

Theory and Observational Constraints in Nonlocal Gravity

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Outline

Nonlocal Infrared Modifications of Gravity

Introduction & Motivations

Nonlocal Cosmology

Observational constraints and parameter inference

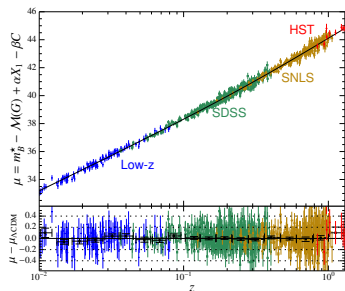
(Some) Small Scale Solutions

Future Perspectives

Multi-Messenger Cosmology

Introduction: Accelerated Expansion of the Late Universe

- ▷ Observation of Type Ia supernovae
- Late accelerated cosmic expansion
[Riess+; Perlmutter+ (1999)]



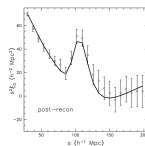
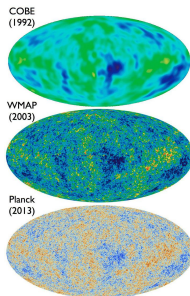
[SNIa Hubble diag., Betoule+ (2014)]

- Introduction of Λ for Λ CDM

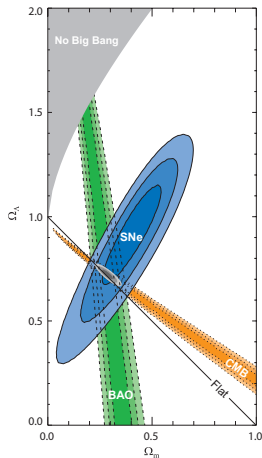
$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + g_{\mu\nu}\Lambda = 8\pi G T_{\mu\nu}$$

- $\theta_{\text{base}} = (\Omega_b, \Omega_\Lambda, H_0, n_s, A_s, z_{\text{re}})$

- ▷ CMB, BAO+ & complementarity
- Λ compatible w/ high precision obs.



[Anderson+ (2013)]



[Kowalski+ (2008)]

Introduction: What is the Dark Energy?

▷ Theoretical and (potential) observational objections

- **Cosmological Constant Problem**

→ No understanding of fundamental vacuum (\sim QG)

- **Coincidence problem**

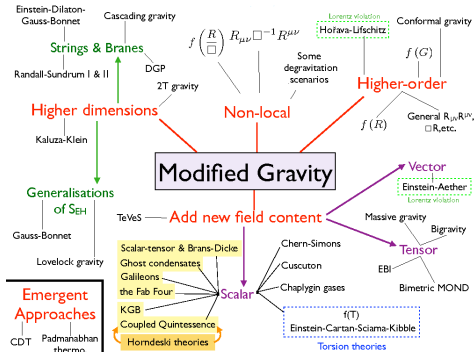
→ Violation of the Cosmological Principle

- **Statistical inconsistencies**

H_0 : CMB vs local measurements

σ_8 : cluster counts vs weak lensing

Ω_K : CMB [Di Valentino+ (2019)]



[Courtesy of Tessa Baker]

⇒ Search for modifications to GR

→ Design and test new alternative theories of gravity

→ Develop methodology for current/future experiments (e.g. LSS, GWs)

Introduction: Nonlocal Gravity Models

- Definition: Nonlocal field theories are those that are not local:
Dynamics at x^μ not only depends on the values of $\{\phi_i\}$ and on $\{\partial_{\mu_1} \dots \partial_{\mu_N} \phi_i\}$ with $N < \infty$ at x^μ .
- Examples: \square^{-1} , ∂^∞ , $\exp(M/\square)$, $\log(\square/M)$, $e^2(\square)$, $f_R(\square)$, ...
→ where e.g. $(\square^{-1}\phi)(x) \equiv \int d^4y \sqrt{-g} G(x,y)\phi(y)$
- From various contexts:
 - ▶ Effective QFT (vacuum pol. of light fields, conformal anomaly)
 - ▶ Extra-dimensions (DGP)
 - ▶ String theories (relevant in the UV)
 - ▶ Infrared resummation on de Sitter
 - ▶ Quantum Gravity considerations
 - ▶ etc.
→ Hard to handle and to understand from first principles
- Dark energy phenomenology: $f(R/\square)$, $m^2 R \square^{-2} R$, $R_{\mu\nu} \square^{-1} R^{\mu\nu}$, more.
→ no EFT-like techniques such as power-counting

Introduction: Nonlocal Gravity Models

- Specific models:

$$G_{\mu\nu} - m^2 (g_{\mu\nu} \square^{-1} R)^T = 8\pi G T_{\mu\nu}$$

[Maggiore (2014)]

$$S_{\text{RR}} = M^2 \int d^4x \sqrt{-g} \left[R - \frac{1}{2} m^2 R \frac{1}{\square^2} R \right]$$

[Maggiore, Mancarella (2014)]

$$S_{\text{DW}} = M^2 \int d^4x \sqrt{-g} R [1 + f(R/\square)]$$

[Deser, Woodard (2007)]

Introduction: Nonlocal Gravity Models

- Degravitiation idea [Arkani-Hamed+ (2002), Barvinsky (2003), Dvali (2006)]

$$\mathcal{L}_{\text{proca}} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{m^2}{2}A_\mu A^\mu - A_\mu \tilde{j}^\mu \Leftrightarrow \mathcal{L}_{\text{nl}} = -\frac{1}{4}F_{\mu\nu} \left(1 - \frac{m^2}{\square}\right) F^{\mu\nu} - A_\mu \tilde{j}^\mu$$

where $(\square^{-1}\phi)(x) = \int d^4y G(x,y)\phi(y)$ and $\partial_\mu \tilde{j}^\mu \equiv 0$

- Application to Fierz-Pauli massive gravity

$$\mathcal{L}_{\text{nl}} = \frac{1}{2}h_{\mu\nu} \left(1 - \frac{m^2}{\square}\right) \mathcal{E}^{\mu\nu\rho\sigma} h_{\rho\sigma} - 2m^2 \chi \frac{1}{\square} \partial_\mu \partial_\nu (h^{\mu\nu} - \eta^{\mu\nu} h)$$

→ Obstruction: covariantization $\Rightarrow g^{\mu\nu} R_{\mu\nu} = 0$ "Covariant vDVZ discontinuity"

$$\left[\left(1 - \frac{m^2}{\square_g}\right) G_{\mu\nu} \right]^T = 8\pi G T_{\mu\nu} \quad [\text{Porrati (2002), Jaccard+ (2013)}]$$

▷ Unviable background cosmology

▷ $\square^{-1}R_{\mu\nu} \subset \square^{-1}G_{\mu\nu} \Rightarrow$ instabilities [Ferreira+ (2013), Amendola+ (2017)]

▷ $g_{\mu\nu}\square^{-1}R \subset \square^{-1}G_{\mu\nu}$ stable [Foffa+ (2013)]

Model RT :

$$G_{\mu\nu} - m^2 (g_{\mu\nu} \square_{ret}^{-1} R)^T = 8\pi G T_{\mu\nu}$$

$$\mathcal{L}_{lin} = \frac{1}{2} h_{\mu\nu} \mathcal{E}^{\mu\nu\alpha\beta} h_{\alpha\beta} - \frac{1}{2} m^2 h_{\mu\nu} P^{\mu\nu} P^{\alpha\beta} h_{\alpha\beta}$$

↓ Covariantization

Propagator ↓

$$S_{RR} = M^2 \int d^4x \sqrt{-g} \left[R - \frac{1}{2} m^2 R \frac{1}{\square^2} R \right]$$

$$\tilde{D}_{GR}(k) + \frac{-i}{k^2} + \frac{-i}{-k^2 + m^2}$$

↓ Localisation

→ No vDVZ discontinuity
→ Scalars are not genuine DoF

$$S_{RR}^{loc} = \int d^4x \sqrt{-g} \left[MR\Phi + \frac{1}{2m^2} (\square\Phi)^2 \right]$$

↓ Einstein Frame

$$S_{RR}^{loc} = \int d^4x \sqrt{-\bar{g}} \left[M^2 \bar{R} - \frac{1}{2} \bar{\nabla}_\mu \phi \bar{\nabla}^\mu \phi + \frac{1}{2} \bar{\nabla}_\mu \psi \bar{\nabla}^\mu \psi - \frac{m^2}{2} e^{-(\phi+\psi)/\tilde{M}} \psi^2 \right]$$

[YD, Mitsou (2014)]

↓ Jordan Frame + Var. Principle
+ Solving for scalars w/ vanishing IC

Model RR :

$$G_{\mu\nu} - m^2 K_{\mu\nu} [\square_{ret}^{-1} R, \square_{ret}^{-2} R] = 8\pi G T_{\mu\nu}$$

Application to Cosmology

Model RT

$$G_{\mu\nu} - m^2(g_{\mu\nu}\square_{ret}^{-1}R)^T = 8\pi G T_{\mu\nu}$$

Model RR

$$G_{\mu\nu} - m^2K_{\mu\nu}(\square_{ret}^{-1}R, \square_{ret}^{-2}R) = 8\pi G T_{\mu\nu}$$

- Resolution method: Localisation

$$\square V = R \quad \Rightarrow \quad V = \square_{ret}^{-1}R + V^{(hom)} = \int^t d^4x' \sqrt{-g} G(x, x') R(x') + V^{(hom)}$$

- ▷ Auxiliary fields with *vanishing initial conditions*
⇒ Not in the spectrum (at least linearly)

$$G_{\mu\nu} + m^2 \left[U g_{\mu\nu} - \frac{1}{2} (\nabla_\mu S_\nu + \nabla_\nu S_\mu) \right] = 8\pi G T_{\mu\nu}$$

$$\square_g U = -R, \quad \partial_\mu U = \frac{1}{2} \nabla_\nu (\nabla_\mu S^\nu + \nabla^\nu S_\mu)$$

$$G_{\mu\nu} - m^2 K_{\mu\nu}(V, S) = 8\pi G T_{\mu\nu}$$

$$\square_g V = R, \quad \square_g S = V$$

- Specialisation to flat FRW

$$ds^2 = -dt^2 + a^2(t) \delta_{ij} dx^i dx^j$$

Background Evolution

- On flat FLRW: $ds^2 = -dt^2 + a^2(t) d\vec{x}^2$
- Modified Friedmann equations :

$$H^2(t) = 8\pi G \sum_i \bar{\rho}_i(t) + m^2 Y(\{\bar{V}_k\}, H(t))$$
 + auxiliary EoM for $\{\bar{V}_k\}$

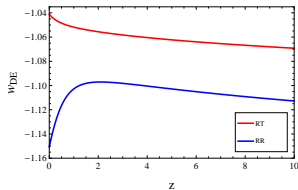
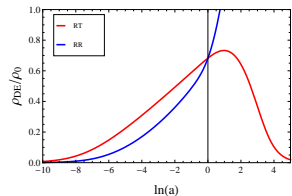
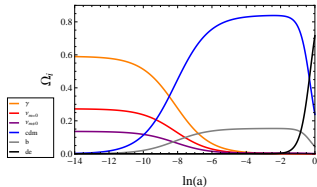
- $m^2 Y \equiv \bar{\rho}_{\text{DE}}(t)$: Dynamical dark energy
- $\square^{-1} R|_{\text{RD}} \simeq 0$: Late-time effectiveness
- Flatness today: $m_{\text{RT}} \simeq 0.67 H_0$, $m_{\text{RR}} \simeq 0.28 H_0$

- From $\dot{\bar{\rho}}_{\text{DE}} = -3H(1 + w_{\text{DE}})\bar{\rho}_{\text{DE}}$
 → On the phantom side: $w_{\text{DE}} < -1$

Fit : $w(t) = w_0 + (1 - a(t)) w_a$

RT: $w_0 \simeq -1.04$, $w_a \simeq -0.02$

RR: $w_0 \simeq -1.15$, $w_a \simeq 0.08$



Background Evolution

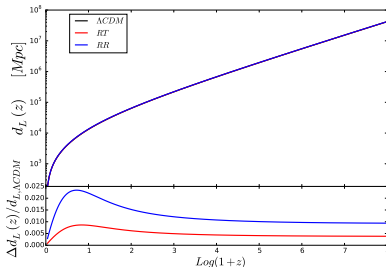
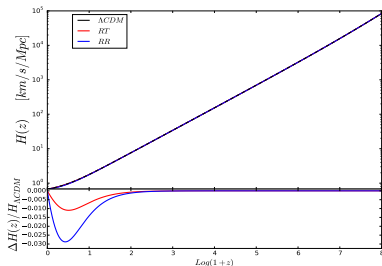
- From dark energy conservation:

$$\Omega_{de}(z) = \Omega_{de,0} \exp\left(3 \int_0^z dz' \frac{1 + w_{de}(z')}{(1+z')}\right)$$

writing $w_{de}(z \approx 0) \simeq -1 + \delta w_0$, $\Rightarrow \Omega_{de}(z \approx 0) \simeq \Omega_{de,0} (1 + 3z \delta w_0)$

\rightarrow Phantom dark energy: $\Omega_{de}(z \geq 0) < \Omega_\Lambda$

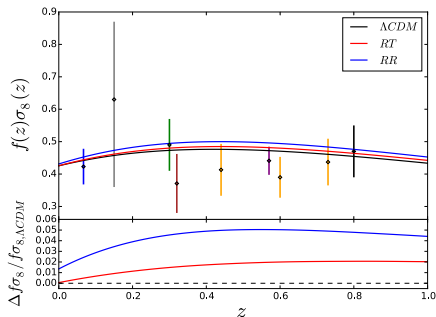
$$H(z) = [\Omega_M(z) h^2 + \Omega_{de}(z) h^2]^{1/2} \times 100 \text{ km/s/Mpc}$$



Linear Structure Formation and Gravitational Waves

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(t)[(1 + 2\Phi)\delta_{ij} + h_{ij}]dx^i dx^j$$

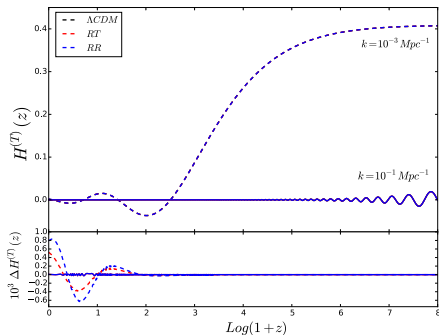
● Growth of structures RSD



▷ Forecasts for GC, WL+: *Euclid-like*
[Casas, YD, Kunz, Maggiore, Pettorino
(in prep.)]

▷ The lower $w_{\text{DE}}(z=0)$ the stronger $f\sigma_8$

● GWs: $h''_A + 2\mathcal{H}[1 - \delta(\eta)]\tilde{h}'_A + k^2\tilde{h}_A = 0$



▷ Modified GWs amplitude

[YD, Foffa, Khosravi, Kunz, Maggiore (2014)]
[YD, Foffa, Kunz, Maggiore, Pettorino (2016)]

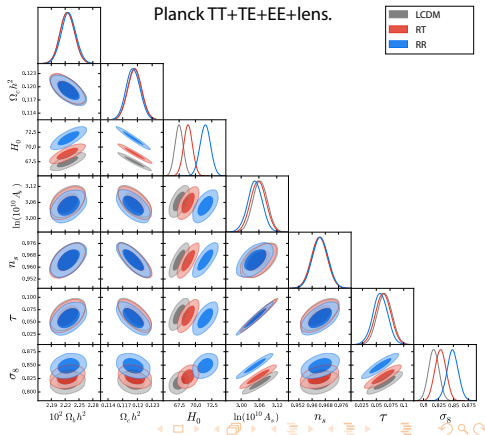
Boltzmann Code and Parameter Inference

- Implementation in CLASS (https://github.com/dirian/class_public/tree/nonlocal)
→ Code tested against a modified version of CAMB [Bellini+ (2018)]
- Observational constraints with MONTEPYTHON [Lesgourgues, Tram, Audren+ (2011)]
- Cosmological scenario: *Planck* baseline $\{\Omega_b, \Omega_c, H_0, A_s, n_s, z_{\text{reio}}\}$ and one massive ν

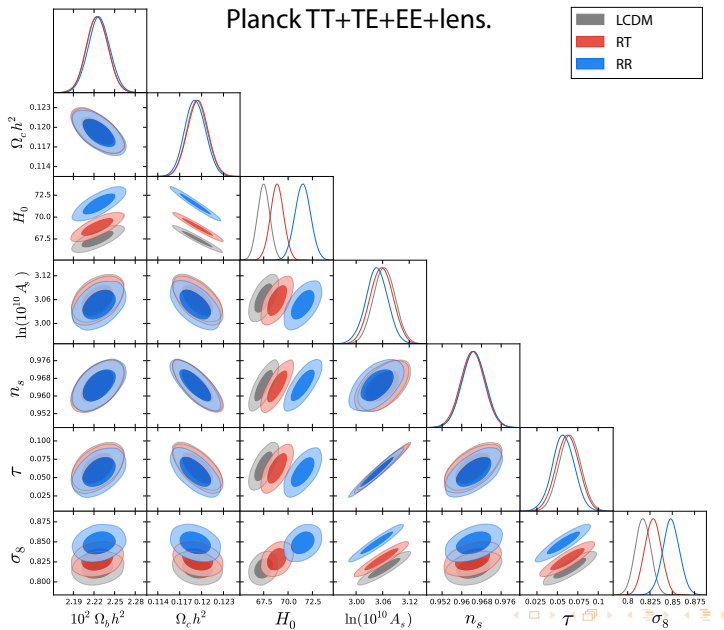
● Datasets:

- ▷ CMB: *Planck* 2015
- ▷ SNIa: *SDSS-II/SNLS3 JLA* 2014
- ▷ BAO: *BOSS, 6dF* and *SDSS MGS*
- ▷ H_0 : *HST* ($70.6 \pm 3.3, 73.8 \pm 2.4$)
- ▷ RSD: $f\sigma_8$

[YD, Foffa, Kunz, Maggiore, Pettorino (2016)]

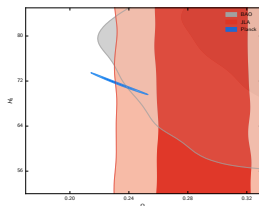
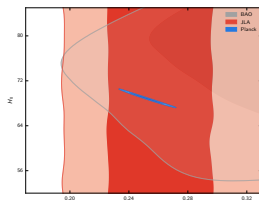


Observational Constraints



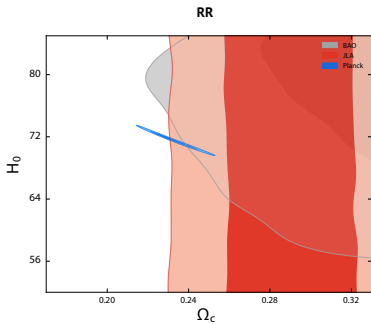
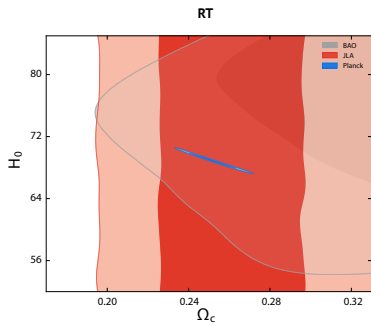
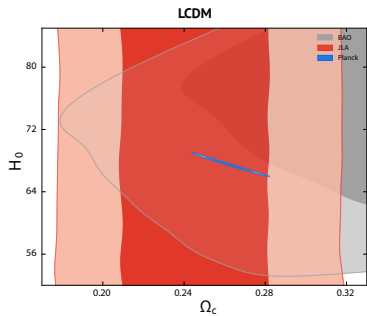
Observational Constraints

Param	Planck			BAO+Planck+JLA		
	Λ CDM	RT	RR	Λ CDM	RT	RR
ω_c	$0.1194^{+0.0015}_{-0.0014}$	$0.1195^{+0.0015}_{-0.0014}$	$0.1191^{+0.0015}_{-0.0014}$	$0.119^{+0.001}_{-0.001}$	$0.1197^{+0.001}_{-0.001}$	$0.121^{+0.001}_{-0.001}$
H_0	$67.5^{+0.65}_{-0.66}$	$68.86^{+0.69}_{-0.7}$	$71.51^{+0.81}_{-0.84}$	$67.67^{+0.47}_{-0.5}$	$68.76^{+0.51}_{-0.46}$	$70.44^{+0.56}_{-0.56}$
$\Delta\chi^2_{\min}$	1.6	1.5	0	0	0.6	6.0



- Few parameters with $\gtrsim 1\sigma$ deviation from Λ CDM
 - Bigger H_0 in nonlocal models
- Nonlocal vs Λ CDM:
 - RT statistically equivalent to Λ CDM
 - RR disfavored with respect to Λ CDM
- ⇒ Bayesian model comparison (SDDR) gives same conclusions
- BAO+Planck+JLA: RR creates a *Planck-JLA* tension

[YD, Foffa, Kunz, Maggiore, Pettorino (2016)]



$$\Delta\omega_c = \Delta(\Omega_c h^2) \sim 1\%$$

Extending the Baseline

[YD (2017)]

$$H(z) \simeq [\Omega_M(z) h^2 + \Omega_{\text{de}}(z) h^2]^{1/2}$$

- Phantom DE: $\Omega_{\text{de}}(z) < \Omega_\Lambda$
- CMB constrains $\omega_M \equiv \Omega_M h^2 \sim 1\%$

$$\theta_* = \frac{r_s(z_*)}{D_A(z_*)} < 0.1\%$$

- Distant SNIa constrain Ω_M :

$$D_L(z, \Omega_M) \equiv (1+z) \int_0^z \frac{dz'}{H(z', \Omega_M)}$$

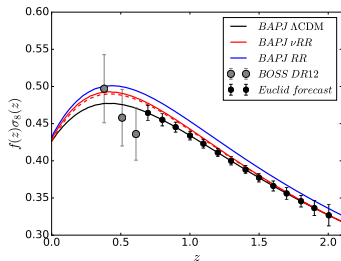
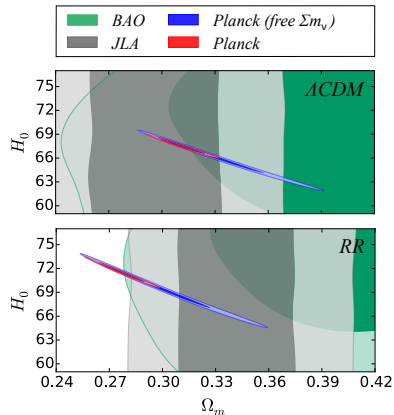
\Rightarrow *Planck* prefers higher H_0 and fixes ω_M
while SNIa prefer higher Ω_M

\rightarrow Solution: Extend the initial baseline

\Rightarrow ν RR statistical equivalent to $\nu\Lambda$ CDM

\Rightarrow RR prefers massive neutrino at 2σ

\rightarrow Future galaxy surveys could be decisive



Solving the tension

[YD (2017)]

- Compute the Bayes factor

$$\begin{aligned} B_{\nu\Lambda, \nu RR} &\equiv \frac{P(d|\mathcal{M}_{\nu\Lambda})}{P(d|\mathcal{M}_{\nu RR})} = \frac{P(d|\mathcal{M}_{\nu\Lambda})}{P(d|\mathcal{M}_{\Lambda})} \frac{P(d|\mathcal{M}_{\Lambda})}{P(d|\mathcal{M}_{RR})} \frac{P(d|\mathcal{M}_{RR})}{P(d|\mathcal{M}_{\nu RR})} \\ &= \frac{B_{RR, \nu RR}}{B_{\Lambda, \nu\Lambda}} B_{\Lambda, RR}, \end{aligned}$$

- The tension gets resolved

$$\text{BIC} : \Delta\chi^2|_{\Lambda, RR} = 6.0 \quad \rightarrow \quad \Delta\chi^2|_{\nu\Lambda, \nu RR} = 3.4 \quad (\text{weak})$$

$$\text{Bayes} : B_{\Lambda, RR} = 22.7 \quad \rightarrow \quad B_{\nu\Lambda, \nu RR} = 1.8 \quad (\text{insignificant})$$

→ νRR model statistical equivalent to $\nu\Lambda\text{CDM}$

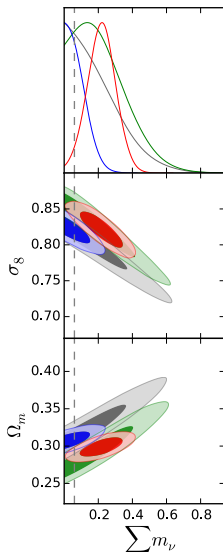
→ BIC “fails” in that case

- Bayesian paradigm incorporates Occam's razor

→ ΛCDM is penalized by its significant preference for small neutrino masses

→ RR prefers massive neutrino at 2σ

→ Future galaxy surveys could be decisive



Future Perspectives

Galaxy survey Fisher forecast in RT

[Casas, YD, Kunz, Maggiore, Pettorino (in prep.)]

- Compute sensitivity to cosmo. param.: Fisher information matrix

$$F_{ij}^{\text{GC}} = \int d^3k \frac{\partial \ln P_{\text{obs}}(z, k_{\text{ref}}, \mu_{\text{ref}})}{\partial \theta_i} \frac{\partial \ln P_{\text{obs}}(z, k_{\text{ref}}, \mu_{\text{ref}})}{\partial \theta_j} \times [\text{noise}] \times V_s$$

where $P_{\text{obs}} \equiv F[P_{\text{theo}}, D_A, H, \sigma_8, P_s, \dots]$

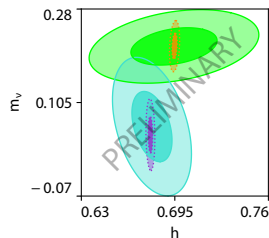
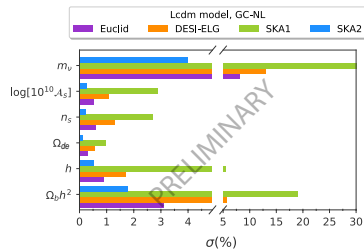
- Fisher code S4 galaxy surveys:
 - GCsp, GCph (Lin, NL), WL, 3x2pt, IM
- Projected Bayesian model comparison

$$B_{\Lambda \text{RT}} = \frac{\sigma_{\Omega_\Lambda}}{\sigma_{\Omega_{X_{\text{RT}}}}} \exp \left[-\frac{1}{2} \left(\frac{\bar{\Omega}_{X_{\text{RT}}}^2}{\sigma_{\Omega_{X_{\text{RT}}}^2}^2} - \frac{\bar{\Omega}_\Lambda^2}{\sigma_{\Omega_\Lambda}^2} \right) \right]$$

→ Prospects for testing Λ CDM vs MG

→ Test method's model independence

⇒ Combine with current and future exp.



Cosmology of the Deser-Woodard model

- The Deser-Woodard model:

$$S_{\text{DW}} = \frac{1}{16\pi G} \int d^4x \sqrt{-g} R \left[1 + f \left(\frac{1}{\square} R \right) \right]$$

→ Function f fixed to reproduce Λ CDM background [Deffayet, Woodard (2009)]

$$h_\Lambda^2(\zeta) \equiv \mathcal{H}_\Lambda^2(\zeta) / H_0^2 = [\Omega_\Lambda + \Omega(\zeta)]$$

$$f(\zeta) = -2 \int_\zeta^\infty d\zeta_1 \zeta_1 \phi(\zeta_1) - 6\Omega_\Lambda \int_\zeta^\infty d\zeta_1 \frac{\zeta_1^2}{h_\Lambda(\zeta_1) I(\zeta_1)} \int_{\zeta_1}^\infty d\zeta_2 \frac{I(\zeta_2)}{h_\Lambda(\zeta_2) \zeta_2^4} + \dots$$

$$X(\zeta) = - \int_\zeta^\infty \frac{d\zeta_1 \zeta_1^2}{h_\Lambda(\zeta_1) I(\zeta_1)}$$

→ Integro-differential system

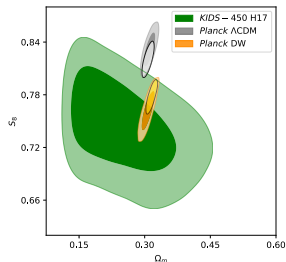
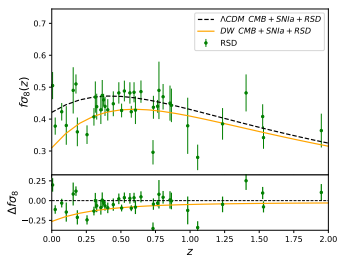
Cosmology of the Deser-Woodard model

[Amendola, YD, Nersisyan, Park (2019)]

- The Deser-Woodard model:

$$S_{\text{DW}} = \frac{1}{16\pi G} \int d^4x \sqrt{-g} R \left[1 + f \left(\frac{1}{\square} R \right) \right]$$

- Phenomenology and observational constraints



→ Lower growth than Λ CDM: Lower σ_8

⇒ Describes cosmological observations as well as Λ CDM

→ Lack of screening mechanism [Belgacem+ (2019)]

(Some) Small Scale Solutions

RR and DW ruled out, RT viable

- Correction to GR of $\mathcal{O}(m^2 r^2)$ on Schwarzschild-like in $r_s \ll r \ll m^{-1}$ [Maggiore+ (2014)]
- No vDVZ discontinuity:

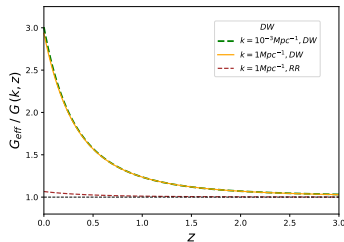
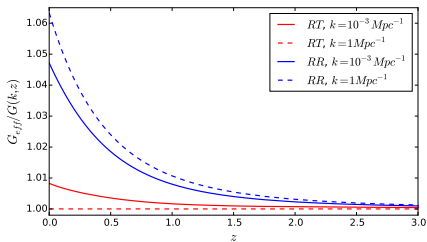
$$\tilde{D}_{\text{GR}}(k) + \frac{-i}{k^2} + \frac{-i}{-k^2 + m^2}$$

\implies No Vainshtein screening (?)

- $G_{\text{eff},N}$ in quasi-static linearised FLRW: $\vec{k}|/H(z) \sim |\square|/R \gg 1$ and $\nabla \cdot \vec{\phi} \ll \phi$
 \rightarrow RR (and DW) claimed to be ruled out by Lunar Laser Ranging \dot{G}/G [Belgacem+ (2019)]
- RT model passes all submitted tests ($R/|\square| \ll 1$) [Belgacem+ (2020)]

\implies Considered by *LSST* and *LISA* collaborations

$$G_{\text{eff},N}/G(z, |\vec{k}|) = \bar{F}(z)(1 + \mathcal{O}(1/|\vec{k}^2|))$$



Future Perspectives

Small Scale Dynamics in RT and Screening

- Corrections $\mathcal{O}(m^2 r^2)$ on Schwarzschild-like
- No vDVZ discontinuity:

$$\tilde{D}_{\text{GR}}(k) + \frac{-i}{k^2} + \frac{-i}{-k^2 + m^2}$$

- $G_{\text{eff},N}$ in quasi-static linearised FLRW:

$$|\vec{k}|/H(z) \sim |\square|/R \gg 1 \text{ and } \square$$

\Rightarrow Understand screening

- Caveat: in these tests

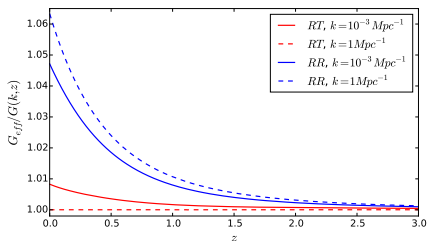
$$R/|\square| \ll 1 \text{ and } \square \rightarrow \nabla_i^2: \text{ non-dynamical}$$

\Rightarrow Test RT in dynamical small scale regimes
($R/|\square| \sim 1$)

\Rightarrow Compact objects tests: Collapsing star, BH perturbation theory,
PN formalism, superradiance ?, etc.

\Rightarrow Theoretical tests: well-posedness, nonlinear Hamiltonian analysis, ...

$$G_{\text{eff},N}/G(z, |\vec{k}|) = \bar{F}(z)(1 + \mathcal{O}(1/|\vec{k}^2|))$$



Multi-Messenger Astronomy

New observational window for cosmology

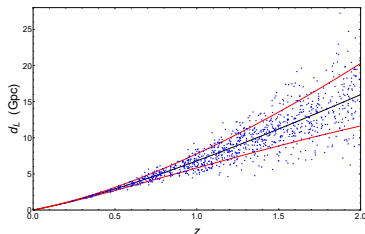
- GWs from ~ 100 mergers by *LIGO/Virgo/KAGRA*
- GWs from 1 inspiralling BNS: GW170817
 - γ -ray burst counterpart: GRB170817A by *FERMI* and *INTEGRAL*
 - ▶ $\tilde{h}''_{+,x} + 2\mathcal{H}\tilde{h}'_{+,x} + c_T^2(\eta)k^2\tilde{h}_{+,x} = 0, \implies |c_T(\eta_0) - c|/c \approx 10^{-15}$
 - Dramatic consequences for modified gravity theories

[Creminelli+, Sakstein+, Ezquiaga+, Baker+ (2017)]

- BNS are “standard sirens” [Schutz (1986)]

- ▶ GW amplitude $\sim d_L^{-1}$
- ▶ Electromagnetic counterparts give z
 - $d_L(z) \Rightarrow$ Hubble diagram for GWs

\implies Cosmological constraints



[GW Hubble diag., Belgacem+ (2018)]

Cosmological Constraints from GW Standard Sirens

[Belgacem, YD, Foffa, Maggiore (2017,2018)]

- Modified propagation for GWs: $\tilde{h}''_A + 2\mathcal{H}[1 - \delta(\eta)]\tilde{h}'_A + k^2\tilde{h}_A = 0$

$$\Rightarrow \tilde{h}_A \sim \frac{1}{d_L^{\text{GW}}(z)}$$

$$\text{with } d_L^{\text{GW}}(z) = d_L^{\text{em}}(z) \exp\left(-\int_0^z \frac{dz'}{1+z'} \delta(z')\right)$$

- Useful parametrisation:

$$\frac{d_L^{\text{GW}}(z)}{d_L^{\text{em}}(z)} = \Xi_0 + \frac{1}{(1+z)^n} (1 - \Xi_0)$$

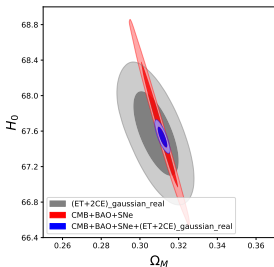
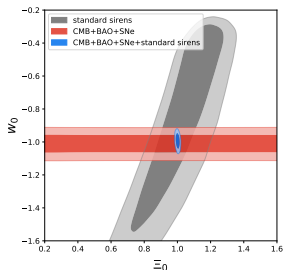
- Forecasts for next generation interferometers:

- ▷ *ET+CE* [Belgacem, YD, Foffa, Howell, Maggiore, Regimbau (2019)]
- ▷ *LISA* [LISA CosWG, Belgacem+ (2019)]

→ Improved prospects to test GR: $\Delta\Xi_0 = \Delta w_0/6$

→ New (multi-messenger) cosmic complementarity

→ $\#_{\text{GW}} / \#_{\text{GW-GRB}} = \mathcal{O}(10^2 - 10^4)$!



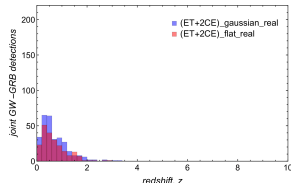
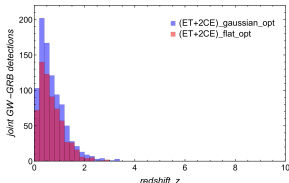
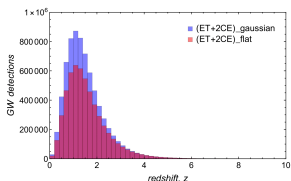
Number of BNS and BNS+GRB events

[Belgacem, YD, Foffa, Howell, Maggiore, Regimbau (2019)]

- For 10 years, for 2G+Fermi, (ET and ET+CE+CE) + full (1/3) THESEUS

Network	GW events	Joint GW-GRB events
HLVKI	814	15
ET	688,426	511 (169)
ET+CE+CE	7,077,131	907 (299)

- Redshift reach: ET: $z = 2 - 3$, +CE: $z \simeq 9$, +THESEUS: $z \simeq 3.4$



- Number of GW+GRB detections is orders of magnitude smaller than GW detections
 - GRB detector sensitivity is limited to smaller redshifts than GW detector threshold
 - GRB detection number “saturates”: insufficient dedicated GRB/optical/IR telescopes

Future Perspectives

GW Luminosity Distance and Cosmic Inhomogeneities

- GW luminosity distance:

$$\tilde{h}_A \sim \frac{1}{d_L^{gw}(z)}, \quad \text{with} \quad d_L^{gw}(z) = d_L^{em}(z) \exp\left(-\int_0^z \frac{dz'}{1+z'} \delta(z')\right)$$

- Useful parametrisation:

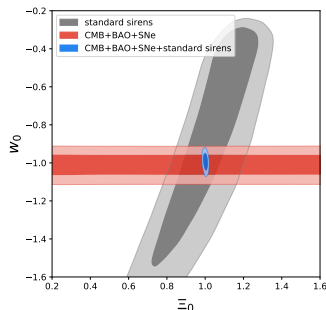
$$\frac{d_L^{gw}(z)}{d_L^{em}(z)} = \Xi_0 + \frac{1}{(1+z)^n} (1 - \Xi_0)$$

- The dipole of d_L^{EM} measures $H(z)$
[Bonvin, Durrer, Kunz (2006)]

- How the dipole of d_L^{gw} measures $H(z)$ and $\delta(z)$?
- By how much do the (forecast) constraints improve?

- Effects of cosmic inhomogeneities

- How do linear FLRW perturbations affect d_L^{gw} ?



Thank you!



[NASA APOD]