \left( \frac{k}{a_0 H_0} \right)^{s_2} \\ c_0(k) = \sqrt{\frac{4}{3} c_1^2 - \frac{1}{3} c_2(k)^2} \end{array} \right.$$

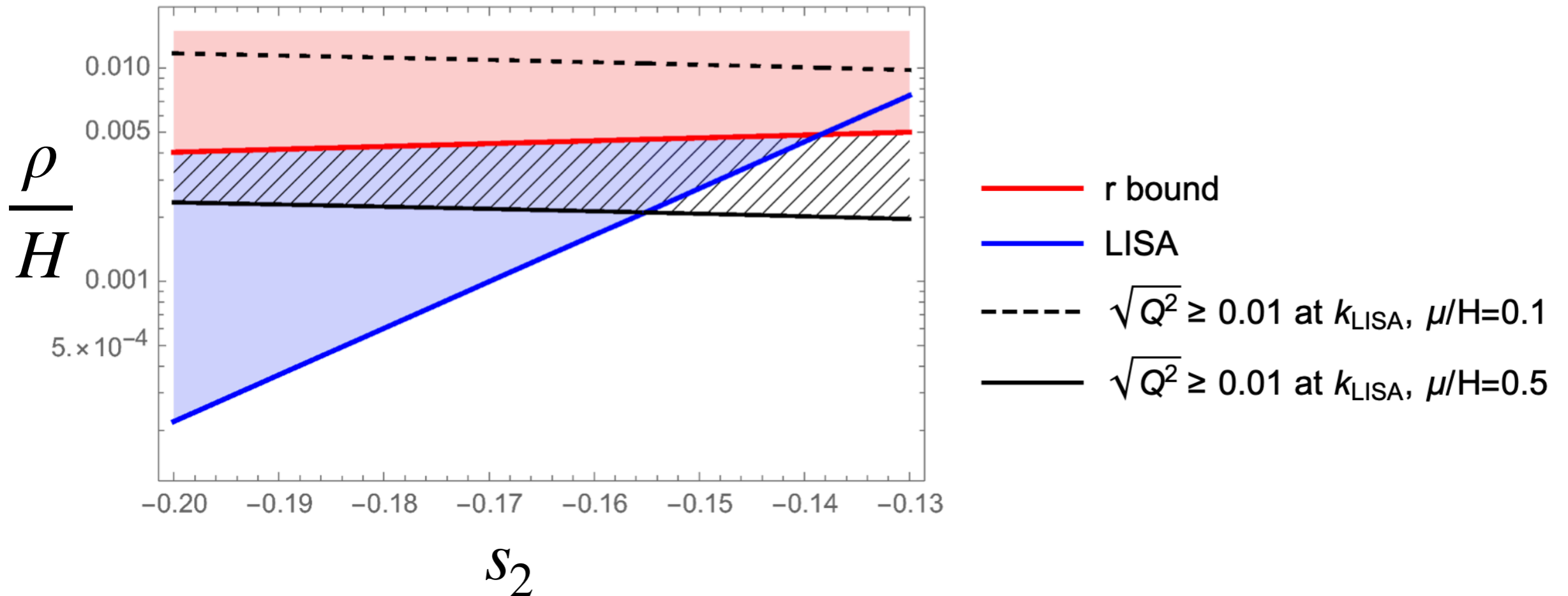
parameters:  $\{H, c_2|_{in}, c_1, \frac{m}{H}\}$

# Example of parameter space analysis

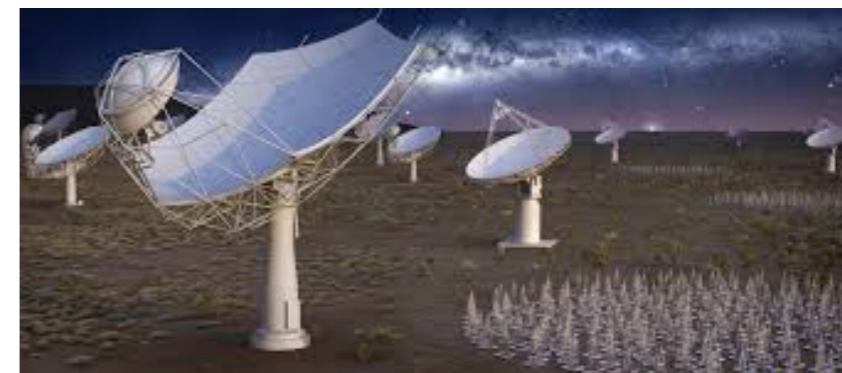
$$H = 10^{13} \text{ Gev} , c_1 = 0.85 , \frac{m}{H} = 0.54 , c_2|_{in} = 10^{-1}$$



$$Q_{lm} \text{ standard deviation: } \sqrt{\bar{Q}^2} = 16 \int_0^{k_{Lmax}} \frac{dk_L}{k_L} f_{NL}^2(k_L, k_S) \mathcal{P}_\gamma(k_L)$$



The same analysis can be performed also considering SKA





# Conclusions

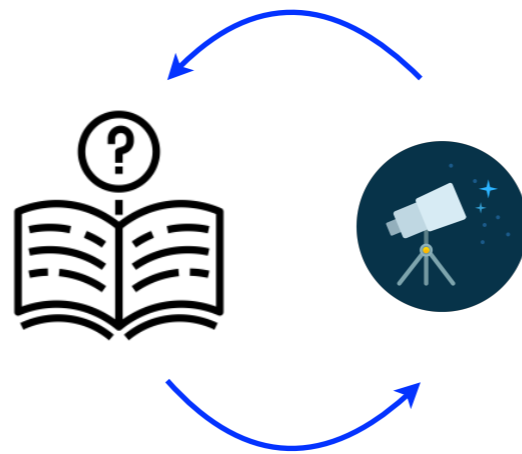


Cosmological probes will soon cross qualitative thresholds e.g. on  $r$ ,  $f_{\text{NL}}$



Lots we can learn on inflationary field content, strong connection with particle physics

Prepare theory to meet experiments

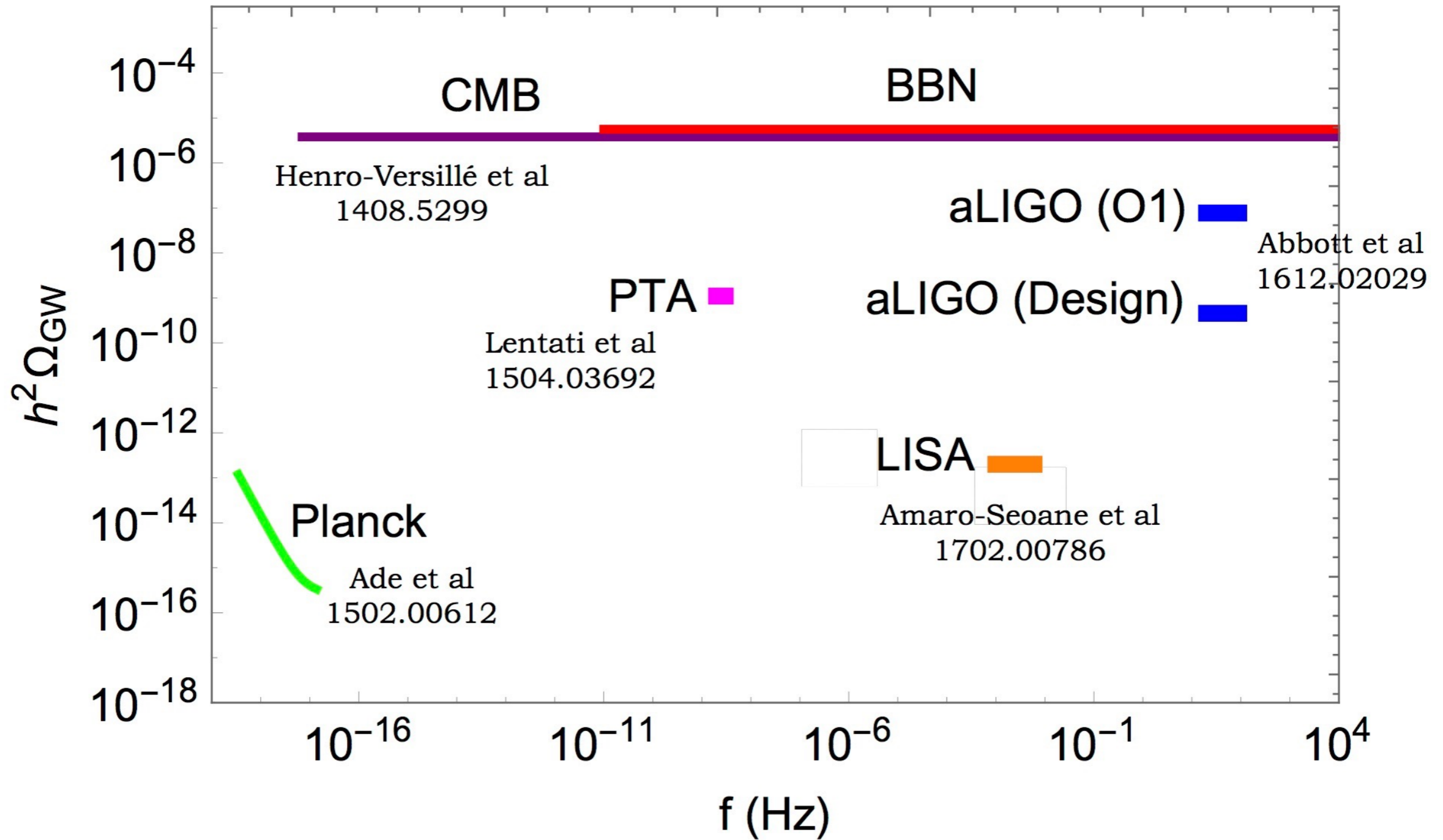


What is Compelling & Testable?

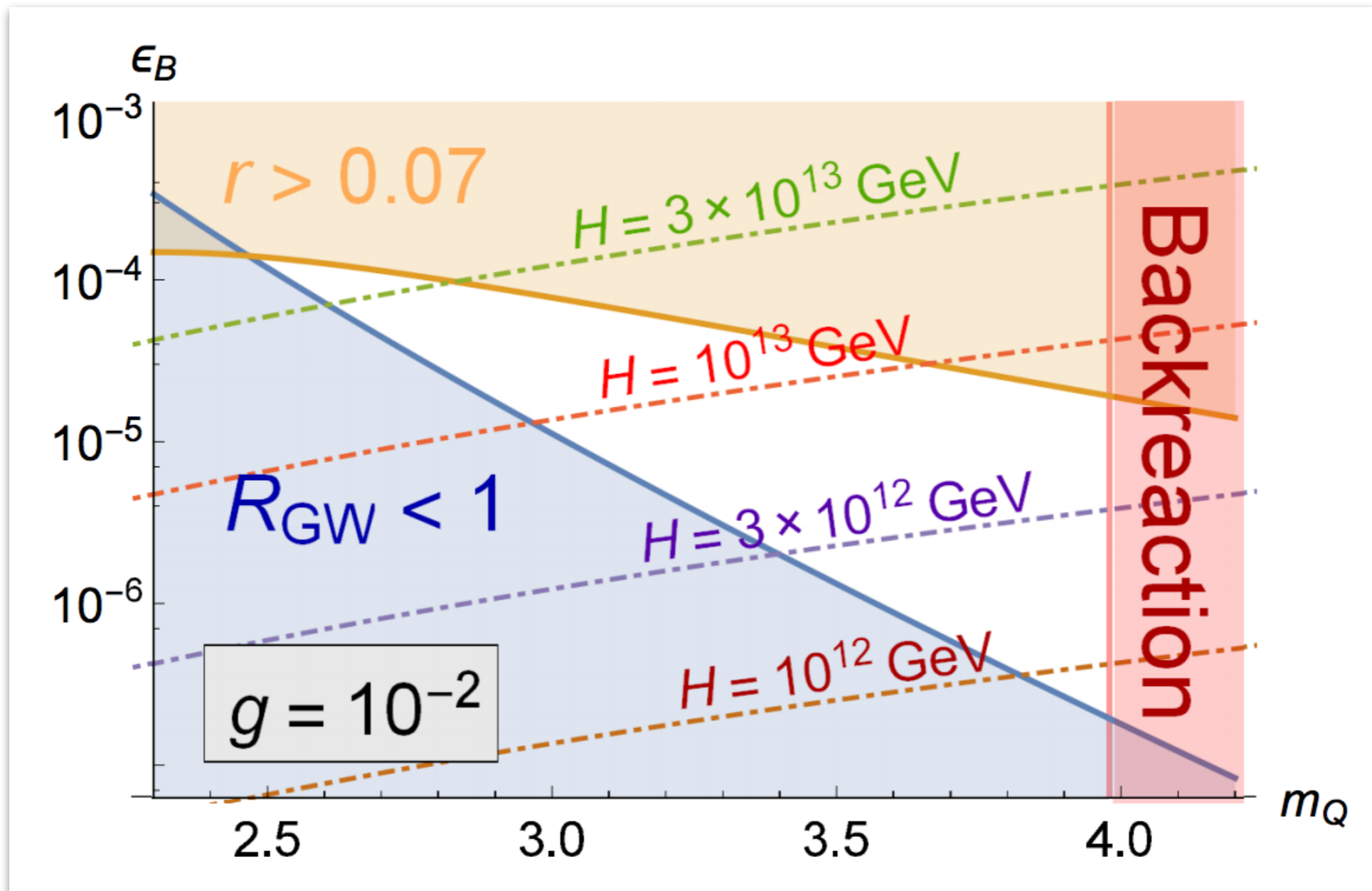
**Thank You!**

# Back-up Slides

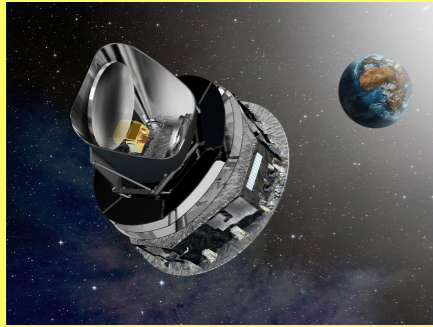
# Observational bounds/sensitivities for SGWB



# Backreaction Under Control



## Scalar bispectrum: current bounds



$$f_{\text{NL}}^{\text{local}} = -0.9 \pm 5.1 \quad f_{\text{NL}}^{\text{equil}} = -26 \pm 47 \quad f_{\text{NL}}^{\text{ortho}} = -38 \pm 24$$

[68 % CL]

## Scalar bispectrum: future bounds

- **LSST**
- **SKA**
- **SPHEREx**

$$\sigma(f_{\text{NL}}^{\text{local}}) \simeq 1$$

- **21-cm**  $\sigma(f_{\text{NL}}^{\text{local}}) \lesssim 10^{-1}$   
[Munoz, Ali-Haïmoud, Kamionkowski]

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## Tensor bispectrum

- **Planck**  
 $f_{\text{NL}}^{\text{tens}} = (8 \pm 11) \times 10^2$   
[68 % CL]

$$f_{\text{NL}}^{\text{tens}} \equiv \frac{B_{\gamma}^{+++}(k, k, k)}{(18/5)P_{\zeta}^2(k)}$$

(parity violating models / roughly equilateral)

- **LiteBIRD**  
 $\sigma(f_{\text{NL}}^{\text{tens}}) = \text{a few}$   
(possibly also with **PICO**)

# Tensor-Scalar-Scalar bispectrum

$$f_{\text{NL}}^{\gamma\zeta\zeta} \equiv \frac{B_{\gamma\zeta\zeta}}{P_{\zeta}^2}$$

$$f_{\text{NL}}^{\gamma\zeta\zeta} = -48 \pm 28 \quad [68\% \text{ CL}]$$

Local shape — temperature data [Shiraishi, Liguori, Fergusson]

$$f_{\text{NL}}^{\gamma\zeta\zeta} \longleftrightarrow \sqrt{r} f_{\text{NL}}$$

## Improvement expected from Planck to CMB-S4 (from BTT):

	CMB-S4	Relative improvement
Local ( $r = 0.01$ )	$\sigma(\sqrt{r} f_{\text{NL}}) = 0.7$	25.3
Equilateral ( $r = 0.01$ )	$\sigma(\sqrt{r} f_{\text{NL}}) = 14.7$	13.7

[CMB-S4 Science Book]